MODIS Normalized Water-leaving Radiance
Algorithm Theoretical Basis Document
(MOD 18)
Version 5

Submitted by

Howard R. Gordon and Kenneth J. Voss
Department of Physics
University of Miami
Coral Gables, FL 33124

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Preface

This algorithm theoretical basis document (ATBD) describes the algorithm for retrieving the normalized water-leaving radiance (reflectance) from MODIS imagery. It replaces Version 0 which was submitted on July 30, 1993, Version 1 submitted February 28, 1994, Version 2 submitted November 1, 1994, Version 3 submitted August 15, 1996, and Version 4 submitted April 30, 1999. Version 1 was peer reviewed in the spring of 1994 and reviewer suggestions were incorporated into Version 2. Version 3 covered additional developments between 1994 and 1996 and was peer reviewed in November of 1996. Version 4 incorporates the progress of studies relevant to the algorithm since Version 3. Version 5 describes the state of the algorithms at the close of the contract. Possible algorithm enhancements, as well as outstanding issues that require further research, are identified in this document.

The basic algorithm described here has been used to process SeaWiFS imagery (since its launch in 1997), with some SeaWiFS-specific modifications. Experience gained with SeaWiFS imagery has been invaluable for assessing the performance of the algorithm. The algorithm has been used in MODIS ocean processing for both Terra and Aqua; however, it does not reflect any changes made by the Ocean Color Discipline Processing Group at GSFC for processing Aqua data.

Chapters 1–4 describe the algorithm in its present form, and also detail outstanding issues that require further work. Chapter 5 describes possible enhancements to the code to deal with these issues.

1.0 Introduction

Following the work of Clarke, Ewing and Lorenzen [1970] showing that the chlorophyll concentration in the surface waters of the ocean could be deduced from aircraft measurements of the spectrum of upwelling light from the sea — the “ocean color” — NASA launched the Coastal Zone Color Scanner (CZCS) on Nimbus-7 in late 1978 [Gordon et al., 1980; Hovis et al., 1980]. The CZCS was a proof-of-concept mission with the goal of measuring ocean color from space. It was a scanning radiometer that had four bands in the visible at 443, 520, 550, and 670 nm with bandwidths of 20 nm, one band in the near infrared (NIR) at 750 nm with a bandwidth of 100 nm, and a thermal infrared band (10.5 to 12.5 μm) to measure sea surface temperature. The four visible bands possessed high radiometric sensitivity (well over an order of magnitude higher than other sensors designed for earth resources at that time, e.g., the MSS on the Landsat series) and were specifically designed for ocean color. The CZCS experience demonstrated the feasibility of the measurement of phytoplankton pigments, and possibly even productivity [Morel and André, 1991; Platt and Sathyendranath, 1988], on a global scale. This feasibility rests squarely on two observations: (1) there exists a more or less universal relationship between the color of the ocean and the phytoplankton pigment concentration for most open ocean waters; and (2) it is possible to develop algorithms to remove the interfering effects of the atmosphere from the imagery. In this document we will describe the basis of the algorithm for removing the atmospheric effects from MODIS imagery over the ocean to derive the normalized water-leaving radiance in the visible. The process of deriving the normalized water-leaving radiance from imagery of the oceans is usually termed atmospheric correction.

1.1 The Normalized water-leaving radiance

The normalized water-leaving radiance, \( [L_w]_N \), was defined by Gordon and Clark [1981] through

\[
L_w(\lambda) = a^{-2} [L_w(\lambda)]_N \cos \theta_0 \exp \left[- \left( \frac{\tau_r(\lambda)}{2} + \tau_O(\lambda) \right) \left( \frac{1}{\cos \theta_0} \right) \right],
\]

where \( L_w(\lambda) \) is the radiance backscattered out of the water at a wavelength \( \lambda \), \( \tau_r(\lambda) \), \( \tau_O(\lambda) \) are the...
optical thicknesses of the atmosphere associated with molecular (Rayleigh) scattering and Ozone absorption, respectively, and $a_{\odot}$ is the earth-sun distance in AU. $\theta_0$ is the solar zenith angle. The normalized water-leaving radiance is approximately the radiance that would exit the ocean in the absence of the atmosphere, with the sun at the zenith, at the mean earth-sun distance (1 AU).

This definition was motivated by the desire to remove, as much as possible, the effects of the atmosphere and the solar zenith angle from $L_w(\lambda)$; however, Morel and Gentili [1993] have shown that a residual dependence on $\theta_0$ remains in $[L_w(\lambda)]_N$ (See Section 3.1.1.13.4). The normalized water-leaving radiance is used in other algorithms to derive nearly all of the MODIS ocean products, e.g., the chlorophyll concentration. As such, it plays a central role in the application of MODIS imagery to the oceans.

In the remainder of this document, for the most part, we will abandon the use of radiance in the description of the algorithm in favor of reflectance. The reflectance $\rho$ associated with a radiance $L$ is defined to be $\pi L/F_0 \cos \theta_0$, where $F_0$ is the extraterrestrial solar irradiance, and $\theta_0$ is the solar zenith angle, i.e., the angle between the line from the pixel under examination to the sun and the local vertical. Reflectance is favored because it may be possible to more accurately calibrate MODIS in reflectance rather than radiance. The desired normalized water-leaving radiance can easily be converted to normalized water-leaving reflectance $[\rho_w]_N$ through

$$[\rho_w]_N = \frac{\pi}{F_0} [L_w]_N,$$

(2)

where $F_0$ is the mean extraterrestrial solar irradiance at the mean earth sun distance, i.e., $F_0 = a_{\odot}^2 F_0$. Then Eq. (1) becomes

$$\rho_w(\lambda) = [\rho_w(\lambda)]_N \exp \left[ - \left( \frac{\tau_r(\lambda)}{2} + \tau_O(\lambda) \right) \left( \frac{1}{\cos \theta_0} \right) \right] = [\rho_w(\lambda)]_N t(\theta_0, \lambda),$$

(3)

where $t(\theta_0, \lambda)$ is the CZCS approximation to the diffuse transmittance of the atmosphere (See Section 3.1.1.5). Thus, retrieving $[\rho_w]_N$ is equivalent to retrieving $[L_w]_N$. The factor $\pi/F_0$ in Eq. (2) is $\approx 0.017$ at 443 and 555 nm. It should be noted that some algorithms use “remote sensing reflectance” ($R_{rs} = L_w/E_d$, where $E_d$ is the downward irradiance just above the sea surface) rather than $[\rho_w]_N$ [Lee et al., 1994; Lee et al., 1996]; however, to a good approximation $[\rho_w]_N = \pi R_{rs}$. 
1.2 Outline of the Document

This document is structured in the following manner. First we provide background on the algorithm’s role in MODIS products, explain why atmospheric correction is necessary and difficult, and discuss the characteristics of MODIS and SeaWiFS that make atmosphere correction possible. In the main body of the document we develop the proposed algorithm in detail, test it with simulated data, and then discuss the remaining research problems and issues. Next, we provide our present implementation of the algorithm. Finally, we describe possibilities for enhancement of the algorithm.
2.0 Overview and Background Information

The purpose of retrieving the normalized water-leaving reflectances \([\rho_w(\lambda)]_N\) is that they are required inputs into algorithms for recovering most of the MODIS ocean products. In this sense they are fundamental to nearly all of the MODIS ocean applications. The accuracy of these products rests squarely on the accuracy of the retrieval of \([\rho_w(\lambda)]_N\).

2.1 Experimental Objectives

The ultimate objective of the application of MODIS imagery over the ocean is to study the primary production, and its spatial and temporal variation, of the oceans on a global scale to better understand the ocean’s role in the global carbon cycle. A required component in the estimation of primary productivity is the concentration of chlorophyll \(a\). Estimation of the concentration of chlorophyll \(a\) from MODIS imagery requires the normalized water-leaving reflectance. An example of how this is accomplished is provided by the CZCS. Figure 1 provides \([\rho_w(\lambda)]_N\) at \(\lambda = 443\) and 550 nm as a function of the pigment concentration (the sum of the concentrations of chlorophyll \(a\) and its degradation product phaeophytin \(a\)) in the water. Figure 2 gives the algorithm used to estimate the pigment concentration from \([\rho_w(443)]_N/[\rho_w(550)]_N\). It can be well represented by

\[
\log_{10} 3.33C = -1.2 \log_{10} R + 0.5(\log_{10} R)^2 - 2.8(\log_{10} R)^3, 
\]

(4)
with $R = 0.5[\rho_w(443)]_N/[\rho_w(550)]_N$. Thus, the pigment concentration $C$ is directly related to the radiance ratios. Analysis [Gordon, 1990] suggests that the pigment concentration can be derived from the radiance ratio with an error of $\sim \pm 20\%$. Because of relationships such as these that relate bio-optical parameters to $[\rho_w(\lambda)]_N$, the normalized water-leaving reflectance plays a central role in the application of ocean color imagery to the oceans, and atmospheric correction becomes a critical factor in determining the fidelity with which bio-optical parameters can be retrieved. When ratios of $[\rho_w]_N$’s are used in computations, as in Eq. (4), small errors of the same sign in the two $[\rho_w]_N$’s will tend to cancel. In most cases the errors in the retrieval of the two $[\rho_w]_N$’s in such ratios will have the same sign.

2.2 Historical Perspective

The algorithm for the retrieval of the $[\rho_w]_N$’s from MODIS imagery follows from experience gained with the CZCS. Its purpose is to identify and remove the component of the radiance measured at the sensor that arises from molecular and aerosol scattering in the atmosphere, as well as reflection from the air-sea interface. Since the aerosol concentration and properties are variable in space and time, their effects are unknown a priori. The radiometric sensitivity of the CZCS
was sufficiently low that it was not necessary to deal with the full complexities of multiple scattering. However, with the increased sensitivity of SeaWiFS and MODIS, multiple scattering in the atmosphere becomes a central issue in the retrieval algorithms for $[\rho_w]_N$. Examples of important secondary issues not addressed in the CZCS algorithm are the presence of whitecaps on the sea surface and the influence of earth curvature on the algorithm.

2.3 Instrument Characteristics

The MODIS and SeaWiFS instruments have similar characteristics (Table 1). The main differences are that MODIS has spectral bands that are half to one-forth as wide as SeaWiFS, MODIS is 12-bit digitized as opposed to 10-bit for SeaWiFS, and MODIS has approximately twice the SNR. The positions of the spectral bands are similar.

Of critical importance for the retrieval of $[\rho_w]_N$ are spectral bands 7 and 8 (745–785 nm and 845–885 nm, respectively) on SeaWiFS and bands 15 and 16 (745–755 nm and 857–872 nm, respectively) on MODIS. Because of the strong absorption by liquid water, virtually no light will exit the ocean in these bands, except in the most turbid coastal waters, so all of the radiance measured by the sensor originates from the scattering of solar irradiance by the atmosphere and the sea surface. These bands can therefore be used to assess the atmospheric effects. Band 6 on SeaWiFS (660–680 nm) and band 13 on MODIS (662–672 nm) can also be utilized in waters with pigment concentration $\lesssim 0.5 - 1.0$ mg/m$^3$, but probably not in coastal waters. Band 7 on SeaWiFS overlaps the $O_2$ “A” absorption band centered at $\sim$ 762 nm. The influence of this absorption band on SeaWiFS atmospheric correction has been studied by Ding and Gordon [1995]; however, as MODIS band 15 does not overlap the $O_2$ absorption, we shall not discuss this issue further in this document.

The application of these bands to atmospheric correction is straightforward in principle: one assesses the contribution of the atmosphere in the NIR and extrapolates it into the visible.
3.0 Algorithm Description

This section provides a description of the entire algorithm. Before beginning, a few preliminaries are useful. Table 1 provides the MODIS radiometric specifications in terms of reflectance for a solar zenith angle of 60° and viewing near the scan edge. For convenience we also provide the “noise equivalent reflectance” (NEΔρ) for the SeaWiFS and CZCS bands closest to the given MODIS band. Note that MODIS is typically 2-3 times more sensitive than SeaWiFS, which in turn is approximately twice as sensitive as CZCS. Exceptions are the MODIS bands 13 and 14 which are to be used to measure the chlorophyll a fluorescence near 683 nm [Neville and Gower, 1977]. These bands are ~ 6 times more sensitive than SeaWiFS and ~ 12 times more sensitive than CZCS. The table also provides the typical top-of-the-atmosphere reflectance ρt and the normalized water-leaving reflectance [ρw]N for a very low pigment concentration (Sargasso Sea in summer) [Gordon and Clark, 1981]. Note that [ρw]N is only a small fraction of ρt. To recover [ρw]N in the blue (443 nm) for these waters with an error < 5% requires an atmospheric correction of ~ ±0.001 to ±0.002 in reflectance, i.e., about five to ten times the NEΔρ. This is our goal for MODIS band 9. It is shown later that when this goal is met, the error in [ρw]N at 550 nm will be ~ 3–4 times smaller than that at 443 nm. In this case, Figure 1 shows that the error in the ratio R in Eq. (4)
usually will be dominated by error in $[\rho_w]_N$ at 443 nm, the exception being very low values of $C$.

### 3.1 Theoretical Description

In this section we provide the theoretical basis of the algorithm. We begin by discussing the basic physics of the algorithm, starting with single scattering and progressing into the multiple scattering regime. Then several auxiliary algorithms, e.g., a whitecap removal algorithm, a sun glitter masking algorithm, etc., are presented. Next, the required ancillary data are itemized, the approximations used in the development of the algorithm are examined, and the remaining research issues are discussed. Finally, an implementation of the algorithm is described and the effects of MODIS radiometric calibration uncertainty is considered.

#### 3.1.1 Physics of the Algorithm

The radiance received by a sensor at the top of the atmosphere (TOA) in a spectral band centered at a wavelength $\lambda_i$, $L_t(\lambda_i)$, can be divided into the following components: $L_{\text{path}}(\lambda_i)$ the radiance generated along the optical path by scattering in the atmosphere and by specular reflection of atmospherically scattered light (skylight) from the sea surface; $L_g(\lambda_i)$ the contribution arising from specular reflection of direct sunlight from the sea surface (sun glitter); $L_{\text{wc}}(\lambda_i)$ the contribution arising from sunlight and skylight reflecting from individual whitecaps on the sea surface; and $L_w(\lambda_i)$ the desired water-leaving radiance; i.e.,

$$L_t(\lambda_i) = L_{\text{path}}(\lambda_i) + T(\lambda_i)L_g(\lambda_i) + t(\lambda_i)L_{\text{wc}}(\lambda_i) + t(\lambda_i)L_w(\lambda_i).$$

$L_{\text{wc}}$ and $L_w$ are area-weighted averages of the radiance leaving whitecap-covered and whitecap-free areas of the surface, respectively. In this equation, $T$ and $t$ are the direct and diffuse, transmittance of the atmosphere, respectively. The diffuse transmittance is appropriate for the water-leaving radiance and the whitecap radiance as they have near-uniform angular distribution. It is discussed in detail in Section 3.1.1.5. In contrast, to the diffuse transmittance, the direct transmittance is appropriate when the angular distribution of the radiance is approximately a Dirac delta function. As the sun glitter is highly directional (except at high wind speeds), its transmittance is approximated by the direct transmittance. The direct transmittance is given by

$$T(\theta_v, \lambda) = \exp \left[ - \left( \tau_\iota(\lambda) + \tau_{O_2}(\lambda) + \tau_a(\lambda) \right) \left( \frac{1}{\mu_v} \right) \right],$$
where $\mu_v = \cos \theta_v$, $\theta_v$ is the angle the exiting radiance makes with the upward normal at the TOA, and $\tau_r$, $\tau_a$, and $\tau_{O_2}$ are, respectively, the Rayleigh, aerosol, and Ozone optical thicknesses. In this equation, we have ignored the possibility of weak continuum (in the atmospheric windows) absorption by water vapor [Eldridge, 1967; Tomasi, 1979a; Tomasi, 1979b] due to the extreme difficulty in separating the direct effect of water vapor absorption from the indirect effect that water vapor will have on the extinction of hygroscopic aerosols [Fraser, 1975]. Converting to reflectance, Eq. (5) becomes

$$\rho_t(\lambda_i) = \rho_{\text{path}}(\lambda_i) + T(\lambda_i)\rho_g(\lambda_i) + t(\lambda_i)\rho_{\text{wv}}(\lambda_i) + t(\lambda_i)\rho_w(\lambda_i).$$  

(6)

Thus, from the measured $\rho_t(\lambda_i)$ we require an algorithm that provides accurate estimates of $\rho_{\text{path}}(\lambda_i)$, $T(\lambda_i)\rho_g(\lambda_i)$, $t(\lambda_i)\rho_{\text{wv}}(\lambda_i)$, and $t(\lambda_i)$. Near the sun’s glitter pattern $T(\lambda_i)\rho_g(\lambda_i)$ is so large that the imagery is virtually useless and must be discarded. A sun glitter mask to remove seriously contaminated pixels is described in Section 3.1.1.7. Away from the glitter pattern, i.e., where values of $T(\lambda_i)\rho_g(\lambda_i)$ become negligibly small, the largest of the remaining terms, and most difficult to estimate, is $\rho_{\text{path}}(\lambda_i)$. This difficulty is principally due to the aerosol by virtue of its highly variable concentration and optical properties. Thus, we concentrate on this term first, then consider the rest, and the ancillary data required to operate the algorithm.

In general, $\rho_{\text{path}}$ can be decomposed into several components:

$$\rho_{\text{path}} = \rho_r(\lambda) + \rho_a(\lambda) + \rho_{ra}(\lambda)$$  

(7)

where $\rho_r$ is the reflectance resulting from multiple scattering by air molecules (Rayleigh scattering) in the absence of aerosols, $\rho_a$ is the reflectance resulting from multiple scattering by aerosols in the absence of the air, and $\rho_{ra}$ is the interaction term between molecular and aerosol scattering [Antoine and Morel, 1998; Deschamps, Herman and Tanre, 1983]. The term $\rho_{ra}$ accounts for the interaction between Rayleigh and aerosol scattering, e.g., photons first scattered by the air then scattered by aerosols, or photons first scattered by aerosols then air, etc. This term is zero in the single scattering case, in which photons are only scattered once, and it can be ignored as long as the amount of multiple scattering is small, i.e., at small Rayleigh and aerosol optical thicknesses. We note that given the surface atmospheric pressure (to determine the value of $\tau_r$) and the surface wind speed (to define the roughness of the sea surface), $\rho_r$ can be computed accurately, even accounting for polarization by scattering [Gordon, Brown and Evans, 1988; Gordon and Wang, 1992b].
In modeling the propagation of radiance in the ocean-atmosphere system, we assume that the atmosphere can be considered to be a vertically stratified, plane parallel medium. The medium is described by providing the extinction coefficient, $c(h)$, as a function of altitude $h$, the scattering phase function for scattering of radiance from direction $\hat{\xi}'$ to direction $\hat{\xi}$, $P(h;\hat{\xi}' \rightarrow \hat{\xi})$, and the single scattering albedo $\omega_0(h)$. Replacing $h$ by the optical depth $\tau$ defined as

$$\tau(h) = \int_h^\infty c(h) \, dh,$$

the propagation of radiance in such a medium in the scalar approximation (the polarization state of the radiance, and the change in polarization induced by the scattering process is ignored) is governed by the radiative transfer equation (RTE):

$$\hat{\xi} \cdot \hat{n} \frac{dL(\tau, \hat{\xi})}{d\tau} = -L(\tau, \hat{\xi}) + \frac{\omega_0(\tau)}{4\pi} \int_{all \hat{\xi}'} P(\tau; \hat{\xi}' \rightarrow \hat{\xi}) L(\tau, \hat{\xi}') \, d\Omega(\hat{\xi}'),$$

where $d\Omega(\hat{\xi}')$ is the differential of solid angle around the direction $\hat{\xi}'$, and $\hat{n}$ is a unit vector in the nadir direction (normal to the sea surface pointed down). Analytical solutions to the RTE are possible only in the simplest case, e.g., $\omega_0 = 0$, so normally one must be satisfied with numerical solutions.

In principal this equation must be solved for the coupled ocean-atmosphere system; however, because of the very low albedo of the ocean (Table 1) it is not necessary to consider the coupling [Gordon, 1976], i.e., we can ignore processes such as photons being backscattered out of the water and then scattered back into the water and backscattered out again, etc. The water-leaving radiance simply propagates to the sensor (i.e., $\rho_{path}$ is independent of $\rho_w$ in Eq. (6)) and the ocean and atmosphere decouple, hence, we need only understand the solution of the atmospheric part of the problem, i.e., an atmosphere bounded by a Fresnel-reflecting ocean surface.

As the goal of atmospheric correction is to retrieve $\rho_w(443)$ with an uncertainty less than $\pm 0.002$, i.e., $\sim \pm 0.6\%$ of $\rho_t(443)$ (Table 1), for the development and testing of the algorithm we require solutions of the RTE that yield $\rho_t$ with an uncertainty $\ll 0.6\%$. For the bulk of the work described here, $\rho_t$ was generated using the successive-order-of-scattering method [van de Hulst, 1980]. To understand the accuracy of this code, a second code was developed employing Monte Carlo methods. Typically, the values of $\rho_t$ produced by the two codes differ by less than 0.05%. Thus, either code meets the accuracy required for this work.
We will assume, as justified earlier, that $\rho_w = 0$ in the NIR (but, see Section 3.1.1.9). The problem we are required to solve can then be stated in a simple manner: given the satellite measurement of the radiance (reflectance) of the ocean-atmosphere system in the NIR, predict the radiance (reflectance) that would be observed in the visible. The difference between the predicted and the measured radiance (reflectance) of the ocean-atmosphere system is the water-leaving radiance (reflectance) transmitted to the top of the atmosphere.

### 3.1.1.1 The Single Scattering Approximation

It is useful to consider $\rho_{\text{path}}(\lambda_i)$ in the the limit that the optical thickness of the atmosphere is $\ll 1$. We refer to this as the single-scattering limit. Formulas for the reflectances in this limit are referred to as the single-scattering approximation. The CZCS algorithm was based on the single-scattering approximation. In this approximation the path reflectance reduces to

$$\rho_{\text{path}}(\lambda_i) = \rho_r(\lambda_i) + \rho_{\text{as}}(\lambda_i),$$

with the aerosol contribution $\rho_{\text{as}}$ provided by

$$\rho_{\text{as}}(\lambda) = \omega_a(\lambda) \tau_a(\lambda) p_a(\theta_v, \phi_v; \theta_0, \phi_0; \lambda) / 4 \cos \theta_v \cos \theta_0,$$

$$p_a(\theta_v, \phi_v; \theta_0, \phi_0; \lambda) = P_a(\Theta_-, \lambda) + \left( r(\theta_v) + r(\theta_0) \right) P_a(\Theta_+, \lambda),$$

$$\cos \Theta_\pm = \pm \cos \theta_0 \cos \theta_v - \sin \theta_0 \sin \theta_v \cos(\phi_v - \phi_0),$$

where $P_a(\Theta, \lambda)$ is the aerosol scattering phase function for a scattering angle $\Theta$, $\omega_a$ is the aerosol single scattering albedo, and $r(\alpha)$ is the Fresnel reflectance of the interface for an incident angle $\alpha$. The angles $\theta_0$ and $\phi_0$ are, respectively, the zenith and azimuth angles of a vector from the point on the sea surface under examination (pixel) to the sun, and likewise, $\theta_v$ and $\phi_v$ are the zenith and azimuth angles of a vector from the pixel to the sensor. These are measured with respect to the upward normal so $\theta_v$ and $\theta_0$ are both less than $90^\circ$ in these equations. In what follows usually (but not always) we take the orientation of the coordinate system so that $\phi_0 = 0$.

Following the approach described above, we assume we are given the the path reflectance at two bands in the NIR at $\lambda_s$ and $\lambda_l$, where the subscript “s” stands for short and “l” for long, e.g., for MODIS $\lambda_s = 748$ nm and $\lambda_l = 869$ nm. [Note that since we are ignoring sun glitter
$T(\lambda_i)\rho_g(\lambda_i)$, this implies that $t(\lambda_i)\rho_{w,c}(\lambda_i)$ has also been provided.] Given estimates of the surface atmospheric pressure and the wind speed (ancillary data), $\rho_r(\lambda)$ can be computed precisely and therefore $\rho_{as}(\lambda_s)$ and $\rho_{as}(\lambda_t)$ can be determined from the associated measurements of $\rho_{path}$ at $\lambda_s$ and $\lambda_t$. This allows estimation of the parameter $\varepsilon(\lambda_s, \lambda_t)$:

$$\varepsilon(\lambda_s, \lambda_t) \equiv \frac{\rho_{as}(\lambda_s)}{\rho_{as}(\lambda_t)} = \frac{\omega_a(\lambda_s)\tau_a(\lambda_s)\rho_a(\theta_v, \phi_v; \theta_0, \phi_0; \lambda_s)}{\omega_a(\lambda_t)\tau_a(\lambda_t)\rho_a(\theta_v, \phi_v; \theta_0, \phi_0; \lambda_t)}.$$  \hspace{1cm} (10)

If we can compute the value of $\varepsilon(\lambda_i, \lambda_t)$ for the MODIS band at $\lambda_i$ from the value of $\varepsilon(\lambda_s, \lambda_t)$, this will yield $\rho_{as}(\lambda_i)$, which, when combined with $\rho_r(\lambda_i)$, provides the desired $\rho_{path}(\lambda_i)$. Clearly, the key to this procedure is the estimation of $\varepsilon(\lambda_i, \lambda_t)$ from $\varepsilon(\lambda_s, \lambda_t)$.$^1$

### 3.1.1.1.1 The CZCS Algorithm

The atmospheric correction algorithm for CZCS was described in detail in Evans and Gordon [1994]. Briefly, the basic CZCS algorithm [Gordon, 1978; Gordon and Clark, 1980] was based on single scattering; however, $\rho_r(\lambda_i)$ was computed accurately, including the effects of multiple scattering and polarization [Gordon, Brown and Evans, 1988]. As there were no NIR bands, the algorithm could not be operated as described in Section 3.1.1.1. However, Table 1 shows that $\rho_{w,}(670)$ can generally be taken to be zero (at least if the pigment concentration is low enough). Thus, the single scattering algorithm was typically operated with $\lambda_t = 670$ nm and $\rho_{w,}(\lambda_t) = 0$. Unfortunately, there was no shorter wavelength ($\lambda_s$) for which $\rho_{w} = 0$, so in the processing of the CZCS global data set [Feldman et al., 1989] $\varepsilon(\lambda_i, \lambda_s)$ was set equal to unity. This is characteristic of a maritime aerosol at high relative humidity.

For sufficiently low $C$ values, Figure 1 (right panel) suggests that $[\rho_{w}(550)]^N$ is approximately constant. This fact can be used to estimate $\varepsilon(550, 670)$ for such “clear water” regions [Gordon and Clark, 1981] in a scene, allowing a basis for extrapolation to 520 and 443 nm. If the resulting $\varepsilon(\lambda_i, \lambda_t)$ is then assumed to be valid for the entire image, retrieval of $[\rho_{w}(\lambda_i)]^N$ and $C$ can be effected for the image. This is the procedure used by Gordon et al. [1983] in the Middle Atlantic Bight. Figure 3 provides an example of atmospheric correction in this region. Note that the intense

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$^1$ It is important to note that $p_a$ in the definition of $\varepsilon(\lambda_s, \lambda_t)$ is not $P_a(\Theta)$ as has implicitly assumed by some authors, i.e., it involves both forward $P_a(\Theta_+)$ and backward $P_a(\Theta_-)$ scattering. Since $P_a(\Theta)$ is strongly peaked in near-forward directions (e.g., see Figure 10), the surface-reflected term $P_a(\Theta_+)$ makes a significant contribution to $\rho_{as}(\lambda)$, i.e., as much as 30% in some geometries.
haze layer seen in $L_t(443)$ is absent from $L_w(443)$, revealing the rich underlying horizontal structure in water-leaving reflectance. Unfortunately, there are serious difficulties applying this procedure routinely. For example, the image of interest may contain no “clear water,” the $\varepsilon$’s may vary over the image because of variations in aerosol type, and the pigment concentration may not be small enough to take $\rho_w = 0$ at 670 nm. Morel and his co-workers have developed a promising approach for dealing these problems in Case 1 waters [André and Morel, 1991; Bricaud and Morel, 1987] based on the ideas of Smith and Wilson [1981]. This involves utilizing a modeled relationship between $C$ and $[\rho_w(\lambda_1)]_N$. Fortunately, for the sensors of concern in this document (SeaWiFS and MODIS), these problems are (usually) circumvented by virtue of the additional spectral bands with $\lambda > 700$ nm. However, the heart of the Morel approach – modeling both the reflectance of the water and the aerosols – forms the basis of algorithms for use in the presence of strongly absorbing aerosols or Case 2 waters [Chomko and Gordon, 1998; Gordon, Du and Zhang, 1997b].
3.1.1.1.2 Application to MODIS

As the key to application of the single scattering algorithm to the EOS era sensors is the extrapolation from $\varepsilon(\lambda_s, \lambda_l)$ to $\varepsilon(\lambda_i, \lambda_l)$, which involves more than a factor of two in wavelength, it is important to try to gain some insight into the possible spectral behavior of $\varepsilon(\lambda_i, \lambda_l)$. This has been attempted by Gordon and Wang [1994a] by computing $\varepsilon(\lambda_i, \lambda_l)$ for several aerosol models. Briefly, they used aerosol models that were developed by Shettle and Fenn [1979] for LOWTRAN-6 [Kenizys et al., 1983]. These models consist of particles distributed in size according to combinations of log-normal distributions. The size frequency distribution $n(D)$ is given by

$$n(D) = \sum_{i=1}^{2} n_i(D),$$

with

$$n_i(D) = \frac{dN_i(D)}{dD} = \frac{N_i}{\log_{10}(10) \sqrt{2\pi \sigma_i D}} \exp \left[ -\frac{1}{2} \left( \frac{\log_{10}(D/D_i)}{\sigma_i} \right)^2 \right],$$

where, $dN_i(D)$ is the number of particles per unit volume between $D$ and $D + dD$, $D_i$ and $\sigma_i$ are the median diameter and the standard deviation, respectively, and $N_i$ is the total number density of the $i$th component. Since hygroscopic particles swell with increasing relative humidity (RH), $D_i$ and $\sigma_i$ are functions of RH. The smaller size fraction is a mixture of 70% water soluble and 30% dust-like particles called the Tropospheric aerosol. It has been used to represent the aerosols within the free troposphere above the boundary-layer [Shettle and Fenn, 1979]. The refractive index $m$ for this component at 555 nm ranges from $1.53 - 0.0066i$ at RH = 0, to $1.369 - 0.0012i$ at RH = 98%. Thus, as the particles absorb more water, the real part of their refractive index approaches that of water and the imaginary part (proportional to the absorption coefficient) decreases. Because of the moderate imaginary part of the refractive index, these particles have weak absorption and $\omega_a$ ranges from 0.959 to 0.989 for $0 \leq RH \leq 98\%$ at 555 nm. The modal diameter of this component is always $< 0.1 \, \mu m$. The larger fraction is a sea salt-based component, the “Oceanic” aerosol. Its modal diameter varies from about 0.3 to 1.2 $\mu m$ as RH varies from 0 to 98%. Its index of refraction is essentially real (imaginary part $\sim 10^{-8}$), so $\omega_a = 1$. Like the tropospheric aerosol its real part ranges from 1.5 at RH = 0 to 1.35 at RH = 98%.

From these components, three basic models were constructed: the Tropospheric model with no Oceanic contribution; the Maritime model for which 99% of the particles have the Tropospheric
characteristics and 1% the Oceanic; and the Coastal model for which 99.5% of the particles have the Tropospheric characteristics and 0.5% the Oceanic. Gordon and Wang [1994a] introduced the Coastal aerosol model to represent the aerosol over the oceans nearer the coast (less Oceanic contribution). The properties of all three aerosol models depend on the wavelength and relative humidity. With the values of $D_i$, $\sigma_i$, and $m_i(\lambda)$ taken from Shettle and Fenn [1979], Mie theory was used to calculate the optical properties for all three models for the SeaWiFS and MODIS spectral bands at different relative humidities.

Sample results for $\varepsilon(\lambda_i, \lambda_l)$, where $\lambda_l$ is taken to be 865 nm (SeaWiFS), are presented in Figure 4 (left panel). These computations suggest that there should be a strong variation of $\varepsilon$ with aerosol model and RH. The increase in particle size (due to swelling) with increasing RH clearly reduces the spectral variation of $\varepsilon$. The spectral variation of $\varepsilon$ is due in large part to the spectral variation of the aerosol optical thickness, $\tau_a$; however, additional variation is produced by the aerosol phase function. Note that Figure 4 is plotted in a format that would yield a straight line under the hypothesis that $\varepsilon(\lambda_i, \lambda_l) = \exp[c(\lambda_l - \lambda_i)]$, where $c$ is a constant. This shows that over the range 412–865 nm $\varepsilon(\lambda_i, \lambda_l)$ can be considered to be an exponential function of $\lambda_l - \lambda_i$, for the Shettle and Fenn [1979] models. Wang and Gordon [1994b] have used this fact to extend the CZCS algorithm.

![Figure 4](image-url)

Figure 4. $\varepsilon(\lambda, 865)$ for nadir viewing with $\theta_0 = 60^\circ$. Left panel: Maritime, Coastal, and Tropospheric aerosol models (the RH values are 50, 80, and 98% from the upper to the lower curves). Right panel: Haze C models (the open symbols are for models with little or no absorption, while the filled symbols are for absorbing models).
for use with SeaWiFS and MODIS.

We now examine the accuracy of this CZCS-type single-scattering algorithm based on an assumed exponential spectral variation of $\varepsilon(\lambda_i, \lambda_f)$. For this purpose, we simulated atmospheres using an array of aerosol models. First, the aerosol optical properties were taken from the Tropospheric, Coastal, and Maritime models at RH = 80\%, denoted, respectively, as T80, C80, and M80. Then, we simulated the aerosol using the Shettle and Fenn [1979] Urban model at RH = 80\% (U80). This model shows strong absorption. In addition to the water soluble and dust-like particles of the Tropospheric model, the Urban model contains soot-like particles (combustion products). Also, the Urban model has a second, larger particle, mode in addition to that of the Tropospheric model. At 865 nm the Mie theory computations yielded, $\omega_a = 0.9934$, 0.9884, and 0.9528, respectively, for the Maritime, Coastal, and Tropospheric models (RH = 80\%), while in contrast, $\omega_a = 0.7481$ for the Urban model. Here, the Urban model is intended to represent aerosols that might be present over the oceans near areas with considerable urban pollution, e.g., the Middle Atlantic Bight off the U.S. East Coast in summer. Finally, we examined aerosols with a different analytical form for the size distribution [Junge, 1958]:

$$n(D) = \frac{dN(D)}{dD} = K,$$

$$= K\left(\frac{D_1}{D}\right)^{\nu+1}, \quad D_0 < D < D_1,$$

$$= K\left(\frac{D_2}{D}\right)^{\nu+1}, \quad D_1 < D < D_2,$$

$$= 0, \quad D > D_2,$$

with $D_0 = 0.06$ $\mu$m, $D_1 = 0.20$ $\mu$m, and $D_2 = 20$ $\mu$m. Following Deirmendjian [1969] we call these Haze C models. Twelve separate Haze C models were considered: $\nu = 2, 3, \text{ and } 4$, with the refractive index of the particles taken to be that of liquid water (from Hale and Querry [1973]), close to that of the dust component in the Tropospheric model $(1.53 - 0.008i)$, nonabsorbing crystals $(1.50 - 0i)$, and absorbing minerals that might be expected from desert aerosols transported over the oceans [d’Almeida, Koepke and Shettle, 1991]. The spectral behavior of $\varepsilon(\lambda, 865)$ for these models is presented in Figure 4 (right panel). We see that the absorption-free (open symbols) Haze C models display a behavior similar to the Shettle and Fenn models; however, for models with strong absorption (solid symbols) departures are seen, especially for the mineral models for which the imaginary part of the refractive index increases with decreasing $\lambda$. An important observation from Figure 4 (right panel) is that, in general, $\varepsilon(765, 865)$ cannot be utilized to discriminate between
weakly- and strongly-absorbing aerosols with similar size distributions.

Using these aerosol models we generated hypothetical atmospheres with a two-layer structure: the aerosols occupying the lower layer, and all molecular scattering confined to the upper layer. This distribution of aerosols is similar to that typically found over the oceans when the aerosol is locally generated, i.e., most of the aerosol is confined to the marine boundary layer [Sasano and Browell, 1989]. The atmosphere was bounded by a flat (smooth) Fresnel-reflecting sea surface, and all photons that penetrated the interface were assumed to be absorbed in the ocean. The RTE in the scalar approximation was solved for this hypothetical atmosphere using the successive-order-of-

Figure 5. Spectral variation of $\tau_a$. Left panel: Maritime, Coastal, and Tropospheric aerosol models (the RH values are 50, 80, and 98% from the upper to the lower curves). Right panel: Haze C models (the open symbols are for models with little or no absorption, while the filled symbols are for absorbing models).

scattering method [van de Hulst, 1980] to provide pseudo TOA reflectance ($\rho_t$) data. All significant orders of multiple scattering were included. As the surface was assumed to be smooth (no wind), the sun glitter and whitecap terms in Eq. (6) are absent. The simulations of $\rho_t$ were carried out for the following geometries: $\theta_0 = 20^\circ$, $40^\circ$, and $60^\circ$, with $\theta_v \approx 1^\circ$ and $\phi_v - \phi_0 = 90^\circ$, i.e., viewing near the MODIS scan center; and $\theta_0 = 0^\circ$, $20^\circ$, $40^\circ$, and $60^\circ$, with $\theta_v \approx 45^\circ$ and $\phi_v - \phi_0 = 90^\circ$, i.e., viewing near the scan edge. In this manner a wide range of sun-viewing geometries were included. Four wavelengths were considered: $\lambda_1 = 443, 555, 765, \text{ and } 865 \text{ nm.}$ The values used for the aerosol optical thickness at 865 nm, $\tau_a(865)$, were 0.1, 0.2, 0.3, and 0.4. The values of $\tau_a(\lambda_1)$
at the other wavelengths were determined from the spectral variation of the extinction coefficient for each particular model. These are provided in Figure 5. The Haze C models clearly show that the spectral variation of $\tau_a$ is principally determined by the size distribution, with the index of refraction playing only a minor role. Equation (10) suggests that there should be a relationship between $\tau_a(\lambda)/\tau_a(865)$ and $\varepsilon(\lambda, 865)$. Figure 6 provides an example of this for $\theta_0 = 60^\circ$ and nadir viewing, i.e., the same geometry as in Figure 4, with $\varepsilon(765, 865)$ used rather than $\varepsilon(\lambda, 865)$. Thus, for a given $\tau_a(865)$, $\tau_a(443)$ will generally increase with increasing $\varepsilon(765, 865)$. This will be useful in interpreting the results described below.

As the true $\rho_w(\lambda_i)$ was taken to be zero in the pseudo data (all photons entering the water were absorbed), the error in atmospheric correction, i.e., the error in the retrieved water-leaving reflectance, $\Delta(t\rho_w)$, is just the error in the predicted path radiance. This is

$$
\Delta(t\rho_w(\lambda_i)) = \rho_t(\lambda_i) - \rho_{\text{path}}(\lambda_i) = \rho_t(\lambda_i) - \rho_r(\lambda_i) - \varepsilon^{(c)}(\lambda_i, \lambda_i)\rho_{\text{as}}(\lambda_i),
$$

(12)

where $\varepsilon^{(c)}(\lambda_i, \lambda_i)$ is the estimated value of $\varepsilon(\lambda_i, \lambda_i)$ assuming an exponential variation with $\lambda_i$:

$$
\varepsilon^{(c)}(\lambda_i, \lambda_i) \equiv \exp[c(\lambda_i - \lambda_i)] = \exp \left[ \left( \frac{\lambda_i - \lambda_i}{\lambda_i - \lambda_s} \right) \log_e \left( \frac{\rho_{\text{as}}(\lambda_i)}{\rho_{\text{as}}(\lambda_i)} \right) \right].
$$

![Figure 6. Relationship between $\varepsilon(765, 865)$ and $\tau_a(443)/\tau_a(865)$ for the various aerosol models with $\theta_0 = 60^\circ$ and nadir viewing.](image)
Normalized Water-leaving Radiance ATBD, Version 5 May 2004

$\rho_r(\lambda_i)$ was computed using the same radiative transfer code, i.e., it includes all effects of multiple scattering, but not polarization. In an actual application, $\rho_r(\lambda_i)$ would be computed using a code that included polarization as well [Gordon, Brown and Evans, 1988]. Figure 7 provides the error in the retrieved normalized water-leaving reflectance, $\Delta[p_w(443)]_N$, for the seven sun-viewing geometries and for $\tau_a(865) = 0.1$ and 0.2. To derive $\Delta[p_w]_N$ from $\Delta t\rho_w$, the approximation for $t$ similar to that used in processing CZCS imagery was utilized (See Section 3.1.1.5). The x-axis in Figure 7, $\varepsilon^{(c)}(765, 865)$, is the estimated value for the indicated model and geometry.

In the absence of aerosol absorption (open symbols), the performance of this simple algorithm is truly remarkable, as Figures 5 (right panel) and 6 show that for $\nu = 4$, $\tau_a(443) \approx 0.35$ and 0.70 for Figure 7 (top panels), respectively. The large negative errors for $\nu = 4$ occur at the scan edge with $\theta_0 = 60^\circ$, i.e., the geometry with the most multiple scattering. For $\nu = 3$ ($\tau_a(443) \sim 0.2$ and 0.4 (Figures 5 and 6 for Figure 7 (top panels), respectively), the retrieved value of $[p_w(443)]_N$ is usually within the acceptable limits.

In the case of absorbing aerosols, the errors are seen to be mostly negative, and to grow rapidly with $\tau_a(443)$. Negative errors are particularly troublesome as they can lead to negative values in the retrieved $[p_w(443)]_N$ when the pigment concentration $\gtrsim 0.5 - 1.0$ mg/m$^3$. The source of the error for absorbing aerosols is twofold. For the Haze C aerosol, it can be seen from Figure 4 (right panel) that, in contrast to the nonabsorbing aerosols, an exponential extrapolation of $\varepsilon(765, 865)$ to $\varepsilon(443, 865)$ would lead to an erroneous overestimation of $\varepsilon(443, 865)$, the single exception being the mineral aerosol with $\nu = 2$. This will cause an overestimation of the aerosol contribution at 443 nm, which in turn will result in a negative error in $[p_w(443)]_N$. In contrast, the extrapolation does work well for T80 (Figure 4, left panel) and, as we shall see later, in this case the error is principally due to multiple scattering, which is strongly influenced by even weak aerosol absorption.

The error in $[p_w(550)]_N$ as related to the associated error in $[p_w(443)]_N$ is provided in Figure 7 (lower panels). The observed improvement in atmospheric correction at 550 compared to 443
nm can be traced to the facts that (1) the $\varepsilon$ determination requires a smaller extrapolation at 550 nm, and (2) there is less multiple scattering at 550 nm as both $\tau_a$ (Figure 5) and $\tau_r$ are smaller. Notably, the error at 550 nm is usually much less than that at 443 nm, there being a tendency for $\Delta[p_w(550)]_N \sim (1/4)\Delta[p_w(443)]_N$, although occasionally $|\Delta[p_w(550)]_N| > |\Delta[p_w(443)]_N|$. Thus, in a pigment ratio algorithm such as Eq. (4), the error at 443 nm would usually be the more significant error in the $R$ ratio.

Figure 7. $\Delta[p_w(443)]_N$ as a function of $\varepsilon^{(c)}(765,865)$ and $\tau_a(865)$ (top) and $\Delta[p_w(550)]_N$ as a function of $\Delta[p_w(443)]_N$ (bottom) for all of the aerosol models and viewing geometries examined in the study. Left panels: $\tau_a(865) = 0.1$. Right panels: $\tau_a(865) = 0.2$. 
It is useful at this point to review the sparse direct observations of the aerosol optical thickness over the oceans. In the open ocean, far from sources of pollution and/or sources of desert aerosols, the atmosphere is very clear. In the Pacific $\tau_a(550)$ is found in the range 0.04 to 0.24 with a mean of 0.13 and Angstrom exponent of 0.56 [Vil éxito et al., 1994], suggesting a mean $\tau_a(865)$ of $\sim 0.1$ and a maximum of $\sim 0.19$. Similar results are obtained for the North Atlantic [Korotaev et al., 1993; Reddy et al., 1990]. In such a region, Lechner et al. [1989] found that there were low concentrations of aerosol in the free troposphere possessing a Haze C-like distribution with an average $\nu$ of $\sim 3.5$, while in the marine boundary layer the concentration was much higher (and highly variable) with an average $\nu$ of $\sim 1.8$, and sometimes even a bimodal size distribution (the large mode presumably resulting from local generation of aerosols by breaking waves). In contrast, in the region of the Atlantic off West Africa subject to Saharan dust, Reddy et al. [1990] found a mean $\tau_a(550)$ of 0.4 with $\tau_a(865) \approx 0.3$, in agreement with the observations of Korotaev et al. [1993], $\tau_a(550) \sim 0.3$ to 0.5. In areas subject to urban pollution, even higher optical thicknesses are observed, e.g., Reddy et al. [1990] found a mean $\tau_a(550) \approx 0.5$ and $\tau_a(865) \approx 0.3$ in the Western North Atlantic in summer when trajectory analysis suggested the origin of the air mass was the North American continent.

Thus, direct observation suggests that over the open ocean most of the aerosol is in the marine boundary layer and, for mean conditions $\tau_a(865) \approx 0.1$. Furthermore, the size distribution is either similar to Haze C with $\nu \approx 2.5$ or bimodal like M80 or C80. Such aerosols would have $\varepsilon(765, 865) < 1.1$ (Figure 6). Figure 7 (top left panel, open symbols) with $\varepsilon(765, 865) < 1.1$ is appropriate to these mean conditions and shows that the single scattering CZCS-type algorithm should be capable of retrieving $[\rho_w(443)]_N$ with the desired accuracy. For the maximum $\tau_a(865)$ ($\sim 0.19$), Figure 7 (top right panel, open symbols) is appropriate and under the same conditions for maximum end of the observed $\tau_a(865)$ range, and for most of the geometries good retrievals are obtained, although in some cases, the error is outside the acceptable range.

For situations with a strong continental influence, e.g., Saharan dust or urban pollution carried over the oceans by the wind, the aerosol is likely to be moderately- to strongly-absorbing. Also, $\tau_a(\lambda)$ will be sufficiently large that aerosol single scattering will no longer be an adequate approximation. Thus, we are forced to consider a full multiple scattering approach.
3.1.1.2 Multiple Scattering Effects

Multiple scattering effects have already been shown [Deschamps, Herman and Tanre, 1983; Gordon, Brown and Evans, 1988; Gordon and Castaño, 1987] to be significant at the level of accuracy required for SeaWiFS and MODIS, i.e., $\Delta[n_{w}(443)]_{N} \approx 0.001 - 0.002$. Although the single scattering approach is seen to work well for sufficiently small optical depth (Figure 7) and nonabsorbing aerosols, typically the case over the open ocean, we desire an algorithm that can cope with even extreme situations. To begin the study of the effects of multiple scattering, we examine the properties of the solutions to the RTE used in providing the pseudo data for Figure 7. Since we are ignoring sun glitter and whitecaps for the moment, we can assess the multiple scattering effects by noting that

$$\rho_{t} - \rho_{r} - t\rho_{w} = \rho_{a} + \rho_{ra} \xrightarrow{\text{Single Scattering}} \rho_{as}.$$ 

Thus, comparison of $\rho_{t} - \rho_{r} - t\rho_{w}$ and $\rho_{as}$ provides a direct assessment of multiple scattering. Figure 8 provides such a comparison for the Tropospheric model with RH = 50% (T50) and the Maritime model with RH = 99% (M99). Note that for the Maritime aerosol for $\rho_{as} \gtrsim 0.01$, the value of $\rho_{a} + \rho_{ra}$ is about 40% greater than $\rho_{as}$, i.e., multiple scattering significantly increases the reflectance due to the aerosol. In contrast, for the Tropospheric model at RH = 50% the aerosol reflectance is only
increased by \( \sim 10\% \). Thus, we see that the influence of multiple scattering depends significantly on the aerosol model. In contrast to the algorithm in Section 3.1.1.1.2, for which multiple scattering was ignored, and for which no knowledge of the aerosol properties was required to effect the atmospheric correction, the model-dependent multiple scattering will make it necessary to utilize aerosol models in the \( \rho_w \) retrieval algorithm.

### 3.1.1.3 The Multiple-Scattering Retrieval Algorithm

From the last section it should be clear that a way must be found to deal with multiple scattering. However, the success of the single-scattering algorithm at low values of \( \tau_a \), and the fact that the only direct link to the aerosol models is through \( \varepsilon(\lambda, \lambda_i) \), or in particular through \( \varepsilon(\lambda_a, \lambda_i) \), it seems reasonable to retain the formalism of the single scattering algorithm, but modify it to include multiple scattering. This is the approach taken here. Writing

\[
\rho_a(\lambda) + \rho_{ra}(\lambda) = K[\lambda, \rho_{as}(\lambda)]\rho_{as}(\lambda),
\]

where the dependence of \( K \) on \( \rho_{as}(\lambda) \) represents the departure of the \( \rho_a(\lambda) + \rho_{ra}(\lambda) \) versus \( \rho_{as}(\lambda) \) relationship from linearity, we see that \( K \) is nearly the same for the two NIR bands, but can be significantly different at 443 nm (Figure 8, left panel). It is irrelevant whether the dependence of \( K \) on \( \lambda \) is explicit \( (K = K[\lambda]) \) or implicit \( (K = K[\rho_{as}(\lambda)]) \) or both, the effect is the same: Eq. (12) becomes

\[
\Delta(t\rho_w(\lambda_i)) = \rho_t(\lambda_i) - \rho_r(\lambda_i) - \frac{K[\lambda_t, \rho_{as}(\lambda_i)]}{K[\lambda_i, \rho_{as}(\lambda_i)]} \varepsilon(\lambda_i, \lambda_l)[\rho_a(\lambda_l) + \rho_{ra}(\lambda_l)],
\]

and the \( \rho_a(\lambda) + \rho_{ra}(\lambda) \) versus \( \rho_{as}(\lambda) \) relationship must be known at each wavelength.

Gordon and Wang [1994a] solved the RTE for a set of \( N \) candidate aerosol models to provide what is essentially a set of lookup tables for \( K[\lambda, \rho_{as}(\lambda)] \). As in the single scattering algorithm, the NIR bands are used to provide the aerosol model through

\[
\varepsilon(\lambda_a, \lambda_l) = \frac{K[\lambda_t, \rho_{as}(\lambda_l)]}{K[\lambda_s, \rho_{as}(\lambda_a)]} \left[ \frac{\rho_a(\lambda_s) + \rho_{ra}(\lambda_s)}{\rho_a(\lambda_l) + \rho_{ra}(\lambda_l)} \right];
\]

however, since the aerosol model is not known at this point, the \( K \) ratio is unknown. Figure 8 suggests that this \( K \) ratio for \( \lambda_l \) and \( \lambda_s \) should not deviate significantly from unity, so Gordon and
Wang [1994a] proposed computing $\varepsilon(\lambda_s, \lambda_l)$ though

$$\varepsilon(\lambda_s, \lambda_l) = \frac{1}{N} \sum_{j=1}^{N} \varepsilon_j(\lambda_s, \lambda_l),$$

where $\varepsilon_j(\lambda_s, \lambda_l)$ is the value of $\varepsilon(\lambda_s, \lambda_l)$ derived from $\rho_a(\lambda_l) + \rho_{ra}(\lambda_l)$ and $\rho_a(\lambda_s) + \rho_{ra}(\lambda_s)$ by assuming that the $K$ ratio for the $j^{th}$ aerosol model is correct. This procedure works reasonably well because the values of $\varepsilon_j$ derived using the individual models are all close to the correct value. The procedure has been further modified by recomputing a new average formed by dropping the two models with the largest values of $\varepsilon(\lambda_s, \lambda_l) - \varepsilon_j(\lambda_s, \lambda_l)$ and the two models with the most negative values. This procedure is carried out several times until the final value is computed using four models: two with $\varepsilon - \varepsilon_j < 0$ and two models with $\varepsilon - \varepsilon_j > 0$.

Having derived a value for $\varepsilon(\lambda_s, \lambda_l)$, the next task is to estimate $\varepsilon(\lambda_i, \lambda_l)$. In general, the derived value of $\varepsilon(\lambda_s, \lambda_l)$ will be bracketed by two of the $N$ candidate aerosol models. We then assume that $\varepsilon(\lambda_i, \lambda_l)$ falls between the same two aerosol models proportionately in the same manner as $\varepsilon(\lambda_s, \lambda_l)$. Finally, we also assume that $K[\lambda_i, \rho_{as}(\lambda_i)]$ falls between the two values for these models in the same proportion as $\varepsilon(\lambda_s, \lambda_l)$. These assumptions are required to proceed, and as we shall see, they are not always valid. However, to the extent that the actual aerosols are similar in their optical properties to the candidate models, the assumptions appear to be reasonably valid.

Initially, twelve candidate aerosol models were used: the Maritime, Coastal, and Tropospheric models with RH = 50, 70, 90, and 99%. Tables of the $\rho_a(\lambda) + \rho_{ra}(\lambda)$ versus $\rho_{as}(\lambda)$ relationship were constructed by solving the RTE for each model for $\theta_0 = 0$ to $80^\circ$ in increments of $2.5^\circ$, and at 33 values of $\theta_v$. The azimuthal dependence of the reflectance was determined through Fourier analysis. Computations were carried out for eight values of $\tau_a(\lambda_i)$ from 0.05 to 0.8. The total number of separate solutions to the RTE used in the preparation of the tables exceeded 33,000 (including the four Urban models used later). To reduce storage, for a given set $(\theta_0, \theta_v)$ the simulations were fit to

$$\log[\rho_t(\lambda) - \rho_r(\lambda) - t \rho_w(\lambda)] = \log[a(\lambda)] + b(\lambda) \log[\rho_{as}(\lambda)] + c(\lambda) \log^2[\rho_{as}(\lambda)]$$

by least-squares. In the case of the azimuth angle $\phi_v$, we expanded $a(\lambda)$, $b(\lambda)$ and $c(\lambda)$ in a Fourier series in $\phi_v$ and stored only the Fourier coefficients. As the reflectances are even functions of the
relative azimuth angle $\phi_v$, $a(\lambda)$, $b(\lambda)$, and $c(\lambda)$ will be even functions of $\phi_v$. Thus, we can write

$$a(\theta_v, \theta_0, \phi_v, \lambda) = a^{(0)}(\theta_v, \theta_0, \lambda) + 2 \sum_{m=1}^{M} a^{(m)}(\theta_v, \theta_0, \lambda) \cos m\phi_v,$$

with

$$a^{(m)}(\theta_v, \theta_0, \lambda) = \frac{1}{\pi} \int_{0}^{\pi} a(\theta_v, \theta_0, \lambda, \phi_v) \cos m\phi_v \, d\phi_v,$$

etc. Using Fourier analysis with $M = 14$ produced about the same accuracy in the results as interpolating with an increment in $\phi_v$ of $5^\circ$ or $10^\circ$.$^2$

### 3.1.1.4 Simulated Test of the Multiple-Scattering Algorithm

We have tested this multiple-scattering algorithm by applying it to pseudo data created using the Shettle and Fenn [1979] Tropospheric, Coastal, Maritime, and Urban models at RH = 80%, denoted by T80, C80, M80, and U80, respectively. Note that these are not part of the candidate aerosol set, although the size and refractive index distributions of T80, C80, and M80 are similar to members of the set. In contrast to the others, and unlike any members of the candidate set, U80 has strong aerosol absorption.

Comparison between the single-scattering and multiple-scattering algorithms for pseudo data created with these models at the seven sun-viewing geometries described earlier is provided in Figure 9 for $\tau_a(865) = 0.2$. Clearly, including multiple scattering in the algorithm significantly improves the retrieval of $[\rho_w(443)]_N$ for the T80, C80, and M80 cases, for which $\tau_a(443) \approx 0.50$, 0.32, and 0.24, respectively (Figures 5, left panel, and 6). In contrast, the U80 retrievals, although somewhat improved over single scattering, are still very poor. Thus, even though the size distribution of the U80 model is similar to the candidates (both in modal diameter and standard deviation), the fact that the particles are strongly absorbing causes as large an error in the retrieval of $[\rho_w(443)]_N$ as neglecting multiple scattering completely. Clearly, particle absorption must have a profound impact on multiple scattering.

$^2$ Note: when $\theta_v$ is near $\theta_0$, $\rho_a + \rho_{aa}$ and $\rho_{as}$ can become very large because of the specular reflection of forward-scattered light from the sea surface. As it would take a very large number of Fourier components to reproduce this “spike” in the reflectances, it is removed before the Fourier analysis. This is of no consequence in the processing, because this is the region of the maximum sun glitter; however, it does considerably reduce the value of $M$ required for a given accuracy.
As in Figure 7 (bottom panels), Figure 9 (bottom panels) provides the relationship between $[\rho_w(550)]_N$ and $[\rho_w(443)]_N$ for the single-scattering and the multiple-scattering (SeaWiFS) algorithms. For the multiple-scattering algorithm, $\Delta[\rho_w(550)]_N \approx (1/4)\Delta[\rho_w(443)]_N$, and with the exception of very low pigment concentrations, the error in atmospheric correction at 443 nm will contribute more significantly to the error in $R$ [Eq. (4)] than that at 550 nm. Fortuitously, the errors at 443 and 550 nm typically have the same sign and, therefore, tend to cancel in $R$. 
Table 2: Mean value of $C$ obtained for seven viewing geometries and three aerosol models (M80, C80, and T80). The number in parenthesis is the standard deviation divided by the mean (in %).

<table>
<thead>
<tr>
<th>$\tau_a(865)$</th>
<th>$C_{\text{True}} = 0.10$ mg/m$^3$</th>
<th>$C_{\text{True}} = 0.47$ mg/m$^3$</th>
<th>$C_{\text{True}} = 0.91$ mg/m$^3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>0.101</td>
<td>0.466</td>
<td>0.912</td>
</tr>
<tr>
<td></td>
<td>(1.6)</td>
<td>(3.4)</td>
<td>(9.1)</td>
</tr>
<tr>
<td>0.2</td>
<td>0.100</td>
<td>0.470</td>
<td>0.940</td>
</tr>
<tr>
<td></td>
<td>(3.1)</td>
<td>(4.7)</td>
<td>(12.8)</td>
</tr>
<tr>
<td>0.3</td>
<td>0.098</td>
<td>0.493</td>
<td>0.936</td>
</tr>
<tr>
<td></td>
<td>(5.5)</td>
<td>(15.3)</td>
<td>(25.3)</td>
</tr>
</tbody>
</table>

The error in the pigment concentration induced by $\Delta[\rho_w(550)]_N$ and $\Delta[\rho_w(443)]_N$ in the multiple-scattering algorithm is provided in Table 2. To prepare this table, the errors were added to values of $[\rho_w(550)]_N$ and $[\rho_w(443)]_N$ that are characteristic of three pigment concentrations (0.10, 0.47, and 0.91 mg/m$^3$) in order to produce retrieved reflectances that include the atmospheric correction error. These were then inserted into Eq. (4) and the resulting pigment concentration was derived for each sun-viewing geometry for the M80, C80, and T80 aerosol models. For each true pigment concentration, the twenty-one retrieved values of $C$ (seven geometries times three aerosol models) were averaged and the standard deviation was computed. The computations were carried out for $\tau_a(865) = 0.1$, 0.2, and 0.3.

As expected, the quality of the retrievals is best for the smallest value of $\tau_a(865)$. Excellent retrievals of $C$ (as indicated by excellent mean values and small relative standard deviations) were obtained for $\tau_a(865) = 0.1$ and 0.2, and for the two lower concentrations for $\tau_a(865) = 0.3$. As mentioned earlier, $\tau_a(865)$ is typically $\lesssim 0.2$ in regions not subjected to urban pollution or desert dust. For $\tau_a(865) = 0.3$ and a true value of $C$ of 0.91 mg/m$^3$, one retrieved value of $C$ was $\approx 9$ mg/m$^3$ ($\theta_0 = 60^\circ$, $\theta_c \approx 45^\circ$, T80, for which $\tau_a(443) \approx 0.75$ and $\tau_a(550) \approx 0.6$). This value was not included in the average or the standard deviation computation. These results suggest that the multiple-scattering algorithm will provide excellent results as long as the candidate aerosol models
are similar in size and composition to the aerosol actually present, they need not be precisely representative of the actual aerosol.

To try to understand the effect of particle absorption on multiple scattering, a set of multiple scattering computations of $\rho_a + \rho_{ra}$ was carried out in which particle absorption alone was varied. Specifically, we used the phase functions for the T50 and M99 aerosol models evaluated at 865 nm (Figure 10). These models have the most weakly (T50) and the most strongly (M99) forward peaked scattering phase function among the candidate models. Simulations of $\rho_a + \rho_{ra}$ as a function of $\tau_a$ (or equivalently $\rho_{as}$) were made for $\theta_0 = 60^\circ$ and $\theta_a \approx 1^\circ$, with $\tau_r = 0.015$ (865 nm) and 0.236 (443 nm), as $\omega_a$ assumed the values of 0.6, 0.8, and 1.0. The results are presented in Figure 11. Two facts concerning the $\rho_a + \rho_{ra}$ versus $\rho_{as}$ relationship emerge from these simulations. First, for $\omega_a = 1$, the relationship is nearly linear and, for the sharply peaked M99 phase function, the Rayleigh-aerosol interaction ($\sim$ the difference between the dashed and solid curves caused by changing $\tau_r$) is small, while for the smoother T50 phase function the Rayleigh-aerosol interaction is significantly larger. This is to be expected, since the mid-angle scattering by T50 is much larger than M99 (Figure 10). Second, as $\omega_a$ decreases, there are greater departures from linearity and an
increase in the significance of the Rayleigh-aerosol interaction for both T50 and M99. The general shape of the curves is explained by the fact that \( \rho_a + \rho_{ra} \) must approach an asymptotic value as \( \tau_a \rightarrow \infty \). Also, increasing \( \tau_r \) causes more diffuse light to enter the aerosol layer and traverse longer paths through it, with the concomitant greater chance of absorption. This explains the strong influence of \( \omega_a \) on \( \rho_{ra} \).

![Diagram showing Phase Function](image)

Figure 11. \( \rho_a + \rho_{ra} \) as a function of \( \rho_{as} \) and \( \omega_a \) for 443 nm (dashed) and 865 nm (solid) Curves from bottom to top correspond to \( \omega_a = 0.6, 0.8, \) and 1.0. Left panel: T80. Right panel: M99.

The impact of the absorption in Figure 11 is serious. Consider a hypothetical situation in which the M99 phase function is appropriate and \( \epsilon(\lambda_1, \lambda_l) = 1 \), so \( \rho_{as}(\lambda_1) = \rho_{as}(\lambda_l) \). Also, assume that \( \epsilon(\lambda_1, \lambda_l) \) is correctly determined by the algorithm and that \( \rho_a + \rho_{ra} \approx 0.02 \) at 865 nm. Then, if \( \omega_a = 1 \) were used for estimating \( \rho_a + \rho_{ra} \) at 443 nm, but the true value of \( \omega_a \) was actually 0.8, Figure 11(right panel) shows that the error in \( \rho_a + \rho_{ra} \) at 443 nm would be \( \sim -0.004 \). In contrast, if the \( \omega_a = 1 \) assumption was correct the error would be \( \sim +0.001 \). Clearly, the effect of absorption is to produce large negative errors in \( t\rho_a \), i.e., to overestimate the effect of the atmosphere. Figure 4 (left panel) suggests that when \( \epsilon(\lambda_1, \lambda_l) \) is estimated from \( \epsilon(\lambda_s, \lambda_l) \) using weakly- or nonabsorbing aerosol models, it will be overestimated, i.e., \( \epsilon(\lambda_1, \lambda_l) \) will be too large, if the aerosol strongly absorbs. This effect will cause a further overestimation of the atmospheric effect.

As the twelve candidate models in Section 3.1.1.3 are combinations of two components with physical properties dependent on RH, they represent a fixed set of values of \( \omega_a \) at each wavelength,
i.e., there are only twelve different values of $\omega_a$. At 865 nm, these range from 0.99857 (M99) to 0.92951 (T50). Furthermore, each model possesses a unique value of $\varepsilon(\lambda_s, \lambda_l)$ and a more or less unique value of $\varepsilon(\lambda_l, \lambda_l)$ for a given sun-viewing geometry (Figure 4, left panel). Thus, the choice of the twelve candidates forces a definite relationship between $\omega_a$ and $\varepsilon(\lambda_l, \lambda_l)$. In the case of the twelve models chosen here, there is a steady decrease in $\omega_a$ with increasing $\varepsilon(\lambda_l, \lambda_l)$. If this relationship is more or less correct, an excellent correction is effected (Figure 9 (top right panel), T80); however, with its low value of $\omega_a$ (0.74806 for U80 at 865 nm) the Urban model falls considerably outside this relationship and the resulting atmospheric correction is very poor (U80 in Figure 9, top right). This is further shown in Figure 12 in which the multiple-scattering

![Figure 12](image-url)

Figure 12. $\Delta[\rho_v(443)]_N$ as a function of $\varepsilon^{(e)}(765, 865)$ for the Haze C models with $\tau_v(865) = 0.2$ and all of the viewing geometries examined in the study, using the multiple-scattering algorithm.

algorithm is applied to the Haze C models. In this Figure we have limited the models to those that fall within the range of variation of the values of $\varepsilon(\lambda_s, \lambda_l)$ of the candidate models, and also models for which $\tau_v(443) \lesssim 0.8$, the upper limit of $\tau_v$ used in the preparation of the $\rho_a + \rho_{ra}$ versus $\rho_{as}$ look up tables. Haze C models with a real index of refraction ($\omega_a = 1$) and $\nu \geq 3$ do not follow the $\omega_a - \varepsilon(\lambda_s, \lambda_l)$ relationship implied by the candidate models, and the values of $\Delta[\rho_v(443)]_N$ are positive. In contrast, the dust and mineral models both display $\omega_a$-values less than T50, and for
these the $\Delta[\rho_w(443)]_N$ are large and negative. Thus, it should be clear that it is imperative to use candidate aerosol models that possess an approximately correct relationship between $\omega_a$ and $\varepsilon(\lambda_s, \lambda_l)$, or physically, an approximately correct relationship between particle size and absorption. Such a relationship must be based on climatology, e.g., when the aerosol optical thickness over the North Atlantic Saharan dust zone is high, one should use candidate models consisting of a linear combination of a Maritime model and Saharan dust model, either uniformly mixed in the marine boundary layer or having a two-layer structure. Given such climatology-based models, preparation of the appropriate look up tables for incorporation into the algorithm is a simple process.

As an example, we modified the algorithm to utilize only four candidate models, the Shettle and Fenn [1979] Urban models at RH = 50%, 70%, 90%, and 99%, and tested it using pseudo data created with the U80 model. In this manner, the $\omega_a$ and $\varepsilon(\lambda_s, \lambda_l)$ relationship was approximately correct. The results are provided in Figure 13, which shows the error in $[\rho_w(443)]_N$ as a function of the aerosol optical thickness of U80 at 865 nm. Recall, from Figure 5 (left panel), that $\tau_a(443) \approx 1.75\tau_a(865)$. Comparison with Figure 12, for which $\tau_a(865) = 0.2$, shows that the maximum error (which occurs at the scan edge with $\theta_0 = 60^\circ$), when the Urban models are used as candidates, is

Figure 13. $\Delta[\rho_w(443)]_N$ as a function of $\tau_a(865)$ for the U80 model, when the candidate aerosol models in the multiple-scattering algorithm are restricted to U50, U70, U90, and U99.
only twice the minimum error when the original twelve candidate aerosol models were used. This underscores the necessity of having realistic climatologically-based aerosol models in situations in which the aerosol concentration is sufficiently large to require consideration of multiple scattering.

3.1.1.5 The diffuse transmittance

The diffuse transmittance was mentioned in Section 3.1.1. It is defined as the water-leaving radiance in a particular viewing direction \((\theta_v, \phi_v)\) “transmitted” to the top of the atmosphere, i.e.,

\[
t(\theta_v, \phi_v) = \frac{\rho_w(\theta_v, \phi_v)_{\text{Top}}}{\rho_w(\theta_v, \phi_v)}.
\]  

(15)

Thus, if the atmosphere were only illuminated from below with radiance \(\rho_w(\theta, \phi)\), the radiance measured at the top of the atmosphere in the direction \((\theta_v, \phi_v)\) would be \(t(\theta_v, \phi_v)\rho_w(\theta_v, \phi_v)\). The diffuse transmittance accounts for the direct loss from \(\rho_w(\theta_v, \phi_v)\) due to absorption and scattering within the atmosphere, as well as for the gain in radiance in the direction \((\theta_v, \phi_v)\) due to scattering of \(\rho_w(\theta, \phi)\), i.e., from all other upward directions, into \((\theta_v, \phi_v)\). It is interesting to note that, unlike the direct transmittance \(T\), there is no requirement that the diffuse transmittance be less than unity. For example, if \(\rho_w(\theta, \phi) = 0\) for a particular viewing direction, but not others, then \(\rho_w(\theta_v, \phi_v)_{\text{Top}} > 0\) because of atmospheric scattering from other directions into \((\theta_v, \phi_v)\). Thus, in this admittedly bizarre example, \(t(\theta_v, \phi_v) = \infty!\) We present it only to underscore the fact that the diffuse transmittance is not a fundamental property of the atmosphere, but depends on the angular distribution of \(L_w\) as well as the optical properties of the atmosphere. In the case of the CZCS, it was assumed that \(\rho_w(\theta_v, \phi_v)\) is independent of \((\theta_v, \phi_v)\). We also employ a similar assumption in the present algorithm and, for emphasis, we designate the diffuse transmittance so computed by \(t^*\) to avoid confusion with the correct diffuse transmittance.\(^{3}\) Then, extending a single scattering analysis of \(t^*\) to approximately include the effects of multiple scattering (by replacing \((1 - x)\) in single scattering formulas by \(\exp(-x)\)), Gordon et al. [1983] approximated \(t^*\) by

\[
t^*(\theta_v, \phi_v, \lambda) = \exp\left[-\left(\frac{\tau_r(\lambda)}{2} + \tau_{Oz}(\lambda)\right)\left(\frac{1}{\mu_v}\right)\right]t_a(\theta_v, \lambda),
\]  

(16)

\(^3\) Actually in the MODIS algorithm it is assumed that the upwelling radiance distribution just beneath the sea surface, \(L_u(\theta_v', \phi_v')\), is uniform. \(\rho_w(\theta_v, \phi_v)\) is related to \(L_u\) through \(\rho_w(\theta_v, \phi_v) = \pi L_u(\theta_v', \phi_v') T_f(\theta_v', \phi_v')/(m^2 F_0 \cos \theta_0)\), where \(T_f(\theta_v', \phi_v')\) is the Fresnel transmittance of the sea surface for light incident from \((\theta_v', \phi_v')\), \(m\) is the refractive index of water, and \((\theta_v', \phi_v')\) relates to \((\theta_v, \phi_v)\) through Snell’s law.
where
\[ t_a(\theta_v, \lambda) = \exp\left[ -\frac{1 - \omega_a(\lambda) F_a(\mu_v, \lambda) \tau_a(\lambda)}{\mu_v} \right] \],
(17)
and \( \mu_v = \cos \theta_v \). \( F_a(\mu_v, \lambda) \) is related to the scattering phase function of the aerosol and is given by
\[ F_a(\mu_v, \lambda) = \frac{1}{4\pi} \int_0^1 P_a(\alpha, \lambda) d\mu d\phi, \]
where \( P_a(\alpha, \lambda) \) is the aerosol phase function at \( \lambda \) (normalized to \( 4\pi \)) for a scattering angle \( \alpha \), and
\[ \cos \alpha = \mu_\mu + \sqrt{(1 - \mu^2)(1 - \mu_v^2)} \cos \phi. \]
If \( \theta_v \) is \( \lesssim 60^\circ \) the factor \( [1 - \omega_a(\lambda) F_a(\mu_v, \lambda)] \) is usually \( \ll 1 \), so \( t_a \) depends only weakly on the aerosol optical thickness and was taken to be unity for CZCS.

Later, Yang and Gordon [1997] carried out a through study of the diffuse transmittance, including its dependence on the \( \rho_w(\theta_v, \phi_v) \). For the case where the upwelling radiance just beneath a flat sea surface is uniform, they derived
\[ t^*(\hat{\xi}_0) = \frac{E_d(\hat{\xi}_0)}{F_0 \cos \theta_0 T_f(\hat{\xi}_0)}, \]
where the solar beam is propagating in the direction \( \hat{\xi}_0 \) and \( E_d \) is the downwelling irradiance just beneath the sea surface. This leads to a very simple monte carlo procedure for computing \( t^* \), i.e., to find \( t^*(\theta_v) \), simply inject photons from the sun into the atmosphere with a solar zenith angle \( \theta_0 = \theta_v \) and record the number that penetrate the water surface (\( E_d/F_0 \cos \theta_0 \) equals number penetrating divided by the number injected). Thus, to compute \( t^* \) (photons propagating from the ocean to the top of the atmosphere) we actually solve a reciprocal problem (photons propagating from the sun to the water). Henceforth, \( t^* \) will be used to designate the diffuse transmittance computed in this manner, as opposed to that computed using the approximate single scattering formulas above. Because the correction algorithm provides models of the aerosol, it is possible to incorporate all of the multiple scattering and aerosol effects into \( t^* \) in the form of look up tables.

As retrieval of \( \rho_w \) from \( \rho_t \) requires \( t \), and relative error in \( t \) will yield an equivalent relative error in \( \rho_w \), it is important to compute this quantity as accurately as possible. Replacing \( t \) by \( t^* \) leads to error that is assessed in a later Section (3.1.1.9.5).
3.1.1.6 Whitecap Removal Algorithm

As mentioned earlier, the term \( t(\lambda_i)\rho_{wc}(\lambda_i) \) in Eq. (6) has been ignored in the development of the algorithm. If we indicate the reflectance measured at the top of the atmosphere as \( \rho_t^{(m)} \), this reflectance consists of two parts; that which would be measured in the absence of whitecaps, and the reflectance added by the whitecaps \( t^*\rho_{wc} \), i.e.,

\[
\rho_t^{(m)} = \rho_t + t^*\rho_{wc}. \tag{19}
\]

Since the \( [\rho_w]_N \)-retrieval algorithm must be operated with \( \rho_t \) rather than \( \rho_t^{(m)} \), \( t^*\rho_{wc} \) must be removed from the imagery before the algorithm can be applied.

As in the case of the normalized water-leaving radiance, we define the normalized whitecap reflectance (or the albedo) \( [\rho_{wc}]_N \) to be the area-weighted reflectance (over several pixels) of oceanic whitecaps at the sea surface. Then the whitecap component of the radiance leaving the surface is

\[
L_{wc}(\lambda) = [\rho_{wc}(\lambda)]_N \frac{F_0 \cos \theta_0}{\pi} t^*(\theta_0, \lambda),
\]

where the whitecaps are assumed to be lambertian. Converting to reflectance we have

\[
\rho_{wc}(\lambda) = [\rho_{wc}(\lambda)]_N t^*(\theta_0, \lambda).
\]

At the top of the atmosphere, the whitecaps contribute

\[
t^*\rho_{wc}(\lambda) = [\rho_{wc}(\lambda)]_N t^*(\theta_0, \lambda) t^*(\theta_v, \lambda).
\]

The problem faced in removing \( t^*\rho_{wc}(\lambda) \) from \( \rho_t(\lambda) \) in Eq. (6) is the estimation of \( [\rho_{wc}(\lambda)]_N \).

Based on previous research on the relationship between whitecaps and environmental parameters, Koepke [1984] estimated that the reflectance \( R \) of whitecaps can be expressed as

\[
R = 6.49 \times 10^{-7} W^{3.52}, \tag{20}
\]

\footnote{The use of \( t^* \) (as defined in the last section) is not rigorously correct here, as \( t^* \), when used with \( \rho_w \) requires that the upwelling radiance just beneath the sea surface be uniform, while \( [\rho_{wc}]_N \) is assumed to be lambertian above the surface. However, the error induced by using the incorrect transmittance is negligible compared to the large uncertainty in \( [\rho_{wc}]_N \).}
where $W$ is the wind speed in m/s measured 10 m above the sea surface. Note that this included the background reflectance as well. Figure 14 provides Koepke’s reflectance as a function of $W$, along with data derived from Monahan [1971]. It shows that Eq. (20) predicts $R$ with a standard deviation approximately equal to the reflectance itself.

To estimate the error in the retrieved $\rho_w$ due to whitecaps, Gordon and Wang [1994b] used Koepke’s reflectance as an approximation to $[\rho_{wc}(\lambda)]_N$, however, the effect of the any error in the estimation of $[\rho_{wc}]_N$ on the retrieved water-leaving reflectance is strongly dependent on its spectral variation. In Gordon and Wang [1994b] it was assumed, based on measurements carried out by Whitlock, Bartlett and Gurganus [1982], that $[\rho_{wc}(\lambda)]_N$ was independent of $\lambda$; however, Schwindling [1995] and Frouin, Schwindling and Deschamps [1996] have reported measurements on breaking waves in the surf zone suggesting that whitecaps may reflect considerably less in the NIR than in the visible, presumably because a significant component of the whitecap reflectivity is due to scattering from submerged bubbles. To understand the effect of spectral variation in $[\rho_{wc}]_N$ on the accuracy of atmospheric correction, the multiple scattering algorithm has been operated in the presence of whitecaps displaying both nonspectral reflectance and the spectral reflectance suggested by Frouin, Schwindling and Deschamps [1996]. Figure 15 compares the error in $[\rho_w(443)]_N$ as a function of $\theta_0$.
for viewing at the edge of the MODIS scan with the M80 aerosol model ($\tau_a(865) = 0.2$) for these two cases when the error in the estimate of $[\rho_{wc}]_N$ (Figure 14) at 443 nm is $\pm 0.002$. This error in $[\rho_{wc}(443)]_N$ corresponds to a wind speed of $\sim 8 - 9$ m/s. Figure 15 shows that for wavelength-independent whitecap reflectivity, the resulting error in $[\rho_w(\lambda)]_N$ can be significantly less ($\sim 1/4$) than the error in the estimate of $[\rho_{wc}(443)]_N$. In contrast, if whitecaps reflect in a manner consistent with the Frouin, Schwindling and Deschamps [1996] observations, the error in $[\rho_w(443)]_N$ can be expected to be of the same order-of-magnitude as the error in $[\rho_{wc}(443)]_N$. Similar simulations using the T80 aerosol model, for which $\varepsilon(\lambda, 865)$ displays strong variation with $\lambda$, show similar effects for the case of whitecaps with the Frouin, Schwindling and Deschamps [1996] reflectance; however, the error for the Whitlock, Bartlett and Gurganus [1982] reflectance model can also be the same order of magnitude as $\Delta[\rho_{wc}(443)]_N$ [Gordon and Wang, 1994b]. Figure 15 shows that an overestimation of $[\rho_{wc}(443)]_N$ leads to a negative error in $[\rho_w(443)]_N$. The same is true at 550 nm.

![Figure 15. $\Delta[\rho_w(443)]_N$ as a function of the error in the whitecap reflectance at 443 nm and $\theta_0$ at the edge of the scan for the M80 aerosol model with $\tau_a(865) = 0.2$. Left panel: whitecap reflectance spectrum is that proposed by Whitlock, Bartlett and Gurganus [1982]. Right panel: whitecap reflectance spectrum is that proposed by Frouin, Schwindling and Deschamps [1996].](image)

When the errors in $[\rho_w(\lambda)]_N$ are negative, algorithms such as Eq. (4), that use radiance ratios, can lead to very large errors in the derived products. Because of this, it is better to underestimate the $[\rho_{wc}(443)]_N$ in the whitecap correction algorithm than to overestimate it.

As whitecaps have the potential of producing errors of a magnitude similar to the magnitude
of the acceptable error in $[\rho_w(\lambda)]_N$, it was important to obtain radiometric data of actual oceanic whitecaps, and validate its dependence on wind speed. In particular, it is critical to understand the spectral dependence of $[\rho_w]$ in the NIR. Our approach to this was to construct a ship-based radiometer for observing whitecaps while a ship is on station or underway [Moore, Voss and Gordon, 1998]. The radiometer, suspended from a boom off the bow of the ship, continuously views a spot about 12 cm in diameter on the sea surface, continuously measuring a radiance $L_s$. A video image, from a TV camera mounted along side of the radiometer to visually observe the water surface, is used to reject sun glitter. A second radiometer on the deck of the ship records the incident irradiance $E_d$. The radiance of the surface measured by the radiometer is recorded as a function of time ($\sim 7$ samples/sec). This radiance consists of background radiance ($L_b$) from whitecap-free areas (the predominant situation) and a much higher radiance ($L_{wc} + L_b$) whenever a portion of a whitecap is in the field of view of the radiometer. After determining the radiance of the whitecap-free areas ($L_b$, essentially the “baseline” of the radiance), and subtracting it from the entire record, we are left with the time-average radiance due to the whitecaps,

$$\langle L_{wc} \rangle = \langle L_s \rangle - \langle L_b \rangle.$$

The associated reflectance (the remote-sensing augmented reflectance, RSAR) is

$$RSAR = \frac{\pi \langle L_{wc} \rangle}{E_d}.$$

Since, under clear skys (see footnote 4),

$$E_d \approx F_0 \cos \theta t(t_0),$$

we see that

$$[\rho_{wc}(\lambda)]_N \approx RSAR(\lambda).$$

The radiometer is accompanied by a meteorological package to provide the speed of the wind relative to the ship (and other, possibly relevant, parameters) and a GPS unit to provide the absolute speed of the ship. Combining these will yield $W$. The whitecap radiometer records in 10 nm bands centered at 6 wavelengths: 410, 510, 550, 670, 750, and 860 nm, and the downward surface irradiance is measured in 5 bands, also 10 nm wide, centered at 410, 510, 550, 670, and 860 nm. Thus, we are able to study the validity of Eq. (20) throughout the relevant spectral region.
An example of two whitecaps passing under the radiometer (deployed from the NOAA ship RV Malcolm Baldrige, April 1996) is shown in Figure 16. The 96 consecutive samples shown are acquired over a period of \( \sim 15 \) seconds. In this example a large whitecap suddenly breaks in view of the radiometer with thick white foam (sample point 11) reaching a peak reflectance of \( \sim 55\% \). Six traces are plotted representing the six radiometer channels. The lower trace corresponds to the 860 nm reflectance. The thick foam is temporarily replaced by a region of submerged bubbles and less thick foam (\( \sim \) sample points 13, 14, 15) and some thick foam comes into view again at sample point 17. At sample point 20 and 21 a thin layer of foam passes followed by the decaying thicker foam to about sample point 35. Sample points from about 35 to 55 show the reflectance of thinning residual foam. From 60 to about 75 the reflectance of the foam free water surface is shown and is suddenly followed by another whitecap of smaller magnitude (sample point 76) and continues to decay out to about sample point 96. The data clearly suggest a significant fall in the NIR reflectance of whitecaps in agreement with the measurements of Frouin, Schwindling and Deschamps [1996] in the surf zone.

From 1 to 13 November 1996, the whitecap radiometer was operated on a cruise from Manzanillo, Mexico to Honolulu, Hawaii. This cruise provided whitecap data under conditions of steady winds (the trades) of essentially unlimited duration and fetch. Unfortunately, analysis of the data
was not as straightforward as expected. Under clear skies it proved very difficult to separate whitecaps from sun glint events. Thus, we performed the analysis only under overcast conditions. Furthermore, the determination of the “baseline” reflectance is critical to the analysis and proved to be difficult as well.

The analysis for estimating RSAR is described in detail in Moore, Voss and Gordon [1997]. The dependence of RSAR at 410 nm on wind speed is provided in Figure 17. The black triangles (joined by a vertical line) are the results of two different methods of data analysis (establishing the baseline). The larger (lower) black triangles are believed to be the better analysis of the data. For these,

\[ RSAR \sim 3 \times 10^{-6}W^{-2.55}. \]

The data also fit the Koepke formula (corrected to RSAR) reasonably well with the multiplier

![Figure 17. Remote-sensing augmented reflectance of whitecaps at 410 nm. The small and large triangles are from Moore, Voss and Gordon [1997] and correspond to two methods of analyzing the whitecap measurements. The open symbols are the Monahan [1971] fractional coverage multiplied by 0.155, the Koepke [1984] effective whitecap reflectance of 0.22 minus 0.065 to convert from reflectance to augmented reflectance. The dashed lines use the Monahan and O’Muircheartaigh [1986] model for a neutrally stable (\( \Delta T = 0 \)) and an unstable (\( \Delta T = 2^\circ \)) atmosphere to provide fractional coverage for use in computing the augmented reflectance: RSAR = \( 3 \times 10^{-6}W^{-2.55} \exp(0.861 \times \Delta T) \).](image)
reduced by $\sim 1/3$, i.e.,

$$RSAR \sim 1.6 \times 10^{-7} W^{3.52}.$$  

Finally, although there was no discernable spectral variation of $RSAR$ in the visible, the $RSAR$ was significantly lower at 860 nm than at 410 nm. (Figure 18). Although the data are very noisy, they suggest that

$$RSAR(860) \sim 0.85 \times RSAS(410),$$

for $RSAR(410) \lesssim 0.06$. This reduction of $RSAR$ in the NIR was less than observed in the surface zone [Frouin, Schwindling and Deschamps, 1996] and in ship wakes [Moore, Voss and Gordon, 1998].

Combining all of the observations, the algorithm for correcting the data for the effects of whitecaps is

$$[\rho_{ec}(\lambda)]_N = S(\lambda) \times 1.6 \times 10^{-7} W^{3.52},$$

where $S(\lambda)$ is a spectral reflectance factor for whitecaps taken to be unity in the visible, 0.925 at 750 nm and 0.85 at 860 nm. While this correction is conservative (underestimate) in the region of our measurements, it may provide a better estimate for $W > 12$ m/s.

![Figure 18. Relationship between RSAR at 865 nm and 410 nm (from Moore, Voss and Gordon [1997]).](image-url)
3.1.1.7 Sun Glitter Mask and Correction

The contribution to the MODIS-measured radiance (or reflectance) at the TOA from sun glitter — the specular reflection of direct sunlight from the sea surface and subsequent propagation to the sensor — can be sufficiently large that the sensor will actually saturate. As such, severely perturbed pixels cannot be processed and need to be masked. For all other pixels, an estimate of the contribution of sun glitter is required for its removal. This estimate is based on the formulation of Cox and Munk [1954]. In their development the sea surface is modeled as a collection of facets with individual slope components $z_x$ and $z_y$. It is a matter of simple geometry to determine the direction that the normal to a facet must have in order to reflect direct sunlight toward the sensor.

Consider a coordinate system (Figure 19) with the $+y$ axis pointing toward the sun (the projection of the sun’s rays on the sea surface is along the $-y$ axis). The solar zenith angle is $\theta_0$. Let the angles $\theta$ and $\phi$ specify the reflected ray, where $\phi$ is measured from the $-y$ axis toward the $-x$ axis (i.e., $\phi$ as shown in Figure 19 is positive). Then, the orientation $(\beta, \alpha)$ of the facet normal $\mathbf{n}_f$ (Figure 19) required for the facet to reflect sunlight in the direction of $(\theta, \phi)$ is found from the following equations:

$$\cos(2\omega) = \cos \theta \cos \theta_0 - \sin \theta \sin \theta_0 \cos \phi$$
$$\cos \beta = (\cos \theta + \cos \theta_0)/2 \cos \omega$$
$$\cos \alpha = (\cos \theta_0 \cos \beta - \cos \omega)/2 \sin \theta_0 \sin \beta$$
$$z_x = \sin \alpha \tan \beta$$
$$z_y = \cos \alpha \tan \beta.$$

Note that for a flat (smooth) surface, $\phi = 0$. Let $\psi$ be the the angle between the projection of the sun’s rays on the sea surface and the direction of the wind vector $\mathbf{W}$, i.e., if $\psi = 0$ the wind vector points in the direction of $-y$ in Figure 19. $\psi$ is measured positive in a clockwise direction (looking toward the surface), i.e., if $0 < \psi < 90^\circ$, the wind vector is in the quadrant formed by the $-x$ and $-y$ axes. Then, the defining the glitter reflectance $\rho_g$ to be the radiance reflected from the sea
surface, $L_g$, times $\pi/F_0 \cos \theta_0$, where $F_0$ is the extraterrestrial solar irradiance, $\rho_g$ is given by

$$
\rho_g(\theta, \phi; \theta_0, \phi_0) = \frac{\pi r_+ (\omega)}{4 \cos \theta_0 \cos \theta \cos^4 \beta} \rho(z_x', z_y')
$$

where $p(z_x', z_y')$ is the probability density of surface slopes given by

$$
p(z_x', z_y') = (2\pi \sigma_u \sigma_c)^{-1} \exp\left[-(\xi^2 + \eta^2)/2\right] \left[ 1 + \sum_{i=1}^{\infty} \sum_{j=1}^{\infty} c_{ij} H_i(\xi) H_j(\eta) \right],
$$

with

$$
\begin{align*}
\xi &= z_x'/\sigma_c = \sin \alpha' \tan \beta/\sigma_c \\
\eta &= z_y'/\sigma_u = \cos \alpha' \tan \beta/\sigma_u \\
\alpha' &= \alpha - \psi.
\end{align*}
$$

$H_i$ is the Hermite polynomial of order $i$. $r_+ (\omega)$ is the Fresnel reflectance for unpolarized light.
incident at an angle $\omega$. It can be found from

$$r_{\pm}(\omega) = \frac{1}{2} \left[ \frac{\tan^2(\omega - \omega')}{\tan^2(\omega + \omega')} \pm \frac{\sin^2(\omega - \omega')}{\sin^2(\omega + \omega')} \right],$$

where

$$\sin \omega' = \frac{1}{m_w} \sin \omega$$

and $m_w$ is the refractive index of water.

The constants $\sigma_u$, $\sigma_v$, and $c_{ij}$ were determined by Cox and Munk by fitting the radiance from glitter patterns photographed from aircraft of the coast of California to these equations. They are:

$$\sigma_u^2 = 0.003 + 1.92 \times 10^{-3} W \pm 0.002$$

$$\sigma_v^2 = 0.000 + 3.16 \times 10^{-3} W \pm 0.004$$

$$c_{21} = 0.01 - 8.6 \times 10^{-3} W \pm 0.03$$

$$c_{03} = 0.04 - 33 \times 10^{-3} W \pm .012$$

$$c_{40} = 0.40 \pm 0.23$$

$$c_{22} = 0.12 \pm 0.06$$

$$c_{04} = 0.23 \pm 0.41.$$

There is considerable debate as to the validity of the values assigned to these parameters. Shaw and Churnside [1997] have directly measured $\sigma_u$ using a scanning-laser glint meter. Their results showed a strong dependence of $\sigma_u$ on the atmospheric stability. The atmospheric stability is characterized by the Richardson number $R_i$ given by

$$R_i = g \frac{(T_a - T_w)}{T_w W^2},$$

where $T_a$ and $T_w$ are, respectively, the air and water temperatures ($^\circ C$), and $g$ is the gravitational constant (9.8 m/s$^2$). The atmosphere is stable when $R_i > 0$ and unstable when $R_i < 0$. They combined their measurements with those of Hwang and Shemdin [1988] and developed the relationship between $\sigma_u$ and $R_i$ provided in Figure 20. The lines on the figure correspond to

$$\frac{\sigma_u^2}{\sigma_{cm}^2} = 1.42 - 2.8 R_i \quad \text{for} \quad -0.23 < R_i < 0.27$$

$$\frac{\sigma_u^2}{\sigma_{cm}^2} = 0.65 \quad \text{for} \quad R_i > 0.27.$$
Cox and Munk [1954] collected most of their data for positive stability, thus for unstable atmospheres, $\sigma_u$ is considerably larger than that suggested by their equations. It is expected that $\sigma_c$ behaves in a manner similar to $\sigma_u$ in respect to its dependence on stability. It is important to note that a larger $\sigma$ implies a more diffuse glitter pattern, i.e., it extends farther from the specular point (the point at which sunlight would be reflected from a flat surface toward the sensor), but with smaller radiance near the specular point.

In contrast to direct measurements of the surface slope statistics, Ebuchi and Kizu [2002] combined directly observed glitter patterns (from a geostationary satellite) with satellite estimates of the wind speed and direction from spaceborne radar scatterometers. They assumed that the apparent radiance of the surface in the visible is proportional to $p(z', z'')$, and on this basis, derived the surface slope parameters. Their resulting $\sigma_c$ agreed well with that measured by Cox and Munk [1954]; however, their $\sigma_u$ showed a considerably weaker dependence on $W$. Considering that most of their measurements were in the tropics, where the atmosphere is expected to be unstable, their conclusions are opposite to Shaw and Churnside [1997] and Hwang and Shemdin [1988]. Ebuchi
and Kizu [2002] attribute this to the likelihood that the direct measurements were made under conditions in which the waves were growing with the wind, whereas in their measurements the waves were in equilibrium with the wind, and therefore, represent average conditions. In our opinion the question of the most realistic values for $\sigma_c$ and $\sigma_u$ remains open.

In the MODIS algorithm, the following values are used

$$\sigma_c^2 = 2.73 \times 10^{-3} W$$
$$\sigma_u^2 = 2.46 \times 10^{-3} W.$$

They were chosen to minimize the variation of $\rho_t$ before MODIS enters saturation due to sun glitter and after it leaves saturation on the other side of the scan. In addition, $\rho_g$ was multiplied by a scaling factor of 0.90 for $\lambda \leq 551$ nm and 0.98 for $\lambda > 551$ nm to improve the performance.

The contribution of $\rho_g$ to the reflectance measured at the top of the atmosphere, $T\rho_g$, where $T$ is the direct transmittance of the atmosphere, is just

$$\rho_g \exp \left[-\tau \left(\frac{1}{\cos \theta} + \frac{1}{\cos \theta_0}\right)\right],$$

where $\tau$ is the total optical thickness of the atmosphere. However, there is a question the appropriateness of using the direct transmittance $T$. Near the center of the glitter pattern (the specular point) the sun glitter overwhelms all other components of the radiance and the radiance distribution is more in the form of a beam, for which the direct transmittance is appropriate. In contrast, away from the specular point, where direct sun glitter is a significantly smaller component of the radiance, e.g., comparable to the aerosol, the glitter radiance distribution is more diffuse, implying that the diffuse transmittance should be more appropriate. As such, it is not possible that a single transmittance factor, appropriate to all pixels, exists.

The sun glitter mask uses the wind vector $\vec{W}$ to estimate $\rho_g$ for each pixel, and if the estimate is larger than a threshold value the pixel is flagged and the normalized water-leaving radiance algorithm is not applied. As the aerosol optical thickness at a given pixel is unknown at the time of the application of the mask, the value determined at the previous pixel along the scan line is used. For pixels that are not masked (or saturated) a sun glitter correction is carried out. This consists of subtracting the computed reflectance $T\rho_g(\lambda)$ from each pixel along the scan line.
In order to correct the total radiance for the polarization sensitivity of MODIS (Section 3.1.1.8), it is important to note that the sun glitter displays partial linear polarization. The polarization properties are relatively easy to establish using the results from electromagnetic theory for reflection of electromagnetic waves from a flat dielectric interface. The only complication is referencing them to the standard reference system used in atmospheric optics — the plane formed by the direction of propagation of the light and the vertical. Here, we present the final results. The degree of polarization of the glitter, $P_g$ and the direction $\chi_g$ are given by

$$P_g = \frac{|r_-(\omega)|}{|r_+(\omega)|} \quad \text{and} \quad \chi_g = \frac{\pi}{2} - \alpha_r,$$

where

$$\sin \alpha_r = \frac{\sin \theta_0 \sin \phi}{\sin 2\omega}.$$

### 3.1.1.8 MODIS Polarization Sensitivity Effects

All scanning radiometers display some sensitivity to the polarization of the radiance they are intended to measure. For MODIS, it was specified that this polarization sensitivity should be less than 2% for all ocean bands (except the 412 nm band for which the agreed-upon limit of 2.3% was inadvertently left out of the final specifications). It was also specified that the polarization sensitivity (amplitude and phase) be mapped as part of the sensor characterization procedure.

The polarization sensitivity of MODIS can be specified in the following manner. Introduce completely (linearly) polarized monochromatic light into MODIS. Let the direction of polarization (the plane of oscillation of the electric field vector) of the incident light be specified by an angle $\chi$ measured with respect to a direction fixed relative to the sensor, e.g., the scan plane. Then, as the angle $\chi$ is varied through $360^\circ$, the output of the sensor will be

$$L^\text{Measured} = m_1 L^\text{Source} [1 + a \cos 2(\chi - \delta)],$$

where $L^\text{Source}$ is the (constant) radiance of the source, $m_1$ is a calibration constant, $L^\text{Measured}$ is the radiance “measured” by the sensor, $a$ the amplitude of the polarization sensitivity, and $\delta$ the phase angle of the polarization sensitivity. Both $a$ and $\delta$ are required to characterize the polarization sensitivity of the instrument. Figure 21 provides the measured values of $a$ for two of
the MODIS bands. Clearly, MODIS exceeds the polarization sensitivity specification at 869 nm and the polarization sensitivity is significantly larger at 412 nm.

Because MODIS does not meet the specifications in all bands, a correction is required to remove the residual polarization effects from \( \rho_l \). (The influence of uncorrected polarization sensitivity on the retrieved water-leaving reflectance \( \rho_w \) is similar to that of calibration errors, which are discussed in Section 3.1.3. Roughly, a 1% error in \( \rho_l \) at 412 nm leads to a 10% error in the retrieved \( \rho_w \).

![Figure 21. Polarization-sensitivity amplitude \( a \) for the Terra version of MODIS for Bands 8 (412 nm) and 16 (869 nm). S1 and S2 refer to the two sides of the MODIS scan mirror.](image)

when the chlorophyll \( a \) concentration is low.) Gordon [1988] developed a formalism that provides the framework for removal of instrument polarization-sensitivity effects. Briefly, a beam of partially polarized light can be described as the incoherent superposition of a beam of unpolarized light of radiance \( L_u \), and a beam of completely polarized light of radiance \( L_p \). The total radiance of the beam is then \( L_u + L_p \), and the degree of polarization, \( P \), is given by

\[
P = \frac{L_p}{L_u + L_p}.
\]

The polarized component, as above, is described by specifying the plane of oscillation of the electric field vector through the angle, \( \chi \), it makes with some reference direction. The partially polarized
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beam is then characterized by its radiance \( L_a + L_p \), its degree of polarization \( P \), and its direction of polarization specified by the angle \( \chi \). In atmospheric optics, the direction \( \chi \) is usually the angle of inclination of the plane of the electric field oscillations of \( L_p \) measured with respect to the plane containing the vertical and the direction of propagation. Specifying the polarization of the reflectance \( \rho_t \) in this manner, the measured reflectance (by the polarization-sensitive radiometer) is related to the true reflectance by

\[
\rho_t^{\text{Measured}} = \rho_t^{\text{True}} [1 + aP \cos 2(\chi - \delta)].
\]

We note that the maximum error in \( \rho_t \) is \( \pm aP \).

The difficulty with removing the polarization sensitivity error, i.e., recovering \( \rho_t^{\text{True}} \) from \( \rho_t^{\text{Measured}} \) given \( a \) and \( \delta \) is that the polarization properties of the radiance backscattered by the aerosol and the water are unknown. Gordon, Du and Zhang [1997a] developed an approximate method for reducing the instrument polarization effects. This method assumes the polarization of the light field at the sensor is that of a pure Rayleigh-scattering atmosphere. In this case,

\[
\rho_t^{\text{True}} = \frac{\rho_t^{\text{Measured}}}{[1 + aP_r \cos 2(\chi_r - \delta)]},
\]

where \( P_r \) and \( \chi_r \) are, respectively, the degree and direction of polarization in an aerosol-free atmosphere with \( \rho_w = 0 \). As the look up tables for the Rayleigh-scattering component \( \rho_r \) contain the complete Stokes vector, the polarization properties of this component of the light field are available within the processing code.

The Gordon, Du and Zhang [1997a] method was implemented in the first version of the algorithm. It uses an analysis of the polarization sensitivity for the instrument based on pre-launch characterization measurements. The polarization sensitivity measured for detector 5, the detector at the center of the linear array for each spectral bands, was used for each spectral band, as it was assumed to be the most accurate.

Prior to the first partial reprocessing, the polarization correction was revised. In the new correction procedure it is assumed that \( \rho_r \) is the only component of the light field that is polarized. That is, it is assumed that \( \rho_{ra}, \rho_a, \rho_{wc}, \rho_g, \) and \( \rho_w \) are totally unpolarized, i.e., the degree of
polarization associated with these individual components is zero. Then,

\[
\rho_t^{\text{True}} = \frac{\rho_t^{\text{Measured}}}{[1 + aP \cos 2(\chi_r - \delta)]},
\]

where

\[ P = P_r \frac{\rho_r}{\rho_t^{\text{True}}}. \]

Note that the unknown \( \rho_t^{\text{True}} \) in the above equation for \( P \) can be replaced by \( \rho_t^{\text{Measured}} \) with little loss in accuracy. Figure 22 shows the efficacy of this revised correction method using simulated

![Figure 22](image.png)

Figure 22. Efficacy of the revised polarization-sensitivity correction method. The true degree of polarization is compared to that in a pure Rayleigh scattering atmosphere and that in which all other contributors to the radiance are unpolarized. The computations are for a wavelength of 869 nm and the geometry is the perpendicular plane (similar to the MODIS scan at moderate sun angles) for a solar zenith angle of 40°. The aerosol model M70, characteristic of the MOBY calibration site, is used in the simulation. Left panel is for \( \tau_a(869) = 0.05 \) (a clear maritime atmosphere) and the right panel is for \( \tau_a(869) = 0.10 \) (a more typical maritime atmosphere).

data. Figures 21 and 22 also underscore the importance of this correction. In an aerosol-free atmosphere, \( P \) is similar at all wavelengths and \( P \approx 0.5 \) near the scan edge. At one edge of the scan, where \( a \approx 0.06 \) and 0.03 at 412 and 869, the error in the uncorrected \( \rho_t \) could be as much as ±2.5% and 1.5%, respectively.

Finally, as the polarization of the sun glitter contribution \( T \rho_g \) is relatively straightforward to determine, it has been included in the correction. The full polarization-sensitivity correction in use
at the completion of this document is
\[ \rho_t^{\text{True}} = \frac{\rho_t^{\text{Measured}}}{[1 + aP \cos 2(\chi - \delta)]}, \]

where \( P \) and \( \chi \) are found from
\[
\begin{align*}
P \cos 2\chi &= \frac{\rho_r P_r \cos 2\chi_r + T \rho_g P_g \cos 2\chi_g}{\rho_t^{\text{True}}}, \\
P \sin 2\chi &= \frac{\rho_r P_r \sin 2\chi_r + T \rho_g P_g \sin 2\chi_g}{\rho_t^{\text{True}}},
\end{align*}
\]

and the sun glitter reflectance, \( \rho_g \), degree of polarization, \( P_g \), and direction of polarization \( \chi_g \) are provided in Section 3.1.1.7. As before, the unknown \( \rho_t^{\text{True}} \) in the above equations for \( P \) and \( \chi \) is replaced by \( \rho_t^{\text{Measured}} \).

### 3.1.1.9 Non-zero \([\rho_w]_N \) in the NIR

A fundamental assumption in the atmospheric correction algorithm is that \([\rho_w]_N = 0 \) in the NIR (748 and 869 nm for MODIS). However, it is well known that at high chlorophyll \( a \) concentrations there is a small, but non-zero, water-leaving reflectance in the NIR, even in Case 1 waters. Therefore, it is necessary to estimate \([\rho_w]_N \) in the NIR. A scheme for effecting this was provided by Siegel et al. [2000] for SeaWiFS, and has been adapted to operate with the MODIS spectral bands.

The water-leaving reflectance can be written \([Gordon et al., 1988]\)
\[
[\rho_w]_N \approx 1.7 \sum_{i=1}^{2} g_i \left[ \frac{b_i}{a + b_i} \right]^i, \tag{22}
\]

where \( a \) is the absorption coefficient of the water plus constituents, \( b_i \) the backscattering coefficient, \( g_1 = 0.0949 \), \( g_2 = 0.0794 \), and the factor 1.7 accounts to the transmission and refraction effects across the air-sea interface. In the NIR, the absorption by sea water is large, so \( a \) can be replaced by \( a_w \), the absorption coefficient of pure sea water. The backscattering coefficient can be decomposed into that due to particles and that due to water:
\[ b_i = b_{ip} + b_{bw}. \]
Morel [1988] has related \( b_{bp} \) to the concentration of chlorophyll \( a \) (\( C \)) and the wavelength through

\[
b_{bp}(\lambda) = 0.416 C^{0.766} \left[ 0.002 + 0.02(0.5 - 0.25 \log_{10} C) \left( \frac{550}{\lambda} \right) \right].
\]

Table 3 provides the values of \( a_w \) and \( b_{bw} \) used in the estimation of \( [\rho_w]_N \).

**Table 3:** Parameters needed for Eq. (22).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Wavelength (nm)</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>748</td>
<td>869</td>
</tr>
<tr>
<td>( a_w ) (m(^{-1}))</td>
<td>2.586</td>
<td>4.436</td>
</tr>
<tr>
<td>( b_{bw} ) (m(^{-1}))</td>
<td>0.00024</td>
<td>0.00014</td>
</tr>
</tbody>
</table>

The estimate of \( [\rho_w]_N \) is incorporated in the atmospheric correction algorithm in the following manner. First, an atmospheric correction is carried out assuming that \( [\rho_w]_N = 0 \) in the NIR. The retrieved reflectances are then used in a ratio algorithm, e.g., similar to Figure 2, to estimate the concentration of chlorophyll \( a \). The estimate of \( C \) (if greater than 0.3 mg/m\(^3\)) is then used to estimate \( [\rho_w]_N \) in the NIR using the above relationships. The estimate of \( [\rho_w]_N \) in the NIR is used to estimate \( t^*\rho_w \) in the NIR, which is then subtracted from \( \rho_t \) and the atmospheric correction algorithm operated again. This procedure is carried out until the retrieved \( C \) changes by less than 20% from the previous iteration, up to a maximum of four iterations.

3.1.1.10 Estimation of Aerosol Optical Depth \( \tau_a \)

There is considerable interest now in the global distribution of aerosols because of their role in climate forcing and biogeochemical cycling [Charlson et al., 1992]. The hypothesis [Charlson et al., 1987] that dimethylsulfide (DMS) from phytoplankton activity leads to an increase in cloud condensation nuclei in the marine atmosphere argues for simultaneous study of aerosols and productivity where possible [Falkowski et al., 1992]. There has been effort in recent years directed toward estimating the aerosol concentration (\( \propto \tau_a \)) and other properties using Earth-orbiting satellites [Durkee et al., 1986; Fraser, 1976; Griggs, 1975; Griggs, 1981; Griggs, 1984; Griggs, 1981; Koepke and Quenzel, 1979; Koepke and Quenzel, 1981; Mekler et al., 1977; Rao et al., 1988]. In this section we show that \( \tau_a \) can be retrieved with a simple extension of the atmospheric correction algorithm.
Even in the single scattering approximation, one notes from Eq. (9) that it is not possible to estimate \( \tau_a \) without assuming a model for the aerosol to provide \( \omega_a \) and \( P_a \). For example, Rao et al. [1988] assume that the aerosol consists of spherical particles with a size frequency distribution \( \propto (\text{radius})^{-4.5} \) and a refractive index of 1.5. The assumption of an incorrect model can produce significant errors (up to a factor of 2–3) in the recovered \( \tau_a \). As in atmospheric correction, we will try to avoid using an incorrect model in the retrieval of \( \tau_a \) by utilizing the only other aerosol information available on a pixel-by-pixel basis — the spectral variation of \( \rho_{os} \).

Our retrieval algorithm is a simple extension of the atmospheric correction algorithm, i.e., the correction algorithm yields the two models which most closely bracket \( \varepsilon(765, 865) \), and we use these two models to invert Eq. (9) to obtain two estimates of \( \tau_a \). As with the atmospheric correction, it is necessary to know the absorption properties of the aerosol. Assuming the aerosols are weakly absorbing, i.e., that the aerosol consists of particles that are accurately described by the Maritime, Coastal, or Tropospheric aerosol models with RH = 80%, \( \rho_t \) is simulated for this aerosol and inserted into the multiple-scattering atmospheric correction algorithm. The correction algorithm provides two candidate models based on \( \varepsilon(765, 865) \) and these specify two sets of \( P_a \) and \( \omega_a \) values for two estimates of \( \tau_a \). The estimated value of \( \tau_a \) is then determined from the weighted average of the two estimates as in the correction algorithm. Tables 4 and 5 provide the % error in the retrieved \( \tau_a(865) \) for three aerosol models at the center and the edge of the MODIS scan as a function of \( \theta_0 \). The true value of \( \tau_a(865) \) was 0.2 or 0.4. All the calculations were carried out for

<table>
<thead>
<tr>
<th>Position</th>
<th>( \theta_0 )</th>
<th>Error (%) in ( \tau_a(865) )</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Maritime</td>
<td>Coastal</td>
</tr>
<tr>
<td>Center</td>
<td>20°</td>
<td>+17.4</td>
</tr>
<tr>
<td></td>
<td>40°</td>
<td>−1.53</td>
</tr>
<tr>
<td></td>
<td>60°</td>
<td>+2.96</td>
</tr>
<tr>
<td>Edge</td>
<td>0°</td>
<td>+0.55</td>
</tr>
<tr>
<td></td>
<td>20°</td>
<td>+1.31</td>
</tr>
<tr>
<td></td>
<td>40°</td>
<td>+2.41</td>
</tr>
<tr>
<td></td>
<td>60°</td>
<td>+3.71</td>
</tr>
</tbody>
</table>
$\phi_e = 90^\circ$. From the tables, we can see that the error in the retrieved aerosol optical thickness is typically within $\pm 10\%$ (and usually considerably less) for most of the cases examined.

Finally, it is of interest to estimate the upper limit to the value of $\tau_a(865)$ that can be estimated with SeaWiFS or MODIS given its design saturation reflectance ($\rho_{\text{max}}$). This is dependent on the particular aerosol model because for a given $\tau_a$ the backscattering (scattering at angles $>90^\circ$)

<table>
<thead>
<tr>
<th>Position</th>
<th>$\theta_0$</th>
<th>Error (%) in $\tau_a(865)$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Maritme</td>
</tr>
<tr>
<td>Center</td>
<td>20°</td>
<td>+16.9</td>
</tr>
<tr>
<td></td>
<td>40°</td>
<td>-1.03</td>
</tr>
<tr>
<td></td>
<td>60°</td>
<td>+3.78</td>
</tr>
<tr>
<td>Edge</td>
<td>0°</td>
<td>+1.12</td>
</tr>
<tr>
<td></td>
<td>20°</td>
<td>+1.87</td>
</tr>
<tr>
<td></td>
<td>40°</td>
<td>+3.41</td>
</tr>
<tr>
<td></td>
<td>60°</td>
<td>+6.49</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Position</th>
<th>$\theta_0$</th>
<th>Maximum value of $\tau_a(865)$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Maritime (RH = 98%)</td>
</tr>
<tr>
<td>Center</td>
<td>20°</td>
<td>0.72</td>
</tr>
<tr>
<td></td>
<td>40°</td>
<td>1.04</td>
</tr>
<tr>
<td></td>
<td>60°</td>
<td>1.69</td>
</tr>
<tr>
<td>Edge</td>
<td>0°</td>
<td>0.88</td>
</tr>
<tr>
<td></td>
<td>20°</td>
<td>0.98</td>
</tr>
<tr>
<td></td>
<td>40°</td>
<td>1.04</td>
</tr>
<tr>
<td></td>
<td>60°</td>
<td>1.02</td>
</tr>
</tbody>
</table>

is strongly dependent on the aerosol size distribution and the refractive index. We estimate the upper limit of $\tau_a(865)$ that can be estimated by using the Tropospheric model with RH = 70% (largest backscattering of the models used here) and the Maritime model with RH = 98% (small backscattering). The results are presented in Table 6.
3.1.1.11 Ancillary Data

Several sets of ancillary data are required to operate the \([\rho_w]_N\) retrieval algorithm. These are listed in Table 7. They may be needed on at most a 1° × 1° latitude-longitude grid, but probably a coarser grid, e.g., 3° × 3° will be sufficient considering the expected quality of some of the data. We will discuss each ancillary data set required below.

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Ancillary Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\rho_t(\lambda_i))</td>
<td>(F_0(\lambda_i))</td>
</tr>
<tr>
<td>(\rho_r(\lambda_i))</td>
<td>(\tau_{O_2}(\lambda_i), W, P_0)</td>
</tr>
<tr>
<td>(\rho_{wc}(\lambda_i))</td>
<td>(W, \Delta T, T_W)</td>
</tr>
<tr>
<td>(\rho_g(\lambda_i))</td>
<td>(\tilde{W})</td>
</tr>
<tr>
<td>(t(\lambda_i))</td>
<td>(\tau_{O_2}(\lambda_i), P_0)</td>
</tr>
<tr>
<td>(T(\lambda_i))</td>
<td>(\tau_{O_2}(\lambda_i), P_0, \tau_a(\lambda_i))</td>
</tr>
<tr>
<td>(\epsilon(\lambda_i, \lambda_j))</td>
<td>RH</td>
</tr>
</tbody>
</table>

3.1.1.11.1 Extraterrestrial Solar Irradiance \(F_0\)

Unless MODIS is calibrated directly in reflectance units, the extraterrestrial solar irradiance is required to convert from \(L_t\) to \(\rho_t\). It is planned that this be taken from Neckel and Labs [1984] unless newer, more accurate, determinations become available in the future. In the event that MODIS is calibrated directly in reflectance units, this quantity is only needed to turn \([\rho_w]_N\) into the desired \([L_w]_N\) and to effect the appropriate out-of-band corrections (see Section 3.1.1.8.5).

3.1.1.11.2 Ozone Optical Thickness

In the radiative transfer model the atmosphere is assumed to be composed of three layers.
The top is the Ozone layer and is non-scattering, the second is a molecular scattering layer and the third is the aerosol layer. The Ozone optical thickness \( \tau_{O_2}(\lambda) \) is needed to compute the two way transmittance of \( \rho_r, \rho_w, \rho_{we} \) and \( \rho_g \) through the Ozone layer. Since the Ozone absorption is small (\( \tau_{O_2} \lesssim 0.035 \)) high accuracy is not needed. It is estimated that an error in the Ozone concentration of \( \sim 20 - 40 \) mAtm-cm (Dobson Units) could be tolerated. These data are acquired from the Goddard DAAC.

3.1.1.11.3 Surface Atmospheric Pressure \( P_0 \)

The atmospheric pressure is needed to compute the Rayleigh optical thickness \( (\tau_r) \) required for the computation of \( \rho_r \). It is also used in the transmittances \( t \) and \( T \). The value of \( \tau_{r0} \), the Rayleigh optical thickness at the standard atmospheric pressure \( P_0 \) of 1013.25 mb is given by [Hansen and Travis, 1974]

\[
\tau_{r0} = 0.008569 \lambda^{-4} \left(1 + 0.0113 \lambda^{-2} + 0.00013 \lambda^{-4}\right),
\]

where \( \lambda \) is in \( \mu \text{m} \). At any surface pressure \( P \), the Rayleigh optical depth is

\[
\tau_r = \frac{P}{P_0} \tau_{r0}.
\]

An error \(< \pm 5 \) mB should be sufficient for the computation of \( \tau_r \). The source of this data set will be the output of numerical weather models.

3.1.1.11.4 Wind Speed \( W \) and Wind Vector \( \hat{W} \)

The wind speed, if known, is used in the computation of \( \rho_r \), otherwise \( \rho_r \) is computed with \( W = 0 \). It is also required for the estimation of \( [\rho_{we}] \). The wind vector is required for the construction of a glint mask, i.e., a mask to remove areas contaminated by sun glint from the imagery before processing. The importance of creating a realistic mask is that good data may be masked if the mask is made in too conservative a manner. An error of \(< 1 - 2 \) m/s in the speed and \(< 30^\circ \) on the direction should be sufficient. The source of this data set will be the output of numerical weather models.

3.1.1.11.5 Sea Surface Temperature and Atmospheric Stability

It was originally thought that these may be needed to estimate \( [\rho_{we}] \), if another estimate
replaces Koepke’s (Eq. (20)), e.g., Monahan and O’Muircheartaigh [1986]. However, use of Eq. (21) obviates the need for these quantities.

3.1.1.11.6 Relative Humidity RH

The surface relative humidity (RH) is not really needed by the algorithm; however, it could be useful as a constraint on the candidate aerosol models chosen by the algorithm as described in Section 3.1.1.3. The error in the value of RH should be $< \pm 5 – 10\%$ to be useful. The source of this data set will be the output of numerical weather models.

3.1.1.11.7 Total Column Water Vapor

Total column water vapor is needed to effect out-of-band corrections for MODIS spectral bands near strong atmospheric water vapor absorption features. The accuracy needed is expected to be $\sim \pm 0.5 - 1$ gm/cm$^2$. The source of this data set will be the output of numerical weather models.

All of the meteorological data ($P$, $\bar{W}$, $T_W$, $\Delta T$, RH, and water vapor) will be acquired from NOAA by the GSFC Data Assimilation Office (DAO) and then supplied to the GSFC DAAC. MODIS will acquire the data fields directly from the GSFC DAAC.

3.1.1.12 Second-Order Effects

In this section we examine the adequacy of the various approximations that were made in the development of the algorithm.

3.1.1.12.1 Aerosol Vertical Structure

The reflectance of the atmosphere in the single-scattering approximation is independent of the manner in which the aerosol is distributed with altitude. However, this independence does not extend to a multiple-scattering atmosphere. As the multiple-scattering algorithm assumes that the aerosol is all located in the bottom layer of a two-layer atmosphere, it is important to understand the effect of aerosol vertical structure on the correction algorithm. This has been studied by comparing the error in the algorithm when the pseudo data are simulated using the “correct” two-layer model, i.e., all of the aerosol at the bottom of the atmosphere as assumed in the algorithm, with the error
when the pseudo data are simulated using a model in which the aerosol and Rayleigh scattering have an altitude-independent mixing ratio, i.e., a uniformly mixed model. Figure 23 (left panel) provides such a comparison for the M80 and T80 aerosol models with $\tau_a(865) = 0.2$. It is seen that the effect of an incorrect assumption regarding the vertical structure will not lead to serious errors in this case. However, in the case of strongly absorbing aerosols, e.g., the Urban models, the assumed vertical structure is very important. Figure 23 (right panel) provides the two-layer versus uniformly mixed cases for the Urban models with $\tau_a(865) = 0.2$. In this case the candidate aerosol models were restricted to U50, U70, U90, and U99, as in the results for Figure 13. For the U80 case, the error becomes excessive, increasing by over an order of magnitude compared to the two-layer case. More disturbing is the performance of the U70 aerosol model. U70 is actually one of the candidate aerosol models in this case. When the vertical structure is the same as assumed by the algorithm, the error is negligible. In contrast, when the incorrect structure is assumed, the error becomes very large.

![Figure 23](image_url)

Figure 23. Effect of the vertical distribution of aerosol on $\Delta[\rho_v(443)]_N$ as a function of $\theta_0$ at the edge of the scan $\tau_a(865) = 0.2$. Note that the correction algorithm assumes that the “Two-layer” stratification is correct. Left panel: T80 and M80. Right panel: U70 and U80.

As we have examined only an extreme deviation from that assumed by the correction algorithm, it is of interest to quantify how the correction algorithm performs as the aerosol layer thickens from being confined just near the surface to being mixed higher in the atmosphere. Thus, the top-of-atmosphere reflectance was simulated using a two layer model with aerosol *plus* Rayleigh scattering.
in the lower layer and only Rayleigh scattering in the upper layer. The fraction of the Rayleigh scattering optical thickness assigned to the lower layer was consistent with aerosol-layer thickness of 0, 1 km, 2 km, 4 km, 6 km, and ∞. The aerosol model used in the simulations was U80, and \( \tau_a(865) \) was kept constant at 0.2. The multiple-scattering algorithm was then operated with this pseudo data using U50, U70, U90, and U99 as candidate models. The results of this exercise are provided in Figure 24. Clearly, progressive thickening of the layer in which the aerosol resides leads to a progressive increase in the error in the retrieved water-leaving reflectance.

This influence of vertical structure on the algorithm when the aerosol is strongly absorbing is easy to understand. The algorithm assumes all of the aerosol resides in a thin layer beneath the molecular scattering layer. As the aerosol layer thickens and encompasses more and more of the molecular scattering layer, the amount of Rayleigh scattering within the aerosol layer will increase causing an increase in the average path length of photons through the layer, and a concomitant

![Figure 24](image)

*Figure 24. Effect of the vertical distribution of aerosol on \( \Delta[\rho_w(443)]_N \) as a function of \( \theta_0 \) at the edge of the scan for the U80 aerosol models with \( \tau_a(865) = 0.2 \). Curves from top to bottom refer to situations in which the aerosol is confined to a layer just above the surface, between the surface and 1, 2, 4, and 6 km, and uniformly mixed throughout the atmosphere.*

increase in absorption. In addition, as the aerosol moves higher into the atmosphere, less Rayleigh
scattering from the lower atmosphere will reach the TOA than would were the aerosol layer at the surface. The influence of the vertical extent of a strongly-absorbing aerosol layer is shown graphically in Figure 25 which relates the spectral variation of \( \rho_a + \rho_{ra} = \rho_t - \rho_r - t \rho_w \) to the thickness of the aerosol layer for a fixed \( \tau_a(865) \) of 0.2. Clearly, for a given \( \tau_a \), \( \rho_t \) will decrease as the thickness of the aerosol layer increases. This decrease is relatively more in the visible than in the NIR, so as the layer thickens, the algorithm will predict values of \( \rho_a + \rho_{ra} \) in the visible that are too large, yielding an over correction, \( \Delta [\rho_w(443)]_N < 0 \). Note that the behavior of \( \rho_a + \rho_{ra} \) in the NIR provides little or no information regarding the vertical distribution of the aerosol.

*Ding and Gordon* [1995] (Figures 9 and 10) have provided some examples of the error in the multiple-scattering algorithm for vertical structures in which the aerosol model as well as concentration varies with altitude. For the weakly-absorbing aerosol of the models that they investigated (\( \omega_a \gtrsim 0.93 \)), the conclusions are similar to those here: as long as the aerosol is weakly absorbing, the error is negligible, but as \( \omega_a \) decreases, the error becomes progressively larger. Clearly, more
study is required for a quantitative assessment of the impact of vertical structure in a strongly absorbing atmosphere; however, the computations provided here demonstrate that a large error in the vertical structure of the aerosol layer assumed for the lookup tables will result in a very poor atmospheric correction, even if the candidate aerosol models are appropriate. Figures 24 and 25 suggest that at a minimum, the lookup tables for the Urban candidates need to be recalculated under the assumption of an aerosol layer of finite physical thickness, i.e., some Rayleigh scattering in the aerosol layer. It also suggests that, for the case studied, if the lookup tables were computed for an aerosol layer of physical thickness 2 km, they would provide reasonable retrievals for layers with thicknesses from 1 to 3 km, i.e., the algorithm could tolerate a ±1 km error in the layer thickness for this case. The influence of absorbing aerosols and methods for atmospheric correction in their presence is discussed further in Chapter 5.

3.1.1.12.2 Earth-Atmosphere Curvature Effects

All atmospheric corrections algorithms developed thus far ignore the curvature of the earth, i.e., the plane-parallel atmosphere approximation has been used in the radiative transfer simulations. However, at the level of accuracy required to utilize the full sensitivity of MODIS, it may be necessary to take the curvature of the earth into account, especially at high latitudes with their associated large $\theta_0$ values. Ding and Gordon [1994] have examined this problem in detail using a model based on a spherical shell atmosphere solved with Monte Carlo techniques. It was found that as long as $\rho_e$ was computed using a spherical shell atmosphere model, the multiple-scattering algorithm performed as well at high latitudes as at low latitudes. They provided a method for the computation of $\rho_e$ for the spherical shell atmosphere; however, it has yet to be implemented for image processing.

3.1.1.12.3 Aerosol Polarization

All of the radiative transfer simulations described in Section 3.1.1 were carried out using scalar radiative transfer theory, i.e., polarization was ignored. In the case of single scattering, except for the terms involving the Fresnel reflectance, scalar (ignores polarization) and vector (includes polarization) radiative transfer theory lead to the same radiances. Thus, the single scattering algorithm is little influenced by polarization. It is well known, however, that, when multiple scattering
is present, the use of scalar theory leads to small errors (\(\sim \text{few} \%)\) in the radiance compared to that computed using exact vector theory [Gordon, Brown and Evans, 1988; Kattawar, Plass and Hitzfelder, 1976]. As with CZCS, in the actual application of the algorithm, \(\rho_r\) is computed using vector theory; however, the lookup tables relating \(\rho_a + \rho_{ra}\) to \(\rho_{as}\) have been computed using scalar theory. To understand the influence of neglecting polarization in the computation of the lookup tables, simulations of the top-of-the-atmosphere reflectance \(\rho_t\) were carried out using both scalar and vector radiative transfer theory. In the case of the scalar simulations, \([\rho_w(443)]_N\) was retrieved as described in Section 3.1.1.3. An identical retrieval procedure was used for the vector simulations with a single exception: as in the case of CZCS, \(\rho_r\) was computed using vector theory. The results are presented in Figure 26 for the M80 and T80 aerosol models. These figures provide

\[
\Delta \rho = t \Delta \rho_w(443) \quad \text{(rather than } \Delta [\rho_w(443)]_N \text{ in the previous figures)}
\]

produced by the multiple-scattering correction algorithm as a function of \(\theta_0\) for \(\tau_a(865) = 0.2\). The notation “S–S” and “V–V” means that both \(\rho_t\) and \(\rho_r\) were computed using scalar (S–S) and vector (V–V) radiative transfer theory, respectively. Note that the difference between computations is the error induced by ignoring polarization in the preparation of the \(\rho_a + \rho_{ra}\) versus \(\rho_{as}\) lookup tables. At present, only a small number of simulations of the type shown in Figure 26 have been carried out; however, for these the difference between S–S and V–V was typically \(\lesssim 0.001\) but reached as much as 0.002 in isolated cases. Thus, compared to the errors possible when strongly absorbing aerosols are present,
this error appears negligible. It could be removed by recomputing the look up tables using vector radiative transfer theory, but at considerable computational cost.

3.1.1.12.4 Sea surface roughness

The roughness of the sea surface caused by the wind can play a large role on the reflectance measured at the top of the atmosphere. The principal effect of the rough surface is to redirect the direct solar beam reflected from the sea surface into a range of angles. This leads to a very large reflectance close to the specular image of the sun, know as sun glitter or the sun’s glitter pattern.

As this can be many times the radiance exiting the atmosphere in the smooth-surface case, the data in the region of the sun glitter must be discarded. This is accomplished by a mask as described in Section 3.1.1.7. The remainder of the rough-surface effect is due to a redistribution of light scattered from the reflected solar beam (because it is redirected) and a redistribution of sky light reflected from the surface (the Fresnel reflection terms in Eq. (9)). This redistribution of radiance contaminates the imagery over all viewing angles. As the lookup tables relating \( \rho_a + \rho_{ra} \) to \( \rho_{as} \) were computed under the assumption that the surface was flat, it is necessary to examine the error in the water-leaving reflectance induced when viewing a rough ocean. This was effected by computing \( \rho_t \) for an ocean roughened by the wind and inserting the result into the multiple-scattering correction

![Graphs showing the effect of sea surface roughness on reflectance](image)
algorithm. In this simulation, the sea surface roughness was based on the Cox and Munk [1954] surface slope distribution function. For computational simplicity, an omnidirectional wind was assumed [Cox and Munk, 1954]. The wind speed was taken to be $\sim 7.5$ m/s. Since Gordon and Wang [1992b] and Gordon and Wang [1992a] showed that at the radiometric sensitivity of SeaWiFS and MODIS, correct computation of the influence of surface roughness on $\rho_r$ required use of vector radiative transfer theory, the computations were carried out using both scalar and vector theory. Sample results from one set of the small number of simulations that have been carried out to assess the effect of surface roughness are provided in Figure 27. These are in the same format as Figure 26. The differences between the two panels is that, in Figure 27 (left panel) $\rho_r$ has been computed assuming a smooth sea surface (a wind speed of zero), while in Figure 27 (right panel) it has been computed using the correct (7.5 m/s) wind speed. For reference, Figure 26 (left panel) provides similar results for a smooth sea surface. Comparing Figures 26 and 27 (left panels) shows that the residual effect of the rough surface external to the sun’s glitter pattern is small ($\Delta \rho \sim 0.0005$), and comparing Figures 26 (left panel) and 27 (right panel) shows that the residual effect can be removed by using the correct wind speed in the computation of $\rho_r$, i.e., ignoring the surface roughness in computation of the lookup tables relating $\rho_a + \rho_{ra}$ to $\rho_{as}$ does not appear to lead to significant error.

In the present version of the algorithm, both polarization and wind speed (but not direction) are included in the computation of $\rho_r$.

### 3.1.1.12.5 Out-of-band Response

In the development of the algorithm, it has been assumed that the MODIS spectral bands were monochromatic, i.e., the reflectance $\rho_t$ is measured at discrete wavelengths. However, the MODIS bands actually average the reflectance over spectral regions that are nominally 10–15 nm wide. Also, the possibility exists that there could be significant out-of-band response, i.e., contributions to the reflectance from spectral regions far from the band center. This problem was particularly severe in the case of the SeaWiFS band at 865 nm [Barnes et al., 1994], for which $\sim 9\%$ of the power measured in this band when observing Rayleigh-scattered sun light originates at wavelengths shorter than 600 nm. Gordon [1995] has developed a methodology for delineating the influence of finite spectral band widths and significant out-of-band response of sensors for remote sensing of
ocean color. The basis of the method is the application of the sensor’s spectral response functions to the individual components of the TOA radiance rather than the TOA radiance itself.

Let \( S_i(\lambda) \) be the spectral response of the \( i^{th} \) spectral band. \( S_i(\lambda) \) provides the output current (or voltage) from the detector for a unit radiance of wavelength \( \lambda \), e.g., \( \int S_i(\lambda) \, d\lambda \) would be the output current for a spectrally flat source of radiance of magnitude 1 mW/cm\(^2\)µm Sr. We define the “band” radiance for the \( i^{th} \) spectral band when viewing a source of radiance \( L(\lambda) \) to be

\[
\langle L(\lambda) \rangle_{S_i} = \frac{\int L(\lambda) S_i(\lambda) \, d\lambda}{\int S_i(\lambda) \, d\lambda}
\]  

(23)

The output current (or voltage) will then be \( \propto \langle L(\lambda) \rangle_{S_i} \).

Given \( S_i(\lambda) \), we can compute the band-averaged quantities needed to operate the algorithm following Gordon [1995]. These are \( \langle F_0(\lambda) \rangle_{S_i} \), \( \langle k_{Oz}(\lambda) \rangle_{F_0 S_i} \), and \( \langle \tau_r(\lambda) \rangle_{F_0 S_i} \), where \( k_{Oz}(\lambda) \) is the Ozone absorption coefficient defined so that the Ozone spectral optical depth for a concentration of \( DU \) (Dobson units or milliatmosphere centimeters) is

\[
\tau_{Oz}(\lambda) = k_{Oz}(\lambda) \frac{DU}{1000}
\]

\[
\langle k_{Oz}(\lambda) \rangle_{F_0 S_i} = \frac{\int k_{Oz}(\lambda) F_0(\lambda) S_i(\lambda) \, d\lambda}{\int F_0(\lambda) S_i(\lambda) \, d\lambda},
\]

(24)

and

\[
\langle \tau_r(\lambda) \rangle_{F_0 S_i} = \frac{\int \tau_r(\lambda) F_0(\lambda) S_i(\lambda) \, d\lambda}{\int F_0(\lambda) S_i(\lambda) \, d\lambda}.
\]

(25)

We have computed these band-averaged quantities using the MODIS relative spectral response functions (Table 8). In addition, we examined the influence of the water vapor absorption bands on the computation of the Rayleigh reflectance. For MODIS, the error in ignoring water vapor (up to a concentration of 3.3 g/cm\(^2\)) is a maximum of 0.25% (for Band 15). For the other spectral bands,
the error is < 0.1%. In contrast, for SeaWiFS the maximum error is 0.55%.

Table 8: Band-averaged quantities needed to compute the Rayleigh reflectance and the Ozone transmittance for the MODIS bands.

<table>
<thead>
<tr>
<th>λ (nm)</th>
<th>Band (i)</th>
<th>( \langle \tau_r(\lambda) \rangle_{F_0 S_i} )</th>
<th>( \langle F_0(\lambda) \rangle_{S_i} ) mW/cm²μm sr</th>
<th>( \langle k_O(\lambda) \rangle_{F_0 S_i} ) (×1000)</th>
</tr>
</thead>
<tbody>
<tr>
<td>412</td>
<td>8</td>
<td>0.3167</td>
<td>170.37</td>
<td>1.47</td>
</tr>
<tr>
<td>443</td>
<td>9</td>
<td>0.2377</td>
<td>186.50</td>
<td>3.78</td>
</tr>
<tr>
<td>488</td>
<td>10</td>
<td>0.1610</td>
<td>191.82</td>
<td>22.21</td>
</tr>
<tr>
<td>531</td>
<td>11</td>
<td>0.1135</td>
<td>188.57</td>
<td>65.66</td>
</tr>
<tr>
<td>551</td>
<td>12</td>
<td>0.0999</td>
<td>187.16</td>
<td>83.22</td>
</tr>
<tr>
<td>667</td>
<td>13</td>
<td>0.0446</td>
<td>154.15</td>
<td>48.69</td>
</tr>
<tr>
<td>687</td>
<td>14</td>
<td>0.0417</td>
<td>149.88</td>
<td>39.95</td>
</tr>
<tr>
<td>748</td>
<td>15</td>
<td>0.0286</td>
<td>128.07</td>
<td>12.02</td>
</tr>
<tr>
<td>869</td>
<td>16</td>
<td>0.0156</td>
<td>97.30</td>
<td>3.75</td>
</tr>
</tbody>
</table>

Finally, the presence of other absorbing gases, over and above Ozone, e.g., water vapor, and the out-of-band response will also influence the aerosol part of the atmospheric correction algorithm. Gordon [1995] showed that this can be taken into account by introducing a factor \( f_i \) (for band \( i \)) defined by

\[
f_i = \frac{\langle \varepsilon(\lambda, 865) \rangle_{F_0 S_i}}{\varepsilon(\lambda_i, 865)}.
\]

where \( \lambda_i \) is the nominal center wavelength for band \( i \), i.e., the wavelength at which the radiative transfer simulations are carried out to produce the lookup tables required by the algorithm. The algorithm is then operated in the normal manner, but with Eq. (13) replaced by

\[
\langle \rho_a(\lambda) + \rho_{ra}(\lambda) \rangle_{F_0 S_i} = f_i K[\lambda, \rho_{as}(\lambda_i)] \rho_{as}(\lambda_i).
\]

Approximating \( \varepsilon(\lambda_i, \lambda_i) \) by

\[
\varepsilon(\lambda_i, \lambda_i) = \exp[c(\lambda_i - \lambda_i)],
\]

where \( c \) is a constant, and using LOWTRAN to compute the atmospheric transmittance, Gordon [1995] found that

\[
f_i = f_i(c, M, w),
\]
where $M$ is the two-way air mass $(1/\cos \theta_v + 1/\cos \theta_o)$ and $w$ is the column water vapor concentration. This function can be approximated by an equation of the form

$$f_i(c, M, w) = (a_{01} + a_{02}M) + (a_{03} + a_{04}M)c$$

$$+ \left[(a_{11} + a_{12}M) + (a_{13} + a_{14}M)c\right]w$$

$$+ \left[(a_{21} + a_{22}M) + (a_{23} + a_{24}M)c\right]w^2.$$  \hspace{1cm} (26)

Only in the case of Bands 13 (667 nm) and 15 (749 nm) does $f_i$ differ from unity by more than 1%.

Table 9: Coefficients $a_{nm}$ in Eq. (26) for MODIS Bands 12–16, for $c$ in nm$^{-1}$ and $w$ in gm/cm$^2$. Notation ±2 stands for 10$^{±2}$, etc.

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>$a_{nm}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Band 12</td>
</tr>
<tr>
<td>$a_{01}$</td>
<td>+1.000 −0</td>
</tr>
<tr>
<td>$a_{02}$</td>
<td>−4.530 −6</td>
</tr>
<tr>
<td>$a_{03}$</td>
<td>+4.389 +0</td>
</tr>
<tr>
<td>$a_{04}$</td>
<td>−1.887 −4</td>
</tr>
<tr>
<td>$a_{11}$</td>
<td>−2.210 −5</td>
</tr>
<tr>
<td>$a_{12}$</td>
<td>−9.093 −6</td>
</tr>
<tr>
<td>$a_{13}$</td>
<td>+1.498 −3</td>
</tr>
<tr>
<td>$a_{14}$</td>
<td>+1.225 −3</td>
</tr>
<tr>
<td>$a_{21}$</td>
<td>+2.646 −6</td>
</tr>
<tr>
<td>$a_{22}$</td>
<td>+1.002 −6</td>
</tr>
<tr>
<td>$a_{23}$</td>
<td>+1.395 −4</td>
</tr>
<tr>
<td>$a_{24}$</td>
<td>−2.259 −4</td>
</tr>
</tbody>
</table>

However, except for Bands 8–11, $f_i$ differs from unity by more than 0.5%, so correction is required. The coefficients $a_{nm}$ have been computed for the individual MODIS spectral bands (12–16). The values of $a_{nm}$ for these bands are provided in Table 9.

### 3.1.1.13 Remaining Issues

Although the algorithm described above has been implemented and used for Terra MODIS processing, there are other questions and issues that are also being studied but are not included in the present processing code. These are outlined in the present section. Plans for enhancing the processing code to address some of these issues are provided in Chapter 5.
3.1.1.13.1 Stratospheric Aerosols and Thin Cirrus Clouds

In some situations, e.g., following volcanic eruptions or when there are thin cirrus clouds present, there can be significant quantities of aerosol in the stratosphere. Gordon and Castaño [1988] showed that the presence of the El Chichón aerosol [King, Harshvardhan and Arking, 1984] had little effect on CZCS atmospheric correction; however, at the higher correction accuracy required for MODIS the Gordon and Wang [1994a] algorithm may be degraded by the presence of stratospheric aerosol. Although not listed in Table 1, MODIS is equipped with a spectral band at 1380 nm that can be used to assess the contamination of the imagery by stratospheric aerosol. This spectral band is centered on a strong water vapor absorption band and photons penetrating through the stratosphere will usually be absorbed by water vapor in the free troposphere [Gao, Goetz and Wiscombe, 1993]. Thus, any radiance measured at 1.38 μm can, in the first approximation, be assumed to be scattered by the stratospheric aerosol alone, providing a mechanism for estimating the stratospheric contribution.

The author and coworkers [Gordon et al., 1996] have assessed the effect of stratospheric aerosols on atmospheric correction and studied ways in which to correct the contamination, assuming that all radiance detected at 1380 nm results from scattering by the stratospheric aerosol alone. Briefly, the stratospheric aerosol contributes to the reflectance at all wavelengths. Thus, in its presence the total reflectance will be changed by an amount $\delta \rho_t^{(s)}$, i.e.,

$$\rho_t^{(s)}(\lambda) = \rho_t(\lambda) + \delta \rho_t^{(s)}(\lambda),$$

where $\rho_t^{(s)}$ is the reflectance of the entire ocean-atmosphere system in the presence of stratospheric aerosol, and $\rho_t$ the reflectance in its absence. To assess the impact of the stratospheric aerosol, the multiple-scattering algorithm was operated using simulated values of $\rho_t^{(s)}(\lambda)$ in the place of $\rho_t(\lambda)$, for four stratospheric aerosol types. The results suggest that stratospheric aerosol/cirrus cloud contamination does not seriously degrade the Gordon and Wang [1994a] algorithm except for large ($\sim 60^\circ$) solar zenith angles and large ($\sim 45^\circ$) viewing angles, for which multiple scattering effects can be expected to be particularly severe.

The performance of a hierarchy of algorithms for using the 1380 nm MODIS band to correct for stratospheric aerosol/cirrus clouds, was also examined. The approach was to use $\rho_t^{(s)}(1380)$
to estimate $\delta \rho_t^{(s)}(\lambda)$ in the visible and NIR. The procedures investigated ranged from simply subtracting the reflectance at 1380 nm from that in the visible bands, i.e., $\delta \rho_t^{(s)}(\lambda) = \rho_t^{(s)}(1380)$, to assuming all of the optical properties of the stratospheric aerosol are known (the reflectance measurement at 1380 nm providing the concentration) and carrying out multiple scattering computations to estimate $\delta \rho_t^{(s)}(\lambda)$. It is not surprising that the most complex procedures yield the best results; however, it was surprising that the complex procedures appear to only reduce the error in the retrieved water-leaving radiance by $\lesssim$ a factor of two compared to the simplest procedures.

In the case of thin cirrus clouds, Gordon et al. [1996] investigated an empirical correction approach in which a detailed model of the cloud optical properties was not required. This correction proved to be satisfactory for cloud optical thicknesses as large as 0.5 with only a coarse estimate of the cloud scattering phase function; however, the correction requires some knowledge regarding the aerosol in the marine boundary layer and, therefore, requires two passes through the aerosol correction algorithm.

The 1.38 $\mu$m band has not yet been used to screen or correct for thin cirrus, due to its initial poor performance on the Terra platform. Performance on Aqua appears to be much better and these ideas could be implemented in Aqua processing.

### 3.1.13.2 Appropriateness of aerosol models

Operation of the multiple-scattering algorithm requires a set of candidate aerosol models. Thus far, models from, or derived from, the work of Shettle and Fenn [1979] have been used as candidates. These models were basically developed from the analysis of aerosol physical-chemical properties and are believed to provide realistic approximations to the extinction and absorption cross section of real aerosols. However, they have never been validated for the role they are being used for here, i.e., for their ability to provide realistic aerosol phase functions and their spectral variation. It is important to utilize as candidates, aerosol models that closely approximate the optical properties of actual aerosols over the ocean, and studies of the optical properties of aerosols over the ocean have been carried out and are on going.

Measurements over and above aerosol optical thickness and its spectral variation are required
to understand the adequacy of candidate aerosol models. Schwindling [1995] compared estimates of the aerosol scattering phase function obtained from a pier at Scripps Institution of Oceanography, La Jolla, CA, with the properties of the Shettle and Fenn [1979] models and concluded that within the accuracy of their measurements the models fit both the phase function and the spectral variation of the aerosol optical thickness. It was also confirmed that $\tau_a(\lambda)$ becomes very low off the coast of California. However, as there was a need to carry out such measurements in different regions and at different times, the AERONET aerosol monitoring network [Holben et al., 1998] based on CIMEL sun/sky radiometers was expanded to include stations at the coast and on small islands.

Smirnov et al. [2003] have analyzed the CIMEL data acquired on the islands of Bermuda (Atlantic Ocean), Lanai, Hawaii (Pacific Ocean), and Kaashidhoo, Maldives (Indian Ocean). The results of their analysis are the size distributions from which aerosol scattering phase functions and other optical properties are derived. Since the basic measurement is optical (sky radiance and sun photometry), the retrieved columnar optical properties should be reasonably accurate. The size distribution components representing average conditions, when the optical depth is low ($\tau_a(500) < 0.15$), are compared with those of Shettle and Fenn [1979] (for dry particles) in Figure 28. In the figure, the individual components have been normalized to their maximum values. In

![Figure 28](image-url)

**Figure 28.** Comparison of size distribution modes (fine and course) and scattering phase functions (865 nm) derived from CIMEL measurements at remote island stations, with a selection from Shettle and Fenn [1979] (“SF”) used in MODIS processing.
reality, the total volume of the fine mode (smaller size) is approximately 20% of the total; however, in a maritime atmosphere influenced by anthropogenic activities, the relative contribution of the fine component increases. It is seen that the individual mode distributions are similar; however, as the relative humidity increases, the median size of the Shettle and Fenn [1979] coarse mode (the Oceanic) shifts to larger particle sizes. (Note, the Smirnov et al. [2003] are for the ambient relative humidity.) Figure 28 also compares the scattering phase functions (at 865 nm) used in MODIS processing with the mean for a maritime atmosphere from Smirnov et al. [2003]. The mean Smirnov et al. [2003] falling approximately midway between the Shettle and Fenn [1979] M50 and M80. This suggests that the optical properties predicted by the Shettle and Fenn [1979] maritime models should be reasonably representative of an unpolluted marine aerosol.

The agreement between the size distributions and scattering phase functions of Smirnov et al. [2003] and Shettle and Fenn [1979] for a marine atmosphere does not suggest that the Shettle and Fenn [1979] models are appropriate for all situations. Rather, it suggests that the models that are employed in the SeaWiFS and MODIS processing are appropriate for most of the open ocean. Indeed, there are special situations, e.g., marine environments influenced by anthropogenic pollution or mineral dust transported by the winds. Remer and Kaufman [1998] analyzed CIMEL measurements made in the mid-Atlantic region of the U.S. in the summer of 1993, and found that there was a strong correlation between the size distribution and the optical thickness. For low optical depth, their retrieved size distribution is similar to Smirnov et al. [2003]; however as the optical depth increases beyond 0.2 (at 670 nm) they found that an additional fine mode was required with modal diameter about twice that of the original fine mode. The contribution of this second fine mode increased as the optical thickness increased, as did the course mode. Thus, the size distribution is dynamically related to $\tau_o$.

In the case of windblown dust, the absorption properties are of special interest because the dust is colored (saharan dust is a pale shade of red). Thus, the refractive index is a strong function of wavelength. Appropriate models for atmospheric correction in the presence of Saharan dust are provided in Section 5.1.1.

Pragmatically, the appropriateness of the aerosol models is determined by the success of atmospheric correction. This can be assessed using SeaWiFS imagery because it is more mature
than MODIS, i.e., there are more comparison data available. It has been clearly demonstrated that the Gordon and Wang algorithm, using the Shettle and Fenn aerosol models, works well with SeaWiFS data [Hooker and McClain, 2000]. In addition, although unnecessary for atmospheric correction, Wang, Bailey and McClain [2000] and Wang et al. [2000] have shown that the SeaWiFS algorithm also provides reasonably good estimates of the aerosol optical depth at 865 nm. To first order, the error in optical depth estimates in the NIR is directly proportional to the error in the product of the aerosol phase function and the single scattering albedo [Wang and Gordon, 1994a] Thus, application of the present scheme, including the Shettle and Fenn models, has been shown to provide an acceptable atmospheric correction and even reasonably good optical depth retrievals in most situations. This implies that the presently used models are realistic enough for the task of atmospheric correction of most ocean color imagery produced by the present-generation color sensors. However, it was noticed that with SeaWiFS, the measured $\varepsilon(765, 865)$ was often below the lowest

\[
\frac{r_b(765)}{r_b(865)} = (865/765)^{AE}
\]

Figure 29. Candidate aerosol models used in the MODIS and SeaWiFS atmospheric correction as a function of their Angstrom exponent (AE). The SeaWiFS model numbers are preceded by “S,” i.e., the MODIS model number 1, O99, is the SeaWiFS model number 2, etc.
value for the M, C, and T models. This suggested models with fewer small particles was required. Thus, we (and the SeaWiFS Project) added the “Oceanic” (“O”) models of Shettle and Fenn [1979] to the candidate list, expanding the number of candidates from 12 to 16 (for MODIS). Figure 29 provides the MODIS and SeaWiFS aerosol models (by number) that are being used for routine processing at the present time.

3.1.1.13.3 Strongly Absorbing Aerosols

In Section 3.1.1.4 it was shown that in the presence of strongly absorbing aerosols, the candidate aerosol models must be restricted to those with values of $\omega_n$ similar to the true aerosol. This was effected there by limiting the candidate models to U50, U70, U90, and U99 when the test aerosol was U80 (Figure 13), since when the initial twelve candidate models were used, the error was excessive (Figure 12). Without a method of determining the absorption characteristics of the aerosols from satellite measurements, an aerosol climatology is required to be able to provide realistic candidate models. Furthermore, in Section 3.1.1.12.1 it was shown that, for strongly absorbing aerosols, even given the appropriate set of candidate models, knowledge of the vertical distribution of the aerosol was required for an adequate correction (Figure 24). Thus, the aerosol climatology needs to contain information concerning the aerosol-layer thickness for regions with strongly absorbing aerosols.

The effort toward building a climatology for absorbing aerosols involves measurements of the type discussed in Section 3.1.1.13.2, i.e., measurements of sky radianc and aerosol optical thickness from ships or small islands in the appropriate regions as are being carried out by AERONET [Holben et al., 1998]. A climatology for the aerosol vertical distribution can be built most effectively using LIDAR measurements [Sasano and Browell, 1989]. An excellent start toward a vertical distribution climatology can be made utilizing data from the Lidar In-Space Technology Experiment (LITE) [McCormick, 1995]. On the basis of LITE-based and aircraft-based measurements Grant et al. [1995] observed that the Saharan dust layer over the Eastern Caribbean extended in altitude from 1-4 km. This is in contrast to the dust-free atmosphere in which the thickness of the aerosol layer is typically 1-2 km. Examining a LITE pass from Wallops Island, Virginia to Bermuda, Ismail et al. [1995] found that the plume of pollution from the U.S. East Coast was in a 1-2 km thick layer above the 0.5-1.0 km thick maritime boundary layer. These observations suggest that the principal absorbing aerosols expected in the Atlantic are mixed higher in the atmosphere than
assumed in the existing candidate aerosol model lookup tables. We have been using a micro pulse lidar [Spinhirne, 1993] to study the vertical distribution of aerosol in conjunction with large-scale aerosol experiments, e.g., ACE-2, INDOEX, ACE-Asia, etc. [Voss et al., 2001; Welton et al., 2000; Welton et al., 2002].

It must be pointed out that, with the exception of TOMS [Herman et al., 1997], there is no spaceborne way of discriminating between weakly- and strongly-absorbing aerosols (however, see Chapter 5). Clearly, it would be extremely useful to be able to detect the presence of absorbing aerosols from measurements made by the ocean color sensor alone, e.g., to be able to distinguish between absorbing and nonabsorbing aerosols. Gordon [1997] proposed a method for using \( \rho_l(\lambda) \) for \( \lambda > 865 \text{ nm} \) for detecting mineral dust based on the variation of its optical properties in the short-wave infrared (SWIR). Because the performance of the MODIS SWIR bands may not be as good as expected, this approach has not been pursued.

Finally, the fact that TOMS is capable of detecting the presence of strongly-absorbing aerosols [Herman et al., 1997] provides an exciting possibility of using such data to aid in atmospheric correction. We note, however, that using this data on an operational basis would introduce a delay in the processing of MODIS data. Two alternatives to using TOMS data are provided in Chapter 5.

### 3.1.1.13.4 In-Water Radiance Distribution

Algorithms for retrieving total pigments, chlorophyll, etc., from ocean color imagery are developed by relating the nadir-viewing water-leaving radiance to the quantity in question. In the analysis of ocean color imagery it has always been assumed that \( [\rho_w]_N \) is independent of the viewing angle. This assumption was based on a small number of observations, e.g., see Smith [1974] and references therein, which suggests that \( L_w(z, \theta, \phi) \), the upwelling radiance at depth \( z \) beneath the surface and traveling in a direction specified by the angles \( (\theta, \phi) \), is only weakly dependent on \( \theta \) and \( \phi \). However, in a series of papers Morel and Gentili [Morel and Gentili, 1991; Morel and Gentili, 1993; Morel and Gentili, 1996] studied theoretically the bidirectional effects as a function of the sun-viewing geometry and the pigment concentration. Their simulations suggest that, although the bidirectional effects nearly cancel in the estimation of the pigment concentration using radiance
ratios (Eq. (4)), \( L_u(z, \theta, \phi) \) can depend significantly on \( \theta, \phi \) and \( \theta_0 \). This means that the value of \( [\rho_w]_N \) retrieved in atmospheric correction is actually appropriate only to the viewing direction in which the measurement of \( \rho_i \) is made. Since most in-water algorithms have been developed based on nadir-viewing measurements, the derived \( [\rho_w]_N \) values should be corrected to nadir-viewing geometry. This requires understanding the bidirectional effects, i.e., validating the Morel and Gentili [1996] model or developing a new model. This is being effected by direct determination of the upwelling radiance distribution for a variety of waters and solar zenith angles using an electro-optics radiance camera system developed by Voss [1989], e.g., see Morel, Voss and Gentili [1995]. These measurements provide direct determination of the effect, and will yield an algorithm for extrapolation to the nadir viewing direction as required for derived product algorithms.

It is useful to review the bidirectional nature of the water-leaving radiance in some detail. Although we have used reflectance rather than radiance to develop and explain the algorithm, here we revert to radiance, noting that the normalized water-leaving reflectances and radiance are related through

\[
[\rho_w]_N = \frac{\pi}{F_0} [L_w]_N.
\]

Following Morel, Antoine and Gentili [2002], the normalized water-leaving radiance seen by MODIS based on the retrieval of \( L_w(\theta_v, \phi_v) \) is given by

\[
[L_w(\theta_v, \phi_v; \theta_0)]_N = \left[ \frac{T_f(\theta_0)T_f(\theta'_v)}{m^2(1 - rR(\theta_0))} \right] \frac{R(\theta_0)}{Q(\theta'_v, \phi_v; \theta_0)},
\]

(27)

where \( \theta_0 \) is the solar zenith angle, \( \theta_v \) and \( \phi_v \) are the viewing angles (\( \phi_v \) measured relative to the sun), \( R(\theta_0) \) is the subsurface irradiance reflectance for a solar zenith angle \( \theta_0 \), and \( Q(\theta'_v, \phi_v; \theta_0) \) is the so-called “Q-factor” defined as the upwelling irradiance just beneath the water surface \( E_u \) divided by the upwelling radiance just beneath the surface in the viewing direction \( L_u(\theta'_v, \phi_v; \theta_0) \). The angles \( \theta'_v \) and \( \theta_v \) are related by Snell’s law: \( m \sin \theta'_v = \sin \theta_v \), where \( m \) is the refractive index of sea water. \( T_f(\theta_0) \) is the transmittance (above the sea surface \( \rightarrow \) below the sea surface) for downwelling irradiance from the sun and sky, and \( T_f(\theta'_v) \) is the transmittance of \( L_u(\theta'_v, \phi_v; \theta_0) \) across the air-sea interface, i.e.,

\[
L_w(\theta_v, \phi_v; \theta_0) = \frac{T_f(\theta'_v)}{m^2} L_u(\theta'_v, \phi_v; \theta_0).
\]
Note that in this section we depart from our usual notation for the water-leaving radiance, i.e., \( L_w(\theta_v, \phi_v) \), and specifically introduce the solar zenith angle \( \theta_0 \) in the argument list. This is to provide the reader with a reminder of the position of the sun in each definition below.

The term in the brackets in Eq. (27) is denoted \( \Re(\theta_v, \theta_0) \) by Morel and Gentili, i.e.,

\[
\Re(\theta'_v, \theta_0) = F_0 \frac{T_f(\theta_0)T_f(\theta'_v)}{m^2(1 - rR(\theta_0))}.
\]

With the exception of \( R(\theta_0) \) in the denominator, this term depends solely on the air-sea interface, i.e., the actual roughness of the wind roughened sea surface (and therefore the wind speed and direction), the sun angle, and the viewing direction. The term \( r \) accounts for the contribution of internal reflections reflections within the medium. When the upward radiance is totally diffuse, \( r \approx 0.48 \) and almost independent of surface roughness [Austin, 1974], so since \( R \) is usually < 0.1, the contribution of this term is small; however it does depend on the angular distribution of the upwelling radiance distribution.

There are three important normalized water-leaving radiances that can be defined. The first is that of Gordon and Clark [1981], the radiance that exits the water traveling toward the zenith when the sun is at the zenith and there is no atmosphere:

\[
[L_w]^\text{Exact}_N \equiv [L_w(0, 0; 0)]_N = F_0 \Re(0, 0) \frac{R(0)}{Q(0, 0; 0)}. \tag{28}
\]

The second is the normalized water-leaving radiance that is usually measured at sea, i.e., the radiance propagating toward the zenith, but with the sun not necessarily at the zenith:

\[
[L_w]^\text{Field}_N \equiv [L_w(0, 0; \theta_0)]_N = F_0 \Re(0, \theta_0) \frac{R(\theta_0)}{Q(0, 0; \theta_0)}. \tag{29}
\]

Finally, the third is the normalized water-leaving radiance deduced from the measurement of \( L_w(\theta_v, \phi_v) \) by a space-borne sensor:

\[
[L_w]^\text{Space}_N \equiv [L_w(\theta_v, \phi_v; \theta_0)]_N = F_0 \Re(\theta'_v, \theta_0) \frac{R(\theta_0)}{Q(\theta'_v, \phi_v; \theta_0)}. \tag{30}
\]

It is reasonable to refer all \( [L_w]_N \) measurements, either from the surface or from space, to the same geometry. This is conventionally taken to be \( [L_w]^\text{Exact}_N \). Thus,

\[
[L_w]^\text{Exact}_N = \frac{\Re(0, \theta_0)}{\Re(0, 0)} \frac{Q(0, 0; 0)}{Q(0, \theta_0)} \frac{R(\theta_0)}{R(0)} [L_w]^\text{Field}_N \tag{31}
\]
and

\[
[L_w]^\text{Exact}_N = \frac{R(\theta'_v, \theta_0)}{R(0, 0)} \frac{Q(0, \bullet, 0)}{Q(\theta'_v, \phi_v, \theta_0)} R(\theta_0) [L_w]^\text{Space}_N \].
\]  

(32)

We note that deriving \([L_w]^\text{Exact}_N\) requires detailed modeling of \(Q\) as a function of sun-viewing geometry, \(R\) as a function of the solar zenith angle, and \(\Re\) as a function of surface roughness (wind speed). \([L_w]^\text{Exact}_N\) is the radiance that is planned for the TERRA/MODIS Level 2 product after validation; however, for vicarious calibration and/or validation purposes, one wants to compare simultaneous measurements of \([L_w]^\text{Field}_N\) and \([L_w]^\text{Space}_N\). These quantities are related through

\[
\frac{[L_w]^\text{Field}_N}{[L_w]^\text{Space}_N} = \frac{R(0, 0)}{R(\theta'_v, \theta_0)} \frac{Q(\theta'_v, \phi_v, \theta_0)}{Q(0, \bullet, \theta_0)} = \frac{T_f(0)}{T_f(\theta'_v)} \frac{Q(\theta'_v, \phi_v, \theta_0)}{Q(0, \bullet, \theta_0)},
\]

(33)

with no dependence\(^5\) on \(R\). This is the normalization that has been reported in the TERRA/MODIS Level 2 product, i.e., \([L_w]^\text{Space}_N\) has been converted to \([L_w]^\text{Field}_N\) using (33). This conversion is effected using a revised Morel-Gentili model [Morel, Antoine and Gentili, 2002].

### 3.1.1.13.5 Diffuse transmittance

As described in Section 3.1.1.5, the present MODIS algorithm replaces the actual diffuse transmittance \(t(\theta_v, \phi_v)\), computed using the actual upwelling radiance distribution just beneath the sea surface, \(L_u(\theta'_v, \phi'_v)\), with the diffuse transmittance \(t^*(\theta_v, \phi_v)\), computed for a uniform \(L_u\), i.e., an \(L_u\) independent of viewing direction. This introduces error into the retrieval of \(\rho_w\). To find the effect of \(L_u(\theta'_v, \phi'_v)\) on the true diffuse transmittance consider the following problem. Let \(F_0\) be the extraterrestrial solar irradiance, \(\hat{\xi}_0\) a unit vector in the direction of propagation of the solar beam, and \(L_R(\hat{\xi})\) the resulting radiance propagating downward just beneath the sea surface in the direction \(\hat{\xi}\). Then, Yang and Gordon [1997] show that

\[
t(-\hat{\xi}_0) = \frac{1}{F_0|\hat{\xi}_0|} \int_{\Omega_d} |\hat{\xi} \cdot \hat{n}| L_R(\hat{\xi}) \frac{L_u(-\hat{\xi})}{L_u(-\hat{\xi}_0)} d\Omega(\hat{\xi}),
\]

(34)

where \(L_u(-\hat{\xi})\) is the upward radiance distribution incident just beneath the sea surface for which we want \(t\), \(\hat{\xi}_0\) and \(\hat{\xi}_0\) are related by Snell’s law, and \(\Omega_d\) indicates the integral is to be evaluated over all downward \(\hat{\xi}\). Note that when \(L_u\) is taken to be totally diffuse (independent of \(\hat{\xi}\)), the result reduces to the formula for \(t^*\) in Section 3.1.1.5.

\(^5\) This ignores the weak dependence of \(r\) on \(Q\).
The error in the retrieved $\rho_w$ induced by using $t^*$ in place of $t$ is just

$$\frac{\Delta \rho_w(-\xi_0)}{\rho_w(-\xi_0)} = \frac{t(-\xi_0) - t^*(-\xi_0)}{t^*(-\xi_0)}. \quad (35)$$

Yang and Gordon [1997] have examined the magnitude of the error for measured radiance distributions $L_u(-\hat{\chi})$ [Voss, 1989] and various aerosol concentrations. They conclude that the error induced in using $t^*$ in place of $t$ can be as large as $\pm 4\%$, and is largest in the blue. Thus, derivation of $\rho_w(443)$ within $\pm 5\%$ will require knowing, or estimating, the shape of the subsurface radiance distribution. It is important to understand that this error represents the natural limit in the accuracy of atmospheric correction when $t^*$ is employed rather than $t$. Morel and Gentili [1996] have devised an iterative scheme for estimating the shape of the subsurface radiance distribution from an estimate of the pigment concentration. Such a scheme (or some alternative that requires multiple passes through the atmospheric correction algorithm) will be required to provide a more realistic value for $t$; however, this cannot be effected until the Morel and Gentili model is completely validated using the measurement program described in Section 3.1.1.13.4.

### 3.1.2 Mathematical Description of the Algorithm

The multiple-scattering algorithm was initially implemented as described in Section 3.1.1.3, i.e., lookup tables (LUTs) providing $K[\lambda, \rho_{as}(\lambda)]$, in the form of $a(\lambda)$, $b(\lambda)$, and $c(\lambda)$ in Eq. (14), for all required viewing geometries, solar zenith angles, wavelengths, aerosol models, and aerosol concentrations, were used to provide the $\rho_t - \rho_r - t\rho_w$ versus $\rho_{as}$ relationship. These tables were derived by solving the RTE for each aerosol model and geometry using a two-layer representation of the vertical structure of the atmosphere — aerosols in the lower layer and Rayleigh scattering in the upper layer. Late in the implementation it was found that for strongly absorbing aerosols, e.g., the Urban models, and large $\theta_0$, it was possible that $\rho_t - \rho_r - t\rho_w < 0$, making it impossible to use Eq. (14) because of the logarithms. To avoid this, we reformulated the LUTs by replacing Eq. (14) with

$$\rho_t(\lambda) - \rho_r(\lambda) - t\rho_w(\lambda) = a(\lambda)\rho_{as} + b(\lambda)\rho_{as}^2 + c(\lambda)\rho_{as}^3 + d(\lambda)\rho_{as}^4,$$

where, as before, for each $\theta_v, \phi_v, \theta_0, \phi_0$, the coefficients $a, b, c, d$ were obtained from the simulations by least-squares. As in the case of Eq. (14), for the azimuth difference $\phi_v - \phi_0$, we
expanded $a(\lambda), b(\lambda), c(\lambda)$ and $d(\lambda)$ in a Fourier series and stored only the Fourier coefficients. As the reflectances are even functions of the azimuth difference $\phi_v - \phi_0$, $a(\lambda), b(\lambda), c(\lambda)$ and $d(\lambda)$ will be even functions of $\phi_v - \phi_0$. Thus, we can write

$$a(\theta_v, \phi_v, \theta_0, \phi_0) = a^{(0)}(\theta_v, \theta_0, \lambda) + 2 \sum_{m=1}^{M} a^{(m)}(\theta_v, \theta_0, \lambda) \cos m(\phi_v - \phi_0),$$

with

$$a^{(m)}(\theta_v, \theta_0, \lambda) = \frac{1}{\pi} \int_{0}^{\pi} a(\theta_v, \theta_0, \lambda, \phi_v) \cos m(\phi_v - \phi_0) \, d\phi_v,$$

etc. The LUTs contain these coefficients for $m = 0$ to $M$ with $M = 14$. This modification produces virtually no change in the retrieved $[\rho_{\text{w}}]_N$ for the cases tested earlier.$^6$

We now describe the algorithm steps in detail with the aid of the annotated flow diagram in Figure 30. All quantities in this diagram are assumed to have been weighted with respect to the MODIS spectral response functions (where required) as described in Section 3.1.1.12.5 and Gordon [1995], e.g., $F_0$ stands for $\langle F_0(\lambda) \rangle_{S_i}$, $L_m$ for $\langle L_m(\lambda) \rangle_{S_i}$, $\rho_r$ for $\langle \rho_r(\lambda) \rangle_{F_0S_i}$, etc., where $S_i$ is the spectral response of the $i^{th}$ MODIS spectral band.

We assume that MODIS measures the radiance $L_m$, and that this is converted to reflectance $\rho_m$ using $F_0$. Alternatively, MODIS may be calibrated to measure $\rho_m$ directly, in which case this step is omitted. The Ozone concentration is used to compute $\langle \tau_{\text{O}_3}(\lambda) \rangle_{F_0S_i}$ in order to remove the effect of Ozone absorption by multiplying $\rho_m$ by

$$\exp[(\tau_{\text{O}_3}(\lambda))_{F_0S_i} M],$$

where $M$ is the two-way air mass

$$M = \frac{1}{\cos \theta_v} + \frac{1}{\cos \theta_0}.$$ 

The wind speed $W$ is then used to estimate the whitecap reflectance, $[\rho_{\text{w}}]_N$ using Eq. (20), and the whitecap contribution

$$t^*(\theta_0) t^*(\theta_v) [\rho_{\text{w}}]_N,$$

where $t^*(\theta_0)$ is provided in Eq. (3), is subtracted from the Ozone-corrected $\rho_m$. The parameters $T_w$ and $\Delta T$ are not used in the present implementation, but are available should a more sophisticated

---

$^6$ The procedure described in footnote 2 was also employed here.
whitecap removal algorithm require them. The wind speed also provides the sun glitter mask as described in Section 3.1.1.7. These procedures return the quantity

$$\rho_t = \rho_r + \rho_a + \rho_{ra} + t \rho_w$$

at unmasked pixels.

The next step in the algorithm is the computation of $\rho_r$. This requires the atmospheric pressure to provide the Rayleigh optical depth, the wind speed to provide an estimate of the surface roughness, and the viewing-sun geometry. For a given solar zenith angle $\theta_0$ and azimuth angle $\phi_0$, the Stokes vector $I_r$ for the Rayleigh scattering contribution to the radiance leaving the TOA can be written

$$I_r = \begin{pmatrix} I_r(\theta_v, \phi_v, \theta_0, \phi_0) \\ Q_r(\theta_v, \phi_v, \theta_0, \phi_0) \\ U_r(\theta_v, \phi_v, \theta_0, \phi_0) \\ V_r(\theta_v, \phi_v, \theta_0, \phi_0) \end{pmatrix} = \begin{pmatrix} I_r^{(0)}(\theta_v, \theta_0) + 2 \sum_{m=1}^{2} I_r^{(m)}(\theta_v, \theta_0) \cos m(\phi_v - \phi_0) \\ Q_r^{(0)}(\theta_v, \theta_0) + 2 \sum_{m=1}^{2} Q_r^{(m)}(\theta_v, \theta_0) \cos m(\phi_v - \phi_0) \\ 2 \sum_{m=1}^{2} U_r^{(m)}(\theta_v, \theta_0) \sin m(\phi_v - \phi_0) \\ 2 \sum_{m=1}^{2} V_r^{(m)}(\theta_v, \theta_0) \sin m(\phi_v - \phi_0) \end{pmatrix}.$$  \hspace{1cm} (36)

The Rayleigh contribution to the reflectance is $\rho_r = \pi I_r(\theta_v, \phi_v, \theta_0, \phi_0)/F_0 \cos \theta_0$. The quantities $Q_r(\theta_v, \phi_v, \theta_0, \phi_0)$ and $U_r(\theta_v, \phi_v, \theta_0, \phi_0)$ are used to correct the total radiance for the polarization sensitivity of the sensor following Gordon, Du and Zhang [1997a] in Section 3.1.1.8. The degree, $P_r$, and the direction, $\chi_r$, of polarization of $\rho_r$ used in Section 3.1.1.8 are

$$P_r = \sqrt{\frac{Q_r^2 + U_r^2}{I_r}} \quad \text{and} \quad \tan 2\chi_r = \frac{U_r}{Q_r}$$

LUTs consisting of $I_r^m$, $Q_r^m$, and $U_r^m$ are provided for $\theta_0 = 0(2^\circ)88^\circ$ for 100 values of $\theta_v$. $V_r^{(m)}$ is identically zero. Bilinear interpolation is used to determine the values specific to the particular viewing geometry.

The $\rho_r$-LUTs have been prepared for standard atmospheric pressure, the value of $\rho_r$ is corrected to the actual pressure by multiplying the interpolated value by [Gordon, Brown and Evans, 1988]

$$1 - \exp[-(P/P_0)\langle \tau_v(\lambda) \rangle_{F_0,S_i}/\cos \theta_v]$$

$$1 - \exp[-\langle \tau_v(\lambda) \rangle_{F_0,S_i}/\cos \theta_v],$$

where $\langle \tau_v(\lambda) \rangle_{F_0,S_i}$ is the band-averaged Rayleigh optical depth for band $i$ at a pressure $P_0$ and $P$ is
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Figure 30. Annotated flow diagram of the algorithm.

Measured Radiance

Measured Reflectance

Remove Whitecaps, Ozone, and Mask for Sun Glint

Compute Rayleigh

Remove Rayleigh

Remove Multiple Scattering Effects in the NIR

Determine $\varepsilon(\lambda_S, \lambda_I)$

Extrapolate to Desired Wavelength

Aerosol Contribution at Desired Wavelength

Remove Diffuse Transmittance ($t^*$)
the actual atmospheric pressure. In the present implementation LUTs are constructed for five wind speeds, and \( \rho_r \) is interpolated to the wind provided in the ancillary data.

After \( \rho_r \) has been determined, it is subtracted from \( \rho_t \) to form

\[
\rho_t - \rho_r = \rho_a + \rho_{ra} + t \rho_w.
\]

The fact that \( \rho_w \) is essentially zero in the NIR, i.e., at \( \lambda_s \) and \( \lambda_l \), then enables the determination of

\[
\rho_a(\lambda_s) + \rho_{ra}(\lambda_s) \quad \text{and} \quad \rho_a(\lambda_l) + \rho_{ra}(\lambda_l).
\]

These quantities are used in a manner described in Section 3.1.1.3 to estimate \( \varepsilon(\lambda_s, \lambda_l) \), and then to find the two aerosol models from among the \( N \) candidates that bracket the observed \( \varepsilon(\lambda_s, \lambda_l) \). In the process, the \( \rho_a + \rho_{ra} \) LUTs are used to convert multiple scattering quantities \( (\rho_a + \rho_{ra}) \) to single scattering quantities \( (\rho_{as}) \). Interpolating between these two models enables estimation of \( \rho_{as}(\lambda) \) for \( \lambda < \lambda_s \), and a second application of the \( \rho_a + \rho_{ra} \) LUTs provides \( \rho_a + \rho_{ra} \) in the visible. This procedure yields \( t(\lambda)\rho_w(\lambda) \) in the visible.

To derive the water-leaving reflectance \( \rho_w \), the diffuse transmittance \( t \) is required. A third set of LUTs provide \( t^*(\theta_0, \lambda) \) for each \( \lambda \) and each aerosol model as a function of the aerosol optical thickness \( \tau_a(\lambda) \). Once \( \rho_{as}(\lambda) \) is determined for each aerosol model it is a simple matter to determine \( \tau_a(\lambda) \) for that model using Eq. (9). The \( t^* \)-LUTs provide the diffuse transmittance for a given aerosol model in the form

\[
t^*(\theta_0, \lambda) = A(\theta_0, \lambda) \exp[-B(\theta_0, \lambda)\tau_a(\lambda)],
\]

where \( A \) and \( B \) are determined from radiative transfer simulations. (It should be noted that in this implementation of the algorithm the bi-directional reflectance distribution function of the upwelling radiance just beneath the surface is assumed to be lambertian, i.e., we are using \( t^* \) instead of \( t \).) \( t^* \) is then interpolated between the two models in a manner similar to \( \rho_a + \rho_{ra} \). Finally, estimation of \( t^*(\theta_v, \lambda) \) provides \( \rho_w(\lambda) = t \rho_w / t^*(\theta_v, \lambda) \).

This completes the retrieval of \( \rho_w \) in the visible. The final products are either the normalized water-leaving reflectances or radiances:

\[
[\rho_a(\lambda)]_N = \rho_w(\lambda) / t^*(\theta_0, \lambda) \quad \text{or} \quad [L_w(\lambda)]_N = \frac{\mathcal{F}_0(\lambda)[\rho_w(\lambda)]_N}{\pi}.
\]
The latter was referred to as $[L_w]^\text{Space}_N$ in Section 3.1.1.13.4. Note that when the spectral response of the sensor is explicitly displayed, the final products are $\langle [\rho_i(\lambda)]_N \rangle F_0 S_i$ and $\langle [L_w(\lambda)]_N \rangle S_i$. These are related by [Gordon, 1995]

$$\langle [L_w(\lambda)]_N \rangle S_i = \frac{\langle [\rho_i(\lambda)]_N \rangle F_0 S_i (F_0(\lambda)) S_i}{\pi}.$$

The $\rho_i$ retrieval procedure described above requires the use of three different LUTs: (1) tables of the Stokes’ vector of the Rayleigh component of the TOA reflectance (Rayleigh-LUTs); (2) tables to provide the relationship between $\rho_a + \rho_{ra}$ and $\rho_{as}$ for the individual aerosol models, and (3) tables of $A$ and $B$ relating the diffuse transmittance of the atmosphere to the aerosol optical thickness for each aerosol model. The Rayleigh-LUTs (item 1) are separate from those in items 2 and 3. The LUTs for items 2 and 3 are combined (Aerosol-LUTs), with a single LUT for each aerosol model used. The Aerosol-LUTs also contain the aerosol phase functions specific to the given aerosol model (these are used to compute the value of $\varepsilon(\lambda, \lambda_l)$ in the algorithm). The Rayleigh-LUTs are small. In contrast, the Aerosol-LUTS are large: approximately 10 MB per aerosol model for a maximum viewing angle of $\sim 60^\circ$ and a maximum solar zenith angle of $80^\circ$. As the algorithm is presently implemented, there is no limit to the number ($N$) of aerosol models that can be used although it is assumed that $N$ is an even number.

Finally, LUTs are required to provide the quantities to convert $[L_w]^\text{Space}_N$ to $[L_w]^\text{Field}_N$ (and later to $[L_w]^\text{Exact}_N$). These have been provided by André Morel based on Morel, Antoine and Gentili [2002].

There are two approximations to these procedures that are used to make the processing faster. First, the $a$, $b$, $c$, and $d$ coefficients are evaluated only once for each $5 \times 5$-pixel box in the image. This was based on tests in which $\rho_a + \rho_{ra}$ for a given $\rho_{as}$ was computed using the $a$, $b$, $c$, and $d$ coefficients for the true values of $\theta_v$, $\theta_0$ and $\phi_v - \phi_0$ and compared with those offset by a given number of pixels. Second, the procedure described for the computation of $\varepsilon(\lambda_s, \lambda_l)$ is applied at only every fifth pixel. After evaluation at a pixel as described in this section, the indices of the final two bounding models are retained and used at the next pixel to compute

$$\varepsilon(\lambda_s, \lambda_l) = \frac{\varepsilon_{\text{low model}}(\lambda_s, \lambda_l) + \varepsilon_{\text{high model}}(\lambda_s, \lambda_l)}{2},$$
where \( \varepsilon_{\text{low model}}(\lambda_s, \lambda_l) \) is the value of \( \varepsilon(\lambda_s, \lambda_l) \) computed using the aerosol model that gave the lower bounding value of \( \varepsilon \) at a previous pixel, etc. If \( \varepsilon(\lambda_s, \lambda_l) \) still falls between the \( \varepsilon \) for the original bounding models, these models are used for the present pixel. Thus, the full \( \varepsilon \)-determination procedure is only used at every fifth pixel. The basis for this modification is that the physical-chemical properties of the aerosol are not expected to change significantly over the spatial scales of a few pixels.

### 3.1.3 Uncertainty Estimates

There are four major sources of error in the algorithm as described thus far. The first is the fact that the \( N \) candidate aerosol models chosen to describe the aerosol may be unrepresentative of the natural aerosol. The magnitude of this effect has been estimated in Section 3.1.1.4. (In particular see Figure 12.) The second is the error in the estimate of the whitecap reflectance \( \rho_{\text{wc}} \). In Section 3.1.1.6 we showed that when the whitecap reflectance depends on wavelength as suggested by Frouin, Schwindling and Deschamps [1996], the error in \( [\rho_{w}]_N \) is similar to the error in the estimate of \( [\rho_{\text{wc}}]_N \), which exceeds \( \pm 0.002 \) at 443 nm for a wind speed of \( \sim 9-10 \) m/s; however, the modeled \( [\rho_{\text{wc}}]_N \) may be too large in the visible for a given wind speed. The third is the error associated with either the misidentification of strongly-absorbing aerosols as being weakly-absorbing, or in the case of strongly-absorbing aerosols, an inaccurate estimate of their vertical extent. The magnitude of these errors was discussed in Sections 3.1.1.4 and 3.1.1.12.1. The forth is the error in the sensor’s radiometric calibration, i.e., the error in \( \rho_t(\lambda) \). In this section we will describe some simulations to estimate the magnitude of the effect of the radiometric calibration error.

Since the desired water-leaving reflectance is only a small part of \( \rho_t \), at most \( \sim 10 - 15\% \) (Table 1), accurate calibration of the sensor is critical [Gordon, 1987]. In this section we describe simulations to estimate the magnitude of the effect of the radiometric calibration error, and discuss how accurate on-orbit calibration can be effected.

To assess the effect of calibration errors, we add a small error to each of the measured reflectances, i.e.,

\[
\rho'_t(\lambda) = \rho_t(\lambda)[1 + \alpha(\lambda)],
\]  

(37)
where $\alpha(\lambda)$ is the fractional error in $\rho_t(\lambda)$ and $\rho'_t(\lambda)$ is the value of $\rho_t(\lambda)$ that the incorrect sensor calibration would indicate. The atmospheric correction algorithm is then operated by inserting $\rho'_t(\lambda)$ as the measured value rather than the true value $\rho_t(\lambda)$ and $t\Delta\rho_w \equiv \Delta\rho$ is computed as before.

Assuming the single-scattering algorithm, Eq. (12), is exact, and $\varepsilon(\lambda_i, \lambda_l) = \exp[c(\lambda_l - \lambda_i)]$, it is easy to show that to first order in $\alpha(\lambda)$, the error in the retrieved $\rho_w$ is

$$t(\lambda_i)\Delta\rho_w(\lambda_i) = \alpha(\lambda_i)\rho_t(\lambda_i) - \varepsilon(\lambda_i, \lambda_l)\alpha(\lambda_l)\rho_t(\lambda_l) - \left(\frac{\lambda_l - \lambda_i}{\lambda_l - \lambda_s}\right)\frac{\varepsilon(\lambda_l, \lambda_i)\varepsilon(\lambda_s, \lambda_l)\alpha(\lambda_s)\rho_t(\lambda_s) - \varepsilon(\lambda_i, \lambda_l)\alpha(\lambda_l)\rho_t(\lambda_l)}{\epsilon(\lambda_s, \lambda_l)}$$

(38)

The first term represents the direct effect of calibration error at $\lambda_i$ on $\rho_w(\lambda_i)$, while the remaining terms represent the indirect effect from calibration error in the atmospheric correction bands at $\lambda_s$ and $\lambda_l$. The second term obviously increases in importance as $\lambda_i$ decreases. Note that if all of the spectral bands have calibration error with the same sign, i.e., all $\alpha(\lambda)$ have the same sign, significant cancelation of the atmospheric correction contribution can occur; however, if $\alpha(\lambda_s)$ and $\alpha(\lambda_l)$ have different signs, the error is magnified as the last two terms in Eq. (38) will add.

To see if this holds for the multiple-scattering algorithm as well, it was also operated by inserting $\rho'_t(\lambda)$ as the measured value rather than the true value $\rho_t(\lambda)$. The results of this exercise are presented in Figure 31 for the M80 aerosol model at the center of the scan. In the top panels, $\alpha(765) = \alpha(865)$ with $\alpha(443) = 0$ or with $\alpha(443) = \alpha(765) = \alpha(865)$. They show the effect of a calibration bias that is the same at 765 and 865 nm. The lower panels show the effect of having calibration errors that are of opposite sign at 765 and 865 nm. Note that in this case even a small calibration error (1%) can make as significant an error in $\rho_w(443)$ as a large calibration error (5%) when the signs are all the same. As discussed above, the reason the error is so much larger when it is of opposite sign at 765 and 865 nm is that it will cause a large error in the estimated value of $\varepsilon(765, 865)$, and this will propagate through the algorithm causing a large error in the retrieved water-leaving reflectance at 443 nm. In the cases examined in Figure 31, the magnitude of the errors is in quantitative agreement with that predicted by Eq. (38).
Figure 31. Error in the retrieved $t(443)\rho_{sw}(443)$ for viewing at the center of the scan with a Maritime aerosol at RH = 80% as a function of the solar zenith angle with $\tau_0(865) = 0.2$ and calibration errors $\alpha(443)$, $\alpha(765)$, and $\alpha(865)$ in Eq. (37) (open circles). Solid circles are for $\alpha(\lambda_i) = 0$ for all $\lambda_i$. 
As the goal for the calibration of the relevant ocean color bands on MODIS is that \( L_t \) have an uncertainty of \(< \pm 5\% \), and Figure 31 (lower panels) show that such an error (even if it were the same in each band) would cause the error in the retrieved \( \rho_w(443) \) to be outside the acceptable range. A method for overcoming these calibration difficulties is discussed in Section 3.2.2.

### 3.2 Practical Considerations

The present algorithm is not capable of adequately dealing with strongly-absorbing aerosols, e.g., the Urban model. Failure of the correction algorithm for aerosols of this type needs to be addressed. This will require that a system be developed to indicate the presence of such aerosols — by unacceptable \([\rho_w]_N\)'s, unacceptable pigments, etc. — and initiate a second pass through the algorithm using a special set of candidate aerosol models with the appropriate absorption properties. This problem is the focus of Chapter 5.

#### 3.2.1 Programming and Procedural Considerations

These considerations are described in the ATBD “Processing Framework and Matchup Data Base: MODIS Algorithm” by R. Evans. The report also includes data volume, networking, and CPU requirements.

#### 3.2.2 Calibration, Initialization, and Validation

In Section 3.1.3 examples were provided to show the sensitivity of the algorithm to sensor calibration errors (Figure 31). It was demonstrated that calibration errors of the order of \( \pm 5\% \), the absolute radiometric calibration uncertainty specified for the MODIS visible bands, would lead to excessive error in \([\rho_w]_N\), even if the calibration error the errors in bands 15 and 16 were of the same sign. When errors in these bands are small (\(~ \pm 1\%\) but have opposite signs (Figure 31, lower panels), the error in the water-leaving reflectance becomes large because of the extrapolation of \( \varepsilon \) into the visible. Thus, it is clear the the calibration uncertainty of MODIS must be reduced in order to provide acceptable \([\rho_w]_N\), retrievals.
3.2.2.1 Calibration Initialization

Although the calibration requirement is difficult if not impossible to meet using standard laboratory methods, it should be possible to perform an adequate calibration in orbit using surface measurements to deduce the true water-leaving radiance and the optical properties of the aerosol. This is normally referred to as vicarious calibration [Evans and Gordon, 1994; Fraser and Kaufman, 1986; Gordon, 1987; Koepke, 1982; Slater et al., 1987]. Gordon [1998] has outlined a plan for effecting such calibration, the process of which we refer to as initialization. This calibration is not radiometric, rather, it is a calibration of the entire system — the sensor plus the algorithms. The sensor calibration is adjusted to force the algorithm to conform to surface measurements of water-leaving radiance and atmospheric (aerosol) properties. A similar procedure was carried out for CZCS [Evans and Gordon, 1994], but without any surface-based atmospheric measurements. It was only moderately successful because the calibration of that instrument varied in time, and there was no independent way of determining the temporal variation. Here, we make the assumption that any change in the sensitivity of the instrument with time can be determined by other methods, e.g., using the SRCA, the solar diffuser, or imagery of the moon.

Gordon [1998] provides the complete details of the initialization procedure along with estimates of the expected accuracy. Briefly, it is assumed that the spectral band at $\lambda_l$ has no calibration error. The effect of calibration error at $\lambda_l$ has been described by Wang and Gordon [2002]. Measurements of the aerosol properties (spectral variation in optical depth) and $L_w$ are then used to predict $L_t$ at the other wavelengths from $L_t(\lambda_l)$, and the calibration of these wavelengths is adjusted to provide the predicted $L_t$. Analysis shows that the residual calibration error at a given $\lambda$ is reduced by a factor of approximately $(\lambda/\lambda_l)^4$, i.e., approximately the ratio of the contributions of $L_r$ to $L_t$, below the radiometric calibration error at $\lambda_l$. Gordon [1998] shows that procedure alone is sufficient to reduce the error in the retrieval of $\rho_w$ from $\rho_t$, using the algorithm described in Section 3.1.1.3, to desirable limits. Reduction of the error in $L_t(\lambda_l)$, using methods described by Gordon and Zhang [1996], will further reduce the error in $\rho_w$, but only slightly [Gordon, 1998].

This procedure was applied to SeaWiFS [Gordon et al., 1998] using data acquired in January and February 1998 near Hawaii. Prior to that time, the SeaWiFS project had used MOBY [Clark et al., 1997] measurements of $[L_w(\lambda)]_N$ near Hawaii, along with the atmospheric correction algorithm
described in this ATBD, to adjust the sensor calibration, for $\lambda < \lambda_I$ and $\lambda_a$, by forcing the retrieved and measured $[L_w(\lambda)]_N$ to agree [McClain et al., 1998]. The Gordon et al. [1998] calibration results were in excellent agreement with the SeaWiFS project’s, suggesting that a MOBY time series of $[L_w(\lambda)]_N$ alone can be used to effect an adequate vicarious calibration. This underscores the importance of continuing the MOBY measurements through the lifetime of MODIS.

A significant difficulty with MODIS (Terra) is that the calibration does not appear to be stable, i.e., it undergoes random variations that must be removed in order to provide a consistent data set. This being the case, the data of highest quality are always produced by retrospective processing. Providing high-quality products has not been possible to date.

3.2.2.2 Validation

By validation of atmospheric correction, we mean quantification of the uncertainty expected to be associated with the retrieval of the water-leaving radiance from the measurement of the total radiance exiting the ocean-atmosphere system. This uncertainty includes that associated with the measurement or estimation of auxiliary data required for the retrieval process, e.g., surface wind speed, surface atmospheric pressure, and total Ozone concentration. For a definitive validation, this quantification should be carried out over the full range of atmospheric types expected to be encountered. However, funding constraints require that the individual validation campaigns must be planned to address the individual components of the atmospheric correction algorithm believed to represent the greatest potential sources of error.

The validation of the $[\rho_w]_N$ product is being effected by comparing simultaneous surface-based measurements and MODIS-derived values at locations not used in the initialization measurements. Station locations will be chosen to provide a wide range of values of $[\rho_w]_N$ and aerosol types. For ship-based validation experiments, aerosol properties ($\tau_a$, $\omega_a$, $P_a$) will be derived from measurements with sun photometers and sky radiance cameras. The specific details of the validation plan are provided in Clark et al. [1997].
3.2.3 Quality Assurance and Diagnostics

By “quality assurance” (QA) we mean providing the \( [\rho_w]_N \)-user with information concerning when the product may not conform to expectations and should be used with caution. QA procedures have been developed in conjunction with R. Evans. A detailed discussion is included in the ATBD “Processing Framework and Matchup Data Base: MODIS Algorithm” by R. Evans. Basically, if our assumptions are valid (Section 4.1), and the wind speed is \( \lesssim 10 \text{ m/s} \), the algorithm can be expected to perform properly except in situations where strongly absorbing aerosols are present (Sections 3.1.1.2 – 3.1.1.4). For these, no reliable algorithm enhancement is available in the processing code at present. Generally absorbing aerosols will result in an over correction and \( [\rho_w]_N \) will be too small; however, as \( [\rho_w]_N \) may be small for other reasons, e.g., high pigment concentration, there is generally no simple rule that can be applied to determine whether the derived values are reasonable; however, the authors along with R. Evans and V. Banzon are presently developing a simple method for detection of dust-contaminated pixels.

3.2.4 Exception Handling

Exceptions occasionally occur in a manner that prevents operation of the algorithm, e.g., missing data in bands 15 or 16, or in a manner that would cause exceptions in algorithms using \( [\rho_w]_N \), e.g., negative values of \( [\rho_w]_N \) caused by atmospheric correction errors (particularly in the blue at high pigment concentrations where \( [\rho_w]_N \) is small). A series of flags have been developed to indicate when atmospheric correction should not be attempted, or to indicate that algorithm failed to operate of failed to provide realistic values for \( [\rho_w(\lambda)]_N \).

3.2.5 Data Dependencies

The required ancillary data is described in detail in Section 3.1.1.11. All will come to MODIS via the GSFC/DAAC. If a particular data set is not available either a nominal value, e.g., the oceanic average, or a climatology will be substituted.
### 3.2.6 Output Products

The output products are the normalized water-leaving radiances in MODIS Bands 8–14, the aerosol optical thickness $\tau_a(\lambda_l)$, $\varepsilon(\lambda_s, \lambda_l)$, and an index describing the two candidate models selected by the algorithm to perform the $[\rho_w]_N$ retrievals. At present $[L_w]_N^{\text{Field}}$ rather than $[L_w]_N^{\text{Exact}}$ is provided to facilitate comparison with measurements made at MOBY. Based on our observations that the combination of $\varepsilon(\lambda_s, \lambda_l) \sim 1$ and small $\tau_a(\lambda_l)$ yields a very good retrieval of $[\rho_w]_N$, while $\varepsilon(\lambda_s, \lambda_l) \sim 1.2$ and large $\tau_a(\lambda_l)$ may yield a poor retrieval, it may be possible to develop a quality index based on a combination of the values of $\varepsilon(\lambda_s, \lambda_l)$ and $\tau_a(\lambda_l)$. 
4.0 Assumptions and Constraints

In this section we describe the assumptions that have been made and how they may influence the resulting $[\rho_w]_N$. We also provide a list of situations in which the algorithm cannot be operated.

4.1 Assumptions

The principal assumption is the validity of the aerosol models used for the implementation of the algorithm, i.e., in developing the lookup tables described in Section 3.1.1.3. We have seen in Section 3.1.1.4 that the algorithm will work well if the models are a reasonable approximation to nature, but if they are unrealistic, i.e., mineral dust without absorption, the error in $[\rho_w]_N$ can be excessive (Figure 12). In fact, Figure 12 shows that it is of vital importance to have the correct absorptive properties of the aerosol. The adequacy of the aerosol models is difficult to judge. For the most part they were developed to model beam propagation, i.e., the total scattering and extinction coefficients, not the scattering phase function and the single scatter albedo. They have not been validated for these quantities; however, Schwinding [1995] showed that the aerosol off the coast of Southern California appeared to fall within the boundaries of the Shettle and Fenn [1979] aerosol models used here. Similar conclusions can be stated for the clean maritime aerosol based on the analysis of Smirnov et al. [2003]. Also, the success of SeaWiFS [Hooker and McClain, 2000] suggests that the models used here are adequate most of the time.

A second, probably less important, assumption is that the radiative transfer in the atmosphere can be adequately described by a two-layer model (aerosols in the lower layer only). Based on tests with absorbing aerosols, we know that this model will have to be changed, e.g., Saharan dust will have to be mixed higher into the atmosphere. This will require generation of new lookup tables. Such tables have been developed for Saharan dust (see Section 5.1.1).

Finally, it is assumed that at low chlorophyll $a$ concentrations the water-leaving radiance in the NIR is near zero. This is usually an excellent assumption in the open ocean; however, in very concentrated coccolithophore blooms [Balch et al., 1991; Gordon et al., 1988] it is possible that the ocean will contribute NIR radiance. The magnitude of this NIR radiance as a function of the coccolith concentration is being studied experimentally as part of a study to derive the
concentration from MODIS imagery. For routine processing, we assume that the Siegel et al. [2000] correction is sufficiently accurate to address this issue (Section 3.1.1.9).

4.2 Constraints

Although algorithm will employ the cloud mask being developed by the MODIS Atmosphere Group to indicate the presence of thin cirrus clouds; an atmospheric correction will be attempted for all imagery that is not saturated in any of Bands 8-16. Of these cloud-free pixels, the algorithm requires that they contain no land and that the estimated sun glitter contamination be below a pre-determined threshold. Also, the algorithm should not be applied closer than a distance $x$ from land (the value of $x$ is a few km) due to the adjacency effect from land pixels [Otterman and Fraser, 1979] and the possibility of sufficiently high sediment loads in the water that $[\rho_w]_N$ can not be considered negligible in the NIR.
5.0 Future Algorithm Enhancements

Section 3 describes the algorithm and its present implementation. There are, however, several planned enhancements proposed for the future. These deal mainly with the issues discussed in Section 3.1.1.13: strongly absorbing aerosols, nonuniform in-water radiance distribution effects, etc. Of the issues discussed there, development of an atmospheric correction algorithm that can deal with strongly absorbing aerosols, e.g., wind-blown desert dust and/or urban pollution, is considered to be the most important.

5.1 Strongly Absorbing Aerosols

As discussed earlier (Sections 3.1.1.4, 3.1.1.12.1, and 3.1.1.13.3) the $\rho_w$-retrieval algorithm as presently implemented (Section 3.1.2) cannot produce acceptable results in the presence of strongly absorbing aerosols. Briefly, two observations indicate how the algorithm is confounded: (1) although aerosol absorption can seriously reduce $\rho_a + \rho_{ra}$ in the visible, it is not possible on the basis of the observed TOA radiance in the NIR to infer the presence of aerosol absorption, because the spectral variation of $\rho_a + \rho_{ra}$ in the NIR depends mostly on the aerosol’s size distribution, e.g., Figure 4 (right panel); and (2) the vertical distribution of strongly absorbing aerosols profoundly influences their TOA reflectance in the visible (especially in the blue) but not in the NIR (Figure 25). In the case of mineral aerosol such as Saharan dust transported over large distances over the ocean by the winds, there is an additional complication: the dust is colored, i.e., the absorption properties of the material itself varies strongly with wavelength. Saharan dust is more absorbing in the blue and green than the red, explaining its reddish color. When such desert aerosol is in the atmosphere over the oceans, the present algorithm will seriously overestimate $\rho_a + \rho_{ra}$ in the blue and therefore underestimate $\rho_w$ there. This underestimation will appear as an elevated pigment concentration $C$. Interestingly, there are observations suggesting that mineral aerosols, by virtue of the trace nutrients they supply when they settle out of the atmosphere into the water, can actually induce an increase in primary productivity and elevate the pigment concentration [Young et al., 1991]. Thus, observation of an elevated pigment concentration could be the result of a poor atmospheric correction and/or “fertilization” of the water by the aerosol itself. Clearly, a robust $\rho_w$-retrieval algorithm for areas subjected to desert dust is of paramount importance.
The fact that the absorption properties cannot be determined on the basis of the observations of $\rho_a + \rho_{ra}$ in the NIR means that observations in the visible are required as well. However, in the visible (especially in the blue) $\rho_w$ can be significant, and cannot be estimated a priori. This suggests that the retrieval of $\rho_w$ (or the pigment concentration) and the atmospheric correction (retrieval of $\rho_a + \rho_{ra}$) must be carried out simultaneously. As retrieval of $\rho_a + \rho_{ra}$ in the existing algorithm requires aerosol models, retrieval of $\rho_w$ will require an optical model of the ocean. Two algorithms, based on simultaneous determination of oceanic and atmospheric properties, that show promise in dealing with absorbing aerosols have been developed [Chomko and Gordon, 1998; Gordon, Du and Zhang, 1997b]. In the following, these two approaches are described and some results of their application to ocean color imagery is provided.

5.1.1 The Spectral Matching Algorithm

The “spectral matching algorithm” is described in detail in Gordon, Du and Zhang [1997b]. In this algorithm, the properties of the ocean and the atmosphere are retrieved simultaneously. Briefly, assuming that $[\rho_w(\lambda_i)]_N = 0$ (an assumption that can be relaxed as we will see later), $\rho_t(\lambda_i) - \rho_r(\lambda_i)$ provides $\rho_a(\lambda_i) + \rho_{ra}(\lambda_i)$. Now, given an aerosol model (the $i^{th}$) one can find the value of the aerosol optical depth, $\tau_a^{(i)}(\lambda_i)$, that reproduces $\rho_a(\lambda_i) + \rho_{ra}(\lambda_i)$. Then from $\tau_a^{(i)}(\lambda_i)$ and the model, $\rho_a^{(i)}(\lambda_j) + \rho_{ra}^{(i)}(\lambda_j)$ and $t^{(i)}(\theta, \lambda_j)$ can be determined for all spectral bands $j$. This provides the quantity

$$t(\theta, \lambda_j)\rho_w^{(i)}(\lambda_j) = \rho_t(\lambda_j) - \rho_r(\lambda_j) - \rho_a^{(i)}(\lambda_j) - \rho_{ra}^{(i)}(\lambda_j)$$

retrieved assuming that the $i^{th}$ aerosol model is correct. At this point the Gordon et al. [1988] two-parameter model of the water-leaving reflectance that uses the pigment concentration, $C$, and a pigment-related scattering parameter at 550 nm, $b_0$, is employed to compute $[\rho_w(\lambda)]_N$ for a discrete set of values of $C$ and $b_0$ that fall within the typical range of variation. The residual

$$\delta(i, C, b_0) \equiv 100\% \sqrt{\frac{1}{n-1} \sum_{j=1}^{n} \left( \frac{t^{(i)}(\theta, \lambda_j) t^{(i)}(\theta_0, \lambda_j) [\rho_w(\lambda_j)]_N - t(\theta, \lambda_j) \rho_w^{(i)}(\lambda_j)}{t^{(i)}(\theta_0, \lambda_j) t^{(i)}(\theta_0, \lambda_j) [\rho_w(\lambda_j)]_N} \right)^2},$$

where $n$ is the number of visible wavelengths, is computed for each model and set of ocean parameters. One might suggest that the set of parameters $i$, $C$, and $b_0$, that yield the smallest $\delta(i, C, b_0)$ should be chosen as the best, i.e., the solution the problem; however, as it is unlikely that the
“correct” model is one of the set of candidates, Gordon, Du and Zhang [1997b] suggest averaging for the ten best retrievals (ten retrievals with the lowest values of \( \delta(i, C, b_0) \)) to obtain the retrieved ocean and aerosol parameters. Extensive tests using simulated pseudo data with Urban models as representative of strongly-absorbing aerosols suggest that this approach is capable of excellent retrievals in the presence of either weakly- and strongly-absorbing aerosols [Gordon, Du and Zhang, 1997b]. Of particular importance is that the algorithm has no difficulty indicating the presence of strongly absorbing aerosols. The algorithm can also incorporate vertical structure by having candidate models with any prescribed vertical structure.

An important feature of this algorithm is that it can be configured to use the same LUTs as the standard algorithm, and therefore could be run concurrently with it. Thus, at a minimum, it could be operated at reduced resolution (say every tenth line and every tenth pixel) to provide a flag for indicating the presence of absorbing aerosols. An unattractive feature of the algorithm is that it requires realistic aerosol models to effect the correction, i.e., the better the models approximate the real aerosol, the better the parameter retrievals. Obviously the results depend on the quality of the ocean model.

In the Atlantic and Indian Oceans, a predominant absorbing aerosol in the marine atmosphere is the mineral dust coming from Africa [Herman et al., 1997]. This dust is strongly absorbing in the blue because it contains ferrous minerals [Patterson, 1981]. In addition, the impact of this absorption is very dependent on the vertical distribution of the aerosol (Section 3.1.1.12.1). This is of primary importance for Saharan dust [Moulin et al., 2001a]. Because of these difficulties, the present MODIS and SeaWiFS algorithms do not process pixels if high \( \rho_v \) is detected in the NIR. The quasi-permanent presence of dust degrades satellite ocean color products in the Tropical Atlantic and Arabian Sea where large areas are not sampled, sometimes for as long as an entire month. An example from the Arabian Sea (SeaWiFS) is provided in Figure 32. It shows that almost the entire Arabian Sea is unsampled during the Southwest Monsoon because of dust from Africa. This failure of the atmospheric correction also prevents observation of the potential fertilization effect due to the supply of nutrients contained in dust to the surface water [Young et al., 1991]. Moulin et al. [2001b] have reported a technique for atmospheric correction through African dust, based in the spectral matching algorithm (SMA), that allows retrieval of \( [\rho_w]_N \) and the chlorophyll concentration at dust
optical depths as high as 0.8. Bazon et al. [2004] have used this algorithm to process the SeaWiFS imagery from the Arabian Sea during 2000 shown in Figure 33 in a novel manner. SMA was used to select the best aerosol model from a set of 18 developed for use in this region [Moulin et al., 2001a]. The selected model was then used to subtract the aerosol component from the imagery yielding the normalized water-leaving reflectance. These values of $[\rho_w]_N$ were used as input to the now-standard SeaWiFS OC4v4 bio-optical algorithm to estimate the concentration of chlorophyll a (Chl). The comparison with the standard SeaWiFS algorithm is striking – there is a dramatic increase in coverage during the monsoon period that clearly reveals the enhanced productivity unseen in the standard processing.

The aerosol models for use in Saharan dust [Moulin et al., 2001a] were developed using SeaWiFS because of its significantly higher saturation radiance than MODIS in the ocean bands. They provide an example of tailoring aerosol models to reproduce actual satellite imagery. The derived optical properties were later found to be consistent with surface-based sky radiance retrievals of the single scattering albedo of Saharan dust [Catrall, Carder and Gordon, 2003].

Application of the SMA to MODIS is straightforward only at low dust concentrations because of the low saturation radiances of the ocean bands; however, the possibility exists of using the NIR MODIS land bands in conjunction with the SMA to derive $[\rho_w]_N$ for pixels that do not saturate in the blue and green. This is the subject of a future study.

5.1.2 The Spectral Optimization Algorithm

The “spectral optimization algorithm” (SOA) is described in detail in Chomko and Gordon [1998]. As in the spectral matching algorithm, the properties of the ocean and the atmosphere are retrieved simultaneously. In contrast to the spectral matching algorithm, no attempt is made to use realistic aerosol models, i.e., aerosol models described by the overly-simple power-law size distributions [Eq. (11)] are employed to derive the ocean properties. Briefly, for a given value of the parameter $\nu$ of the power-law distribution, assuming the particles are spherical, and ignoring the aerosol vertical distribution for the moment, the aerosol reflectance $\rho_a(\lambda) + \rho_{ra}(\lambda)$ depends only on the real ($m_r$) and imaginary ($m_i$) parts of the aerosol refractive index and the aerosol optical
Year 2000: SeaWiFS Monthly Chl \( \alpha \)

Standard processing leads to data gaps due to cloud/dust masking.

Figure 32. Monthly concentration of chlorophyll \( \alpha \) derived from SeaWiFS imagery using the standard atmospheric correction algorithm [Gordon and Wang, 1994a].

Year 2000: SMA Monthly Chl \( \alpha \)

SMA processing leads to greater coverage during the summer months.

Figure 33. Monthly concentration of chlorophyll \( \alpha \) derived from SeaWiFS imagery using the spectral matching algorithm [Moulin et al., 2001b].
depth ($\tau_w(\lambda_t)$). The values of $m_r$ and $m_i$ are assumed to be independent of $\lambda$, so such a model will apply only to wavelength-independent absorbing aerosols, e.g., carbonaceous. As in the spectral matching algorithm, the water contribution to the TOA reflectance depends on the parameters $C$ and $b_0$ through the Gordon et al. [1988] reflectance model. Nonlinear optimization is then used to determine the values of these parameters.

Application to SeaWiFS imagery off the U.S. East Coast has been presented by Chomko and Gordon [2001]. It showed consistent retrieved water properties between days with turbid and clear atmospheres. Unfortunately, because the bio-optical model differed considerably from that for the standard SeaWiFS processing, an unbiased comparison of the SOA and SeaWiFS ocean products was not possible. Rather than discussing these results in detail, we will present a version of the SOA that is improved through the addition of a more complete bio-optical model.

In the Chomko et al. [2003] version of the SOA, the Gordon et al. [1988] bio-optical model is replaced by the Garver and Siegel [1997] model as modified by Maritorena, Siegel and Peterson [2002]. In this model (which henceforth we refer to as “GSM01”) of Case 1 waters there are three constituent parameters (as opposed to two in Gordon et al. [1988]): $a_{ph}(443)$, the absorption coefficient of phytoplankton at 443 nm; $a_{cdm}(443)$, the sum of the absorption coefficients of dissolved and suspended detrital material at 443 nm; and $b_{bp}(443)$, the backscattering coefficient of suspended particles at 443 nm. The spectral variation of these components is given by

$$a_{ph}^\ast(\lambda) = a_{ph}^\ast(\lambda) C,$$

$$a_{cdm}(\lambda) = a_{cdm}(443) \exp[-S(\lambda - 443)],$$

$$b_{bp}(\lambda) = b_{bp}(443) \left(\frac{443}{\lambda}\right)^n,$$

where $a_{ph}^\ast(\lambda)$ is the specific (to $C$) absorption spectrum of phytoplankton. The parameters $a_{ph}^\ast(\lambda)$, $S$ and $n$ have been determined by Maritorena, Siegel and Peterson [2002] through an optimized fit to surface data for Case 1 waters. Thus, $\rho_w$ is a function of $C$, $a_{cdm}(443)$, and $b_{bp}(443)$. We follow Chomko et al. [2003] and write the model-estimated value of $[\rho_w(\lambda)]_N$ functionally as

$$[\tilde{\rho}_w(\lambda)]_N = [\tilde{\rho}_w(\lambda, C, a_{cdm}(443), b_{bp}(443))]_N.$$

The size distribution for the aerosol model is Junge power-law distribution. The same limits, $D_0$, $D_1$, and $D_2$, are used as in Eq. (11), so the modeled aerosol contribution to the reflectance
\( \hat{\rho}_A \equiv \hat{\rho}_a + \hat{\rho}_ra \) will be a function of the solar-viewing geometry, \( m_r, m_i, \nu, \) and \( \tau_a \). Functionally,

\[
\hat{\rho}_A = \hat{\rho}_A(G, \lambda, m_r, m_i, \nu, \tau_a(\lambda)),
\]

where \( G \) represents the parameters associated with the sun-viewing geometry, e.g., \( \theta_0, \theta_v, \) etc. In the SOA, \( m_r \) is either 1.50 or 1.333, and \( m_i = 0, 0.001, 0.003, 0.010, 0.030, \) and 0.040. The parameter \( \nu \) ranges from 2.0 to 4.5 in steps of 0.5. Thus there are 72 separate aerosol models (2 values of \( m_r \times 6 \) values of \( m_i \times 6 \) values of \( \nu \)). For each of these models, \( \hat{\rho}_A \) is computed as a function of the aerosol optical thickness \( \tau_a(\lambda) \) for a wide range of viewing and solar geometries and fit to a quartic expression

\[
\hat{\rho}_A(G, \lambda, m_r, m_i, \nu, \tau_a(\lambda)) = a(G, \lambda, m_r, m_i, \nu)\tau_a(\lambda) \\
= b(G, \lambda, m_r, m_i, \nu)\tau_a^2(\lambda) \\
= c(G, \lambda, m_r, m_i, \nu)\tau_a^3(\lambda) \\
= d(G, \lambda, m_r, m_i, \nu)\tau_a^4(\lambda),
\]

and the quantities \( a, b, c, \) and \( d \), are stored in the form of lookup tables. Similarly, the diffuse transmittances \( t^*(\theta_v) \equiv t_v^* \) and \( t^*(\theta_0) \equiv t_0^* \) are computed and stored in lookup tables.

After correcting \( \rho_i \) for sun glitter and whitecaps, the aerosol and water contribution to the reflectance in a particular geometry is given by

\[
\rho_{Aw}(G, \lambda) = \rho_i(G, \lambda) - \rho_v(G, \lambda),
\]

where

\[
\rho_{Aw}(G, \lambda) = \rho_A(G, \lambda) + t_v(G, \lambda)\rho_w(G, \lambda).
\]

The modeled counterpart of \( \rho_{Aw} \) is then

\[
\hat{\rho}_{Aw}(G, \lambda, m_r, m_i, \nu, \tau_a(\lambda), C, a_{cdm}(443), b_{bp}(443)) \equiv \hat{\rho}_A(G, \lambda, m_r, m_i, \nu, \tau_a(\lambda)) \\
+ \hat{t}_v(G, \lambda, m_r, m_i, \nu, \tau_a(\lambda)) \\
\times \hat{t}_0(G, \lambda, m_r, m_i, \nu, \tau_a(\lambda)) \\
\times [\hat{\rho}_w(\lambda, C, a_{cdm}(443), b_{bp}(443))]_N.
\]

As in the SMA, it is assumed that the water-leaving reflectance in the NIR (i.e., at \( \lambda_s \) and \( \lambda_t \)) is negligible (this is relaxed later). This allows the direct estimation of \( \nu \) and \( \tau_a(\lambda_t) \) from determinations of \( \rho_{Aw}(\lambda_s) \) and \( \rho_{Aw}(\lambda_t) \). Thus for each index set \( (m_r, m_i) \) the values of \( \nu \) and \( \tau_a(\lambda_t) \) that
exactly reproduce $\rho_{\text{AW}}(\lambda_s)$ and $\rho_{\text{AW}}(\lambda_l)$ are determined. This results in 12 combinations $(\nu, \tau_a)$ from which the functions $\nu = \nu(m_r, m_i)$ and $\tau_a = \tau_a(m_r, m_i)$ are found through interpolation. Then the quantity

$$\sum_{\lambda_i} \left\{ \hat{\rho}_{\text{AW}}(G, \lambda_i, m_r, m_i, \nu, \tau_a, C, a_{\text{cdm}}(443), b_{bp}(443)) - \rho_{\text{AW}}(G, \lambda_i) \right\}^2,$$

where the sum is over the remaining spectral bands, is minimized subject to the constraints $\nu = \nu(m_r, m_i)$ and $\tau_a = \tau_a(m_r, m_i)$, using standard optimization techniques, to find the other 5 parameters. In effect, we have optimized for 7 parameters: $C, a_{\text{cdm}}(443), b_{bp}(443), m_r, m_i, \nu$, and $\tau_a(\lambda_l)$.

The SOA algorithm has been applied to a full resolution SeaWiFS image from the Middle Atlantic Bight (MAB) acquired on Day 279 of 1997 [Chomko et al., 2003]. SeaWiFS was used rather than MODIS because the calibration difficulties associated with MODIS made testing new algorithms difficult. As described in Chomko and Gordon [2001], the atmosphere over the MAB on this day was quite turbid with $\tau_a(865)$ exceeding 0.2 over large portions of the image. Retrieved images of $C$ and $a_{\text{cdm}}(443)$ are shown in Figure 34. A partial validation of this algorithm was

![Figure 34](image)

Figure 34. $C$ (left panel) and $a_{\text{cdm}}(443)$ (right panel) retrieved from SeaWiFS imagery obtained on day 279, 1997. ($C$-scale is logarithmic and labels are 0.05, 0.10, 0.30, 0.50, 1.00, and 1.50 mg/m$^3$.) ($a_{\text{cdm}}$-scale is logarithmic and labels are 0.003, 0.010, 0.030, 0.100, and 0.300 m$^{-1}$.)

effected by comparing the retrieved $C$ with that from the standard SeaWiFS 8-day mean $C$ that included Day 279. The results were in excellent agreement. The retrieved $a_{\text{cdm}}$ was compared with
measurements of the absorption coefficient of the \textit{dissolved} portion of the detritial material made using the Airborne Oceanographic Lidar (AOL) [Hoge et al., 1995] along the flight line on the right panel of the figure. The agreement was also excellent in the open ocean, with areas of disagreement near the coast explained by the variability of the parameter $S$ (not considered in the algorithm) from the coastal to the open ocean regime.

An important aspect of the SOA is the ease with which it can be extended to Case 2 waters. A major difficulty for atmospheric correction in Case 2 waters is that the assumption that $\rho_w = 0$ in the NIR is rarely valid. In fact, $\rho_w$ is often large in the NIR because of the presence of high quantities of suspended sediment. Extension of the algorithm to the cases where $\rho_w \neq 0$ in the NIR is immediate: operate the algorithm in an iterative manner, where at each stage in the iteration, water-leaving reflectance in the NIR is computed from the derived bio-optical parameters from the previous iteration. We have tested this idea in the sediment-dominated Case 2 waters of Pamlico Sound, NC. Figure 35 shows the two retrieved parameters of the aerosol model $\nu$ (upper panel), the free parameter in the power-law size distribution, and $\omega_0$ (lower panel), the aerosol single scattering albedo. Neither of these atmospheric parameters would be expected to be very different over the Sound and over the near-by ocean, i.e., we would expect continuity in both going from the Sound into the open ocean. Figure 35 shows that when the algorithm is operated in the Case 1 mode $\omega_0$ is lower and $\nu$ is higher over the Sound than the off-shore waters. In contrast, almost complete continuity is observed when the algorithm is operated in the Case 2 mode. This suggests that atmospheric correction was achieved in these turbid Case 2 waters. In this case, the quality of the retrieved bio-optical properties will be completely determined by the quality of the bio-optical model.

We believe that it should be possible to tune the Garver and Siegel [1997] model parameters to the particular Case 2 waters under examination to retrieve bio-optical parameters; however, such tuning will have to be site specific and season specific. We are in the process of attempting validation of this algorithm for the Case 2 waters of the Chesapeake Bay, and have begun implementation in the MODIS processing environment.
Figure 35. Comparison of the retrieved values of $\nu$ (upper panel) and $\omega_0$ (lower panel) between Case 1 and Case 2 processing with the SOA. Note that the atmospheric parameters are virtually unchanged in going from the open ocean to the coastal waters with the Case 2 processing.
5.2 Other Enhancements

There are several other enhancements that require further study, but that should be implemented when the studies are complete.

5.2.1 Use actual $L_u(\theta_v, \phi_v)$ in the computation of $t$.

Presently, the diffuse transmittance $t$ is computed by assuming the distribution $L_u(\theta_v, \phi_v)$ is uniform, i.e., independent of $\theta_v$ and $\phi_v$. When a valid distribution model is available, $t^*$ should be replaced by the correct $t$. The Morel, Antoine and Gentili [2002] model of the angular distribution of $L_u$ is being used to correct $\rho_w$ for bidirectional effects. As described in Section 3.1.1.13.4, we are in the process of attempting to validate this model using our own measurements of the upwelling subsurface radiance distribution. An example of this validation attempt is presented in Figure 36.

This shows that the Morel, Antoine and Gentili [2002] model is excellent in the principal plane in

![Figure 36](image-url)

Figure 36. Comparison of the $L_u$ model of Morel, Antoine and Gentili [2002] (open symbols) with experimental measurements (filled symbols) in the principal plane (plane containing the sun and the zenith). Measurement conditions: 440 nm, $\theta_0 = 38^\circ$, $C = 10.1$ mg/m$^3$.

the direction of the sun, but fails in the direction opposite to the sun. It also provides an example
of the magnitude of the dependence of $L_w$ on viewing direction.

5.2.2 Introduce the earth curvature effect at high latitude.

As described in Section 3.1.1.12.2 at large $\theta_0$ the influence of the curvature of the earth can be significant, especially in the computation of $\rho_r$. Ding and Gordon [1994] described a method for incorporating the earth-curvature effects, but it was not implemented. Implementation of the Ding and Gordon [1994] method, or something similar to include earth curvature, is necessary for processing high-latitude imagery in winter.

5.2.3 Cirrus Clouds.

If the 1.38 $\mu$m band (Band 26) on Aqua MODIS performs properly (as it appears to), it is important to incorporate at least a simple procedure to partially correct imagery corrupted by thin cirrus. The methods studied by Gordon et al. [1996] may not be applicable if spectral matching or spectral optimization is used to address absorbing aerosols.
References


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Fraser, R. S., Satellite measurement of mass of Sahara dust in the atmosphere, Applied Optics, 15, 2471–2479, 1976.


# Glossary

<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
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<tbody>
<tr>
<td>AERONET</td>
<td>Aerosol Robotic Network</td>
</tr>
<tr>
<td>ATBD</td>
<td>Algorithm Theoretical Basis Document</td>
</tr>
<tr>
<td>CZCS</td>
<td>Coastal Zone Color Scanner</td>
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<tr>
<td>DAAC</td>
<td>Distributed Active Archive Center</td>
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<tr>
<td>GAC</td>
<td>Global Area Coverage</td>
</tr>
<tr>
<td>GSFC</td>
<td>Goddard Space Flight Center</td>
</tr>
<tr>
<td>IOP</td>
<td>Inherent Optical Property</td>
</tr>
<tr>
<td>MOBY</td>
<td>Marine Optical Buoy</td>
</tr>
<tr>
<td>MODIS</td>
<td>Moderate-Resolution Spectroradiometer</td>
</tr>
<tr>
<td>NEΔρ</td>
<td>Noise Equivalent Reflectance</td>
</tr>
<tr>
<td>NIR</td>
<td>Near infrared (700–1000 nm)</td>
</tr>
<tr>
<td>RTE</td>
<td>Radiative Transfer Equation</td>
</tr>
<tr>
<td>SeaWiFS</td>
<td>Sea-viewing Wide-Field-of-view Sensor</td>
</tr>
<tr>
<td>SNR</td>
<td>Signal-to-noise Ratio</td>
</tr>
<tr>
<td>SRCA</td>
<td>Spectroradiometric Calibration Assembly</td>
</tr>
<tr>
<td>TBD</td>
<td>To be determined</td>
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<tr>
<td>TOMS</td>
<td>Total Ozone Mapping Spectrometer (Nimbus-7)</td>
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